
**ELECTROMAGNETIC
WAVES** **PIER 9**

**Progress
In
Electromagnetics
Research**

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Chief Editor: J. A. Kong

Bianisotropic and
Bi-isotropic Media and
Applications

Editor: A. Priou

PREFACE

The bi-isotropic and bianisotropic media are opening a new field in electromagnetics research and becoming a challenging topic covering many aspects of electromagnetic theory and applications. The first manifestation of the bi-isotropic media was revealed by the chiral media with possible applications in the microwave range. In various countries in the world many works started and various meetings and conferences were organized where results have been presented. This includes fields related to mathematics, physics, optics, chemistry, biology, and life sciences. The number of papers per year in the field is increasing very rapidly. The objective of this special issue is to present a state-of-the-art report and future trends in bianisotropic and bi-isotropic media and their applications. An attempt is made to collect theoretical and applied researches carried out in the world in the last years including works from China, Finland, France, Italy, Russia, Sweden, UK, and USA.

In Chapter 1, I. Lindell and A. Viitanen considered the problem of a plane wave propagation in the most general uniaxial bianisotropic medium, with symmetric parameter dyadics. The dispersion relations and eigenvector expressions are derived.

The formalisms of the bi-isotropic media are quite numerous and different in appearance. In Chapter 2, S. Ougier, I. Chenerie, A. Sihvola, and A. Priou classified the various constitutive relations that have been employed and established the links between them. In Chapter 3, F. Guerin examined three different formalisms commonly used for describing wave propagation in reciprocal bi-isotropic media and make comparisons with respect to the question of energy dissipation. The author presented the influence of the chirality parameter on the reflection coefficient and the possibility of obtaining absorbing material with new properties.

The contribution of A. Sihvola in Chapter 4 deals with the electromagnetic modeling of bi-isotropic media. All the mixture equations for spherical and ellipsoidal inclusions were presented. This chapter includes, also, an important part on temporal dispersion effect in bi-isotropic media.

In the two following chapters the polarizabilities of a layered chiral sphere or a layered dielectric bi-isotropic ellipsoids are derived. In Chapter 5, M. Ermutlu and A. Sihvola solved the dipole moments that are induced by electromagnetic fields in a layered chiral sphere consisting of a spherical core and a spherical shell. The result is the low-frequency polarizability matrix of the sphere used for calculating the Rayleigh scattering of the object. In Chapter 6, Wei Ren derived the polarizabilities of a general layered bi-isotropic ellipsoids using a chain-matrix algorithm. The results are used in the analysis of layered bi-isotropic mixtures.

In Chapter 7, W. Yin, P. Li, and W. Wang derived the eigenfunction expansions of dyadic Green's function in unbounded and multilayered bi-isotropic media in terms of normalized cylindrical and elliptical cylinder vector wave functions. They were able to calculate the radiation characteristics of sources in stratified bi-isotropic media.

The contribution of S. He, M. Norgren, and S. Strom in Chapter 8 deals with the problem of a time-harmonic electromagnetic plane wave obliquely incident on a stratified chiral slab with multiple discontinuities in the materials parameters. Up and down-going eigenmodes are identified together with their dispersion equations. The solution for the reflection coefficient matrix is given for both a multilayered structure and a general stratified slab.

In Chapter 9, S. Tretyakov and A. A. Sochava addressed the issue of electromagnetic properties of plane layers of microstructures comprising two arrays of small metal wire elements embedded in an isotropic matrix constituting a novel uniaxial bianisotropic material. This novel structure offers possibilities for increasing shielding efficiency of screens in wide ranges of frequencies and incidence angles having applications in radar and antenna technology.

Chapter 10 by A. Toscano and L. Vegni deals with a formulation for the solution of the electromagnetic fields in vertically stratified structures with a general bianisotropic grounded slab under planar electric excitation conditions. As an application of the theory, the authors present the transmission-line representation for an unbounded pseudo chiral W medium.

In Chapter 11, Guerin presented, after a brief review of experimental studies carried out so far, a wave propagation theory in a chiral medium and the interaction of plane waves with a chiral slab. The main focus of this article is on experimental chiral media research works. The author presented on-going works related to measurements and modeling.

The three following papers are related to applications:

In Chapter 12, P. Pelet and N. Engheta, using the dyadic Green's functions and method of moments, presented theoretically the radiation properties of a center fed finite length thin-wire chirostrip antenna which can be thought of as a thin cylindrical wire antenna on a grounded substrate of lossless chiral material.

In Chapter 13, C. R. Brewitt-Taylor presented a model of a helix-loaded chiral material by computing the polarizabilities of an helix and using these elements to obtain electromagnetic constants for a homogeneous equivalent composite medium. These are in turn used to compute the reflection from a chiral radar absorbing coating.

In Chapter 14, F. Mariotte, P. Pelet, and N. Engheta presented a review of analytical and experimental studies of guided-wave structures utilizing chiral and, in general, bianisotropic materials that have been the subject of research interest for many researchers and engineers. The waveguiding elements constitute an important part of most devices and as a result the functional characteristics of these devices depend, among many factors, on guidance condition and propagation properties of guided modes in these waveguides.

In Chapter 15, M. M. I. Saadoun and N. Engheta presented in some detail theoretical study of electromagnetic properties of non-local Ω medium which they recently introduced as a generalization to the idea of pseudo-chiral Ω medium. Conceptually it consists of a composite medium with an isotropic host materials within which a large number of "stretched" Ω shaped conducting planar microstructures are embedded.

It is our hope that this special issue will provide the inspiration for developing many possible applications of these materials and participate in the terms of new devices, circuits, or systems.

As guest editor, I wish to thank Professor J. A. Kong for his guidance and constant encouragement throughout this endeavor. I would also like to express my sincere gratitude and appreciation to the authors, whose contributions are the foundations upon which this special issue is formed. Finally I would address all my thanks to all reviewers who gave their time and expertise so generously to undertake the important task of reviewing the various papers.

Alain Priou

*Paris, France
September 1994*

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