

## THEORY OF ZERO-POWER RFID SENSORS BASED ON HARMONIC GENERATION AND ORTHOGONALLY POLARIZED ANTENNAS

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**Abstract**—In this paper a novel approach is proposed to solve the issue of the absolute accuracy required by the most of the passive chip-less RFID sensors. To this purpose the sensor information is encoded as the phase difference between two signals, one of the two acting as the reference signal for the other one. First the tag receives a carrier at frequency  $f_0$ , then two equal signals at frequency  $2f_0$  are generated by means of a diode-based frequency doubler and a power divider. At this point one of the two signals is phase-shifted using a passive sensing element. Finally the  $2f_0$  signals are re-irradiated by exploiting two orthogonally polarized antennas. With this approach the sensor information can be extracted by a suitable reader equipped with two complex (I/Q) receivers. The idea will be first developed from a theoretical basis and then verified with several particular cases. The novel tag concept is compatible with paper substrate and inkjet printing technology since antennas diodes and passive sensing elements, i.e., all the main tag components, are going to be developed on paper materials.

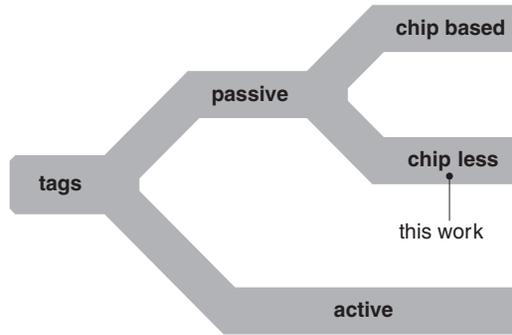
### 1. INTRODUCTION

The short-range wireless transmission of sensor information finds application in several fields ranging from the monitoring of biological parameters in medicine [1–6], to the measurements of mechanical quantities in industrial applications [7–10] and robot guidance [11]. In the last years several technologies have been developed to this purpose, but the emerging one is based on the Radio-Frequency IDentification (RFID) concept [12], due to the convergence of several new ideas

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*Received 1 September 2012, Accepted 29 October 2012, Scheduled 1 December 2012*

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**Figure 1.** Classification of the RFID tag technologies.

and approaches such as the RF-energy harvesting [13, 14], RF-carrier reuse, load modulation method, organic [15–21] and inkjet printed [22–27] electronics. The RF energy harvesting and RF-carrier reuse, for example, allow for battery-less (i.e., passive) RFID sensors that can operate for years without any maintenance.

A classification of the available tag technologies is sketched in Fig. 1. The passive systems can be divided in two families, namely: chip-based and chip-less tags. The first family exploits usually a low-power CMOS chip to implement the main tag functions (RF carrier rectification, DC voltage regulation, ASK demodulation, ID decoding, load modulation, etc.) and thus can be adapted to sensor applications by a few additional circuit blocks (signal conditioning, ADC, etc.). The main advantage of such an approach is the digital modulation of the transmitted signal, and thus the reliability of the data treatment, as shown in [28, 29]. The production costs of chip based tags are mostly associated to the heterogeneous integration of the silicon chip with the antenna [30, 31], the latter being typically fabricated on a flexible substrate or textile substrate [32–37].

In order to reduce the above mentioned costs, the chip-less tag family has been introduced and applied to wireless sensing in last years [38–43]. The chip-less RFID sensor tags exploit an antenna, the electrical properties of which are controlled by the change of the physical parameter to be measured. There are, mostly, two proposed approaches: the first is to induce a permanent change in the antenna property when a certain critical threshold (acceleration, temperature, fluid level, etc.) is exceeded [10]. The second exploits a sensing load, the impedance of which is controlled by the sensed variable, connected to an antenna [44]. In both cases the wireless sensor system (tag and reader) needs to have an absolute accuracy, this limiting the system

performance with respect to both distance and fabrication tolerances.

A different method has been recently introduced by [45]. In this paper a novel sensing principle is associated to the generation of an inter-modulation signal from a tag, the latter being illuminated by two waves at different frequencies. The advantage of this idea is that the tag response is generated at a perfectly known frequency, thus the presence or the absence of such a signal can hardly be equivocated. Similar techniques have been used in harmonic radar systems [46] and in one-bit frequency doubling tags [47].

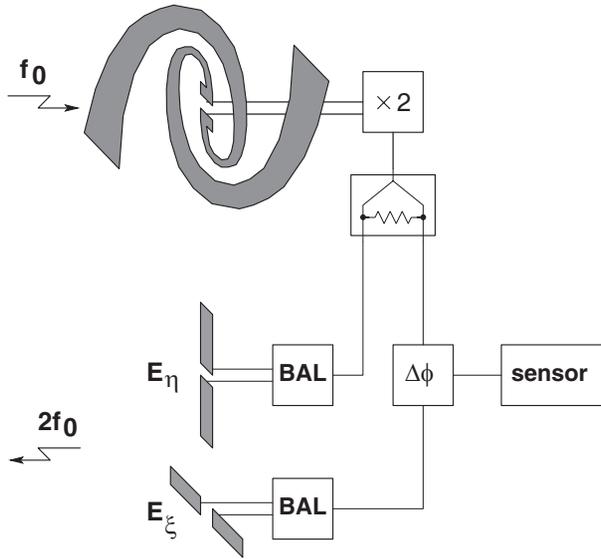
In this work a novel and original approach is proposed to solve the issue of absolute accuracy of most passive chip-less RFID sensors. To this purpose the sensor information is encoded as the phase difference between two signals, acting as the reference signal one to each other. First the tag receives a carrier at frequency  $f_0$ . Then two equal signals at frequency  $2f_0$  are generated by means of a diode-based frequency doubler and a power divider. At this point one of the two signals is phase-shifted using a passive sensing element. Finally the  $2f_0$  signals are re-irradiated by exploiting two orthogonally polarized antennas. With this approach the sensor information can be extracted by a suitable reader equipped with two complex (I/Q) receivers. The above tag concept is compatible with paper substrate and inkjet printing technology since antennas [48], diodes [49] and passive sensing elements or [50–53], i.e., all the main tag components, will be soon available on paper material. In addition, Substrate Integrated Waveguide (SIW) structures [54], a way to implement standard waveguide geometries [55] exploiting planar processes and dielectric substrates, will be soon available on paper. As a consequence, a further cost reduction of standard PCB technologies [56] could be directly achieved.

This article is organized as follows. The sensor architecture is described in Section 2 where both tag and reader sub-systems are considered. Then, Section 3 illustrates the theory of operation and the basic equations needed to recover the information. Finally the developed theory is verified in Section 4 by means of four particular cases.

## 2. SENSOR ARCHITECTURE

The proposed RFID sensor is based on the harmonic radar concept [57, 58], i.e., on tag that, being illuminated by a carrier at frequency  $f_0$ , is capable of generating the second harmonic  $2f_0$ . Such a tag, however, is also responsible for the sensor information encoding, as shown in Fig. 2.

To describe the tag operation let's consider the signal flow shown

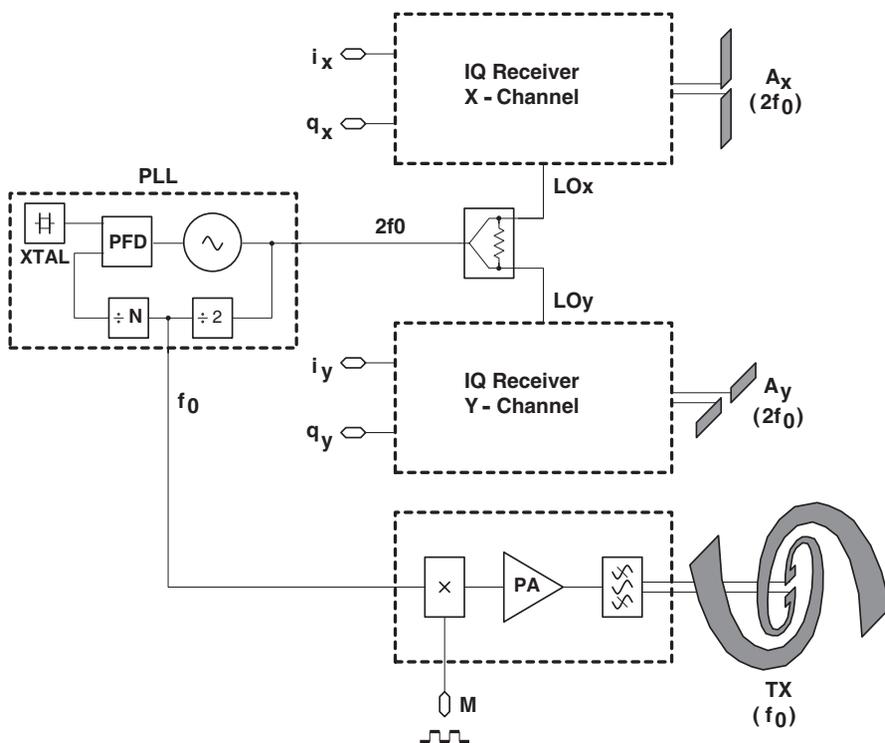


**Figure 2.** Harmonic tag block diagram.

in the same figure. The incoming electromagnetic wave at frequency  $f_0$  is received by a spiral or an helical antenna [59]. In this way the power at the antenna output is maximized regardless of the polarization or the relative reader-tag orientation. The received power is then fed into a varactor or a Schottky diode frequency doubler [60] and the second harmonic is generated. At this point the  $2f_0$  signal is split by a power divider. The first part is directly re-irradiated in vertical polarization (e.g.,  $E_\eta$  in Fig. 2) in such a way as to form a reference signal component. The second part, instead, is phase-shifted by the angle  $\Delta_\varphi$  and then re-irradiated in horizontal polarization (e.g.,  $E_\xi$  in Fig. 2). Phase shifters based on the concept proposed in [61] could, for example, be used to this purpose.

The phase angle  $\Delta_\varphi$  encodes the sensor information and must be recovered by the reader. To this purpose the reader is composed of four sub-systems, as depicted in Fig. 3. A Phase Locked Loop (PLL) oscillator is used to generate both the  $f_0$  and the  $2f_0$  signals in a synchronous way.

The  $f_0$  carrier is managed by the transmitter (TX) and serves to remotely illuminate the tag. The transmitter operates in Continuous Wave (CW) mode or exploiting a modulated carrier (see M input in Fig. 3). It is composed by a modulator and a power amplifier, the latter followed by a band-pass filter at  $f_0$  (or a stop-band filter a

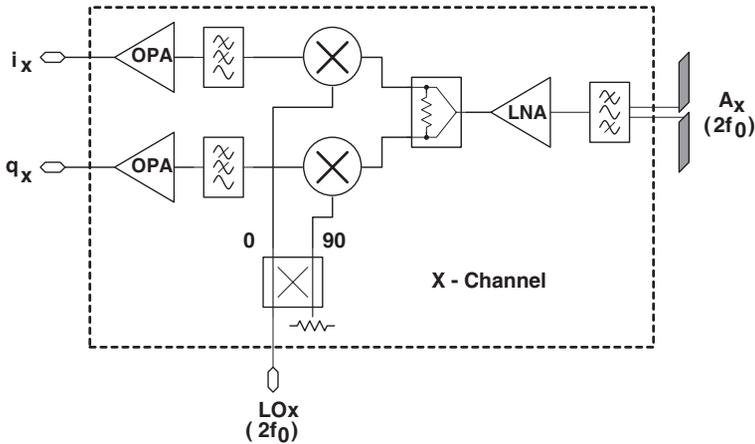


**Figure 3.** Reader block diagram.

$2f_0$ ). The filter is necessary to significantly reduce the second-harmonic generated by the power amplifier, thus eliminating the risk of blinding the receiver. The second harmonic of the TX, in-fact, should be kept below the noise floor of the receiver.

The transmitting antenna is again of spiral or helical type in order to maximize the illumination power regardless of the orientation.

The  $2f_0$  component, instead, is used as the local oscillator of the receiver. Such a signal is thus divided in two parts and applied to both the  $x$ - and  $y$ -receiver channels. Each channel is sensitive to a particular wave polarization, this by exploiting dipole antennas. In particular, the  $x$ -channel is adopted to receive the vertical polarization signal while, the  $y$ -channel is exploited for the horizontally polarized one. Because the sensor information is encoded as phase difference  $\Delta\varphi$  between the two polarizations, a vector receiver is needed for each channel. This vector receiver is based on a zero-IF In-phase and Quadrature (IQ) architecture, as illustrated in Fig. 4.



**Figure 4.** IQ receiver ( $x$ -channel) block diagram.

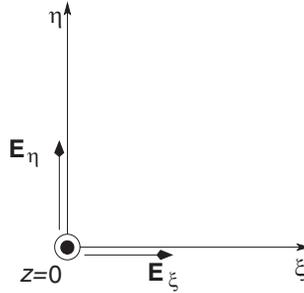
### 3. THEORY

This section is devoted to the operation theory of the novel RFID sensor system. First, the detection of the two orthogonal  $2f_0$  plane waves is considered. These waves are generated and irradiated by the tag whereas the relevant phase and amplitude information associated to them is recovered by the reader. The illumination of the tag with a carrier at  $f_0$ , the second harmonic generation and the phase information coding will be also treated in this section.

The theory will be developed under the basic assumption to have a tag antenna plane parallel to the reader antenna plane. In addition the two antenna systems will be considered axially aligned along the propagation direction. This hypothesis is satisfied in many industrial applications such as the contact-less measurement of mechanical quantities in rotating systems like engines and turbines [62] or monitoring of objects above a conveyor belt in a distribution chain. In the last case the tag is assumed to be interrogated when it is exactly perpendicular to the reader.

#### 3.1. Tag Information Encoding

The proposed RFID sensor relies on the phase and amplitude information written on two orthogonally polarized plane waves at frequency  $2f_0$ . These waves are fully determined by the knowledge of the associated electric field vectors as in Fig. 5. In particular, the  $\xi$ - $\eta$  coordinate system is used in the tag plane while the two electric fields



**Figure 5.** Coordinate system adopted in the tag plane (i.e.,  $\xi$ - $\eta$  plane) and  $2f_0$  electric field components. These electric fields are irradiated by the two equal orthogonal tag antennas.

$\mathbf{E}_\xi$  and  $\mathbf{E}_\eta$  are irradiated by two equal antennas, linearly polarized along  $\xi$  and  $\eta$  respectively.

Adopting the complex vector formalism one can write:

$$\begin{aligned} \mathbf{E}_\xi &= E_\xi e^{j\varphi_\xi} \mathbf{u}_\xi \\ \mathbf{E}_\eta &= E_\eta e^{j\varphi_\eta} \mathbf{u}_\eta \end{aligned} \tag{1}$$

where  $E_k$ ,  $\varphi_k$  and  $\mathbf{u}_k$ , with  $k = \xi, \eta$ , are the electric field amplitudes, the electric field phases and the unit vectors respectively. In particular the amplitudes  $E_k$  will be assumed real and positive having concentrated all the phase relationships between the two fields in the  $\varphi_k$  values.

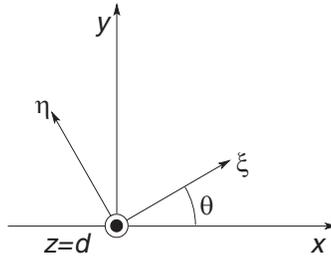
As a consequence of (1) the total electric field  $\mathbf{E}_T$ , irradiated by the tag at  $2f_0$ , is given by:

$$\begin{aligned} \mathbf{E}_T &= \mathbf{E}_\xi + \mathbf{E}_\eta \\ &= E_\xi e^{j\varphi_\xi} \left[ \mathbf{u}_\xi + \frac{E_\eta}{E_\xi} e^{j\Delta\varphi} \mathbf{u}_\eta \right] \end{aligned} \tag{2}$$

with  $E_\xi \neq 0$  and  $\Delta\varphi$  being the phase difference between the two fields:

$$\Delta\varphi = \varphi_\eta - \varphi_\xi \tag{3}$$

It is worth noticing that (2) is the general expression for an elliptical polarized plane wave. As particular cases both purely linear ( $\Delta\varphi = 0, \pi$ ) and purely circular ( $E_\eta/E_\xi = 1$  and  $\Delta\varphi = \pm\pi/2$ ) polarizations are allowed. This means that the relevant tag information can be encoded either in the phase difference  $\Delta\varphi$  or in the amplitude ratio  $E_\eta/E_\xi$ .



**Figure 6.** Coordinate system adopted in the reader plane (i.e.,  $x$ - $y$  plane). The reader plane is parallel to the tag plane. The tag  $\xi$ - $\eta$  coordinate system is rotated by an angle  $\vartheta$  with respect to the reader  $x$ - $y$  coordinate system. The distance between reader and tag is equal to  $d$ .

### 3.2. Received Reader Voltages

Let's now consider a reader placed at a distance  $d$  from the tag. The reader exploits two equal linear polarized antennas in orthogonal directions to detect the elliptical polarized wave generated by the tag. This situation is summarized in Fig. 6, where the reader antenna plane has been assumed parallel to the tag antenna plane. In this scheme the two reader antennas are placed along the  $x$ - and the  $y$ -axis. Moreover, an angle  $\vartheta$  is formed between  $\xi$ - and  $x$ -axis. Such an angle will, in general, not be known since it depends on the way the tag is attached to the object to be monitored.

As a final assumption let us consider the case when the reader and the tag antenna systems are perfectly aligned along a common  $z$ -axis. In this case the electric field at the reader location  $\mathbf{E}_R$  is simply given by the tag field  $\mathbf{E}_T$  multiplied for the transfer function of the channel:

$$\mathbf{E}_R = \alpha e^{-j\beta d} \mathbf{E}_T \quad (4)$$

where  $\alpha$  is the path loss,  $\beta$  is the propagation constant and  $d$  is the reader-tag distance. If a free-space radiation model can be applied to the considered problem,  $\alpha$  and  $\beta$  are:

$$\alpha = \frac{\lambda}{4\pi d} \sqrt{D_R D_T}$$

$$\beta = \frac{2\pi}{\lambda}$$

In (5) the wavelength  $\lambda$  is evaluated at  $2f_0$ , whereas  $D_R$  and  $D_T$  are the reader and the tag antenna directivity, respectively. The electric field

at the reader location  $\mathbf{E}_R$  can then be projected along the  $x$ -oriented receiver antenna:

$$\begin{aligned} E_x &= \mathbf{E}_R \cdot \mathbf{u}_x \\ &= E_0 \left[ \mathbf{u}_\xi \cdot \mathbf{u}_x + \frac{E_\eta}{E_\xi} e^{j\Delta\varphi} \mathbf{u}_\eta \cdot \mathbf{u}_x \right] \end{aligned} \quad (5)$$

similarly, for the  $y$ -oriented receiver antenna one gets:

$$\begin{aligned} E_y &= \mathbf{E}_R \cdot \mathbf{u}_y \\ &= E_0 \left[ \mathbf{u}_\xi \cdot \mathbf{u}_y + \frac{E_\eta}{E_\xi} e^{j\Delta\varphi} \mathbf{u}_\eta \cdot \mathbf{u}_y \right] \end{aligned} \quad (6)$$

In (5) and (6) the phasor  $E_0$  is defined as:

$$E_0 = \alpha e^{j(\varphi_\xi - \beta d)} E_\xi \quad (7)$$

Considering that the projections of the  $\xi$  and  $\eta$  unity vectors along the  $x$  and  $y$  directions are given by:

$$\begin{aligned} \mathbf{u}_\xi \cdot \mathbf{u}_x &= \cos \vartheta \\ \mathbf{u}_\eta \cdot \mathbf{u}_x &= -\sin \vartheta \\ \mathbf{u}_\xi \cdot \mathbf{u}_y &= \sin \vartheta \\ \mathbf{u}_\eta \cdot \mathbf{u}_y &= \cos \vartheta \end{aligned} \quad (8)$$

one obtains:

$$E_x = E_0 \left[ \cos \vartheta - \frac{E_\eta}{E_\xi} e^{j\Delta\varphi} \sin \vartheta \right] \quad (9)$$

$$E_y = E_0 \left[ \sin \vartheta + \frac{E_\eta}{E_\xi} e^{j\Delta\varphi} \cos \vartheta \right] \quad (10)$$

The  $E_x$  and  $E_y$  fields can be finally related to the received voltages processed by the two reader's channels. To this purpose one can exploit the effective antenna length  $l_e$  as defined in [63, p. 305]. The input received voltages are:

$$V_k^i = l_e E_k \quad (11)$$

where  $k = x, y$  and the apex  $i$  stands for input. If, for example, an half-wave dipole antenna is considered, the maximum  $l_e$  is:

$$l_e = \frac{\lambda}{\pi} \quad (12)$$

which is smaller than  $\lambda/2$  due to the sinusoidal distribution of the current along the dipole itself. Inserting (9) and (10) in (11) and using the Euler's formula to express  $e^{j\Delta\varphi}$  one gets:

$$V_x^i = l_e E_0 (A_x + jB_x) \quad (13)$$

$$V_y^i = l_e E_0 (A_y + jB_y) \quad (14)$$

where the  $A$  and  $B$  quantities contain all the relevant tag information, i.e.,  $\Delta\varphi$ ,  $E_\eta/E_\xi$  and  $\vartheta$ :

$$A_x = \cos \vartheta - \frac{E_\eta}{E_\xi} \cos \Delta\varphi \sin \vartheta$$

$$A_y = \sin \vartheta + \frac{E_\eta}{E_\xi} \cos \Delta\varphi \cos \vartheta \quad (15)$$

$$B_x = -\frac{E_\eta}{E_\xi} \sin \Delta\varphi \sin \vartheta$$

$$B_y = \frac{E_\eta}{E_\xi} \sin \Delta\varphi \cos \vartheta \quad (16)$$

The time-domain signals are easily obtained from the phasors in (13), (14) and considering the expression of  $E_0$  quoted in (7). The  $x$ -channel input voltage is given by:

$$v_x^i(t) = \Re \{ V_x^i e^{j2\omega_0 t} \} = V_0 \Re \{ (A_x + jB_x) e^{j(2\omega_0 t + \varphi_\xi - \beta d)} \}$$

$$= V_0 [A_x \cos(2\omega_0 t + \varphi_\xi - \beta d) - B_x \sin(2\omega_0 t + \varphi_\xi - \beta d)] \quad (17)$$

$V_0$  being the amplitude of the input referred voltage:

$$V_0 = l_e |E_0| = \alpha l_e E_\xi \quad (18)$$

Similarly,  $y$ -channel input voltage can be written as:

$$v_y^i(t) = V_0 [A_y \cos(2\omega_0 t + \varphi_\xi - \beta d) - B_y \sin(2\omega_0 t + \varphi_\xi - \beta d)] \quad (19)$$

### 3.3. Conversion Products

Once the time-domain expression have been obtained, it is quite straightforward to derive the conversion products and, from them, the in-phase  $i(t)$  and quadrature  $q(t)$  output signal components. For the  $x$ -channel one obtains:

$$i_x(t) = \text{LPF} \{ 2G_v^{rx} v_x^i(t) \cos(2\omega_0 t - \psi) \} = G_v^{rx} V_0 (A_x \cos \psi_R - B_x \sin \psi_R) \quad (20)$$

$$q_x(t) = \text{LPF} \{ -2G_v^{rx} v_x^i(t) \sin(2\omega_0 t - \psi) \} = G_v^{rx} V_0 (A_x \sin \psi_R + B_x \cos \psi_R) \quad (21)$$

where  $G_v^{rx}$  is the overall receiver gain,  $\psi$  is the local oscillator phase and  $\text{LPF} \{ \}$  is the low-pass operator cutting the  $4\omega_0$  mixing product. The quantity  $\psi_R$  is defined as:

$$\psi_R = \psi + \varphi_\xi - \beta d \quad (22)$$

Similarly, the  $y$ -channel outputs are:

$$i_y(t) = G_v^{rx} V_0 (A_y \cos \psi_R - B_y \sin \psi_R) \quad (23)$$

$$q_y(t) = G_v^{rx} V_0 (A_y \sin \psi_R + B_y \cos \psi_R) \tag{24}$$

In the case of a modulated carrier (signal injected at the M input in Fig. 3), (20)–(24) represent the amplitude of the base-band signal at the receiver output. As a final observation it is worth noticing that the same receiver gain  $G_v^{rx}$  and local oscillator phase  $\psi$  have been assumed for both the  $x$  and the  $y$  reader’s channels. In practice this condition can be met by calibrating the two receivers with a set of preliminary measurements.

### 3.4. Information Recovery

The relationships (20), (21) and (23), (24) constitute a set of 4 equations that can be written at each time instant. The known terms are given by the in-phase and quadrature signals at the output of the two reader’s channels, i.e., by measurable values. The unknowns are the received amplitude  $V_0$ , the overall received phase  $\psi_R$  and the tag quantities, namely:  $\vartheta$ ,  $\Delta\varphi$  and  $E_\eta/E_\xi$ . As a results 5 unknowns are obtained, this means that additional knowledge of the system is needed. For example, if the tag is designed to have a determined  $E_\eta/E_\xi$  ratio, all the information is encoded within  $\Delta\varphi$ .

In order to eliminate  $V_0$  and  $\psi_R$  from the above system of equations the following ratio is computed at each time instant:

$$U = U_R + jU_I = \frac{i_x + jq_x}{i_y + jq_y} \tag{25}$$

Developing the above expression one obtains:

$$U_R = \frac{i_x i_y + q_x q_y}{i_y^2 + q_y^2} = \frac{A_x A_y + B_x B_y}{A_y^2 + B_y^2} \tag{26}$$

$$U_I = \frac{q_x i_y - i_x q_y}{i_y^2 + q_y^2} = \frac{B_x A_y - A_x B_y}{A_y^2 + B_y^2} \tag{27}$$

The  $U_R$  and  $U_I$  values can be directly evaluated from the measured output voltages (known terms), whereas the tag unknowns are within the  $A$  and  $B$  quantities. The relationship between  $U_R$ ,  $U_I$  and these unknowns can be found by inserting Equations (15), (16) in (26), (27). After some manipulation one obtains:

$$U_R = \frac{1}{D_u} \left\{ \left[ 1 - \left( \frac{E_\eta}{E_\xi} \right)^2 \right] \cos \vartheta \sin \vartheta + \frac{E_\eta}{E_\xi} \cos \Delta\varphi (\cos^2 \vartheta - \sin^2 \vartheta) \right\} \tag{28}$$

$$U_I = -\frac{1}{D_u} \frac{E_\eta}{E_\xi} \sin \Delta\varphi \tag{29}$$

where the denominator  $D_u$  is given by:

$$D_u = \sin^2 \vartheta + \left( \frac{E_\eta}{E_\xi} \right)^2 \cos^2 \vartheta + 2 \frac{E_\eta}{E_\xi} \cos \vartheta \sin \vartheta \cos \Delta\varphi \quad (30)$$

#### 4. RESULTS

The results of the above general theory will now be analyzed in a number of particular cases of practical interest. The first case is that of a tag with fixed (and a-priori known) orientation angle  $\theta$ , in which the information is encoded by the amplitude only. This assumption means that  $\Delta\varphi$  is constant, whereas  $\rho = E_\eta/E_\xi$  is varied according to the physical quantity to be measured. If  $\theta = 0$  and  $\Delta\varphi = 0$ , Equations (26), (27) reduce to:

$$U_R = \frac{E_\xi}{E_\eta} \quad (31)$$

$$U_I = 0 \quad (32)$$

As a consequence the information can immediately be derived by  $U_R$ , thus identifying a very simple method of zero-power wireless transmission of sensor data.

In the second case the tag has again a fixed orientation angle  $\theta = 0$ , but the information is encoded as a variation of the phase angle  $\Delta\varphi$  only. Here a unit amplitude ratio between the two tag channels is assumed:  $\rho = E_\eta/E_\xi = 1$ . As a result Equations (26), (27) reduce to:

$$U_R = \cos \Delta\varphi \quad (33)$$

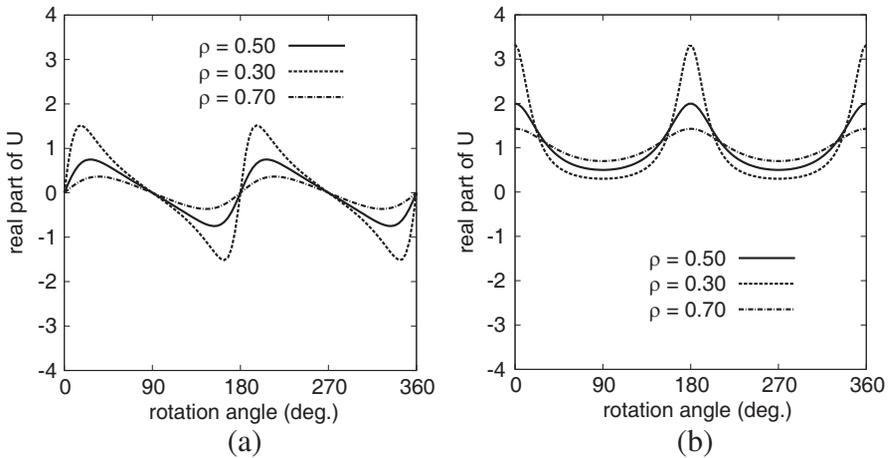
$$U_I = -\sin \Delta\varphi \quad (34)$$

Again the information can immediately be recovered from  $U_R$  and  $U_I$ . Note that a digital information could be transmitted by simply switching  $\Delta\varphi$  between 0 ( $U_R = 1, U_I = 0$ ) and  $-\pi/2$  ( $U_R = 0, U_I = 1$ ).

Let now consider a situation where  $\theta$  is not a-priori known and, possibly, variable with time. As discussed above, one can decide to encode the sensor information either in the amplitude ratio  $\rho = E_\eta/E_\xi$  or in the phase difference  $\Delta\varphi$  of the tag. The third case refers to the amplitude encoding mechanism. To this purpose  $\Delta\varphi \neq 0$  because two quantities (i.e.,  $\rho$  and  $\theta$ ) should now be extracted from the two measured quantities (i.e.,  $U_R$  and  $U_I$ ). Thus, in the third application case,  $\Delta\varphi = -\pi/2$  is considered. As a results one obtains:

$$U_R = \frac{(1 - \rho^2) \sin(2\theta)}{(1 + \rho^2) - (1 - \rho^2) \cos(2\theta)} \quad (35)$$

$$U_I = \frac{2\rho}{(1 + \rho^2) - (1 - \rho^2) \cos(2\theta)} \quad (36)$$



**Figure 7.** Real  $U_R$  and imaginary  $U_I$  parts of the  $U$  function versus the rotation angle  $\theta$ . The function is drawn in the particular case  $\Delta\varphi = -\pi/2$  and for three values of  $\rho = E_\eta/E_\xi$ . Such a parameter has been assumed in the range between 0.3 to 0.7 degrees to avoid singularities when  $\rho$  approaches zero.

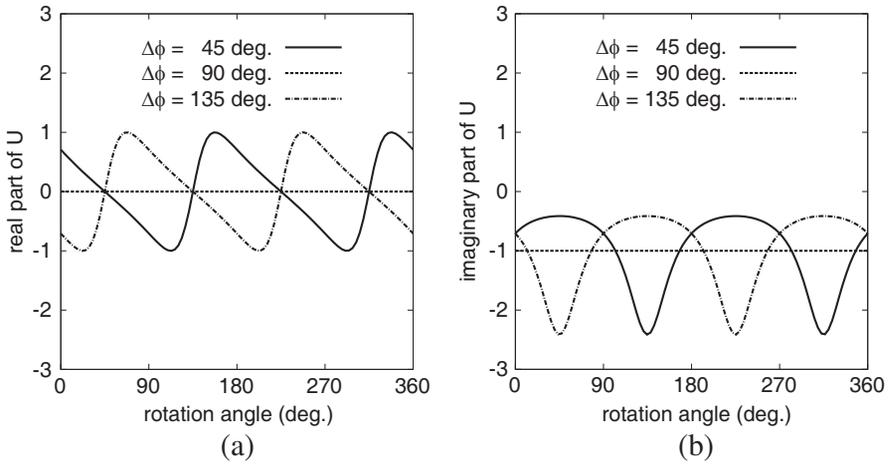
The previous equations are reported in Fig. 7 as a function of the rotation angle  $\theta$  and for  $\rho$  equal to 0.3, 0.5 and 0.7. At this point it is interesting to note that the proposed reader-tag system can be also used as a wireless rotation sensor. In such a situation the only information is the angle  $\theta$ , so it is sufficient to set  $\rho$  at a fixed value, for example  $\rho = 0.5$ .

Finally, in the fourth application case, the information is encoded in the phase difference  $\Delta\varphi$ , whereas it is extracted from the measured quantities along with the orientation angle  $\theta$ . If  $\rho = E_\eta/E_\xi = 1$ , Equations (26), (27) becomes:

$$U_R = \frac{\cos \Delta\varphi \cos (2\theta)}{1 + \cos \Delta\varphi \sin (2\theta)} \quad (37)$$

$$U_I = \frac{-\sin \Delta\varphi}{1 + \cos \Delta\varphi \sin (2\theta)} \quad (38)$$

The function  $U_R$  is singular whenever its denominator is equal to zero. This occurs for particular values of the phase  $\Delta\varphi$  (i.e., of the phase encoding the sensor information) and of the rotation angle  $\theta$ . The critical angles can easily be computed and are reported in Table 1. The function  $U_I$ , instead, is never singular since, for  $\Delta\varphi = n\pi$  with  $n$  integer, its numerator is always zero. Nevertheless, for  $\Delta\varphi$  close to the critical angles of Table 1, also the  $U_I$  values can be very high.



**Figure 8.** Real  $U_R$  and imaginary  $U_I$  parts of the  $U$  function versus the rotation angle  $\theta$ . The function is drawn in the particular case  $\rho = E_\eta/E_\xi = 1$  and for three values of  $\Delta\varphi$ . Such a parameter has been assumed in the range between 45 to 135 degrees to avoid singularities.

**Table 1.** Critical angles.

$\Delta\varphi$	$\theta$
$0, 2\pi \dots$	$\frac{3}{4}\pi, \frac{7}{4}\pi \dots$
$\pi, 3\pi \dots$	$\frac{1}{4}\pi, \frac{5}{4}\pi \dots$

The singularity problem occurs for those values of  $\Delta\varphi$  producing a purely linear wave polarization. Such a problem can always be solved in the following way. When a high value of  $U_R$  is detected, the ratio between  $(i_y + jq_y)$  and  $(i_x + jq_x)$  is evaluated instead of (25). Alternatively, the critical values of  $\Delta\varphi$  can be avoided, by conditioning the modulating signal. The latter approach is illustrated in Fig. 8, where  $U_R$  and  $U_I$  are drawn versus the rotation angle  $\theta$  and for  $\Delta\varphi$  in the 45 to 135 degrees range. It is interesting to note that  $\Delta\varphi = \pi/2$  implies a purely circular polarization and thus both  $U_R$  and  $U_I$  are independent on the rotation angle.

## 5. CONCLUSIONS

In this work a novel zero-power wireless sensor has been conceived. The sensor is based on harmonic generation and orthogonally polarized waves. The information is encoded in the phase difference or in the amplitude imbalance between two signals that are transmitted in orthogonal polarization. The mathematical development shows that the rotation angle between the sensor and the reader can also be retrieved on the basis of measurable data. Although the developed theory is absolutely general, practical applications could be well targeted in the UHF frequency range ( $f_0 = 960$  MHz and  $2f_0 = 1920$  MHz) or in the WLAN band ( $f_0 = 2.45$  GHz and  $2f_0 = 4.90$  GHz). These results demonstrate the feasibility of the proposed zero-power chip-less sensor tag and of the corresponding reader electronics.

## ACKNOWLEDGMENT

The authors wish to acknowledge the University of Perugia for supporting the patent of the system described in this paper. The invention has been filed to the Italian patent office on May 2th, 2012, file number: RM2012A000190.

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