
**ELECTROMAGNETIC
WAVES PIER 51**

**Progress
In
Electromagnetics
Research**

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**ELECTROMAGNETIC
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Chief Editor: J. A. Kong

Metamaterials Exhibiting
Left-Handed Properties and
Negative Refraction

Editor: Tomasz M. Grzegorczyk

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METAMATERIALS EXHIBITING LEFT-HANDED PROPERTIES AND NEGATIVE REFRACTION

PREFACE

This issue of the Progress in Electromagnetics Research (PIER) is a special issue on metamaterials exhibiting left-handed properties and negative refraction. These materials were first postulated theoretically in 1968, and one of their property – the negative refraction – was verified experimentally in 2001. Since then, the topic challenged all aspects of scientific research: theory, numerical simulations, and experiments. Currently, numerous teams all around the world are involved in research on left-handed materials in one or more of these aspects.

Not surprisingly, the papers gathered here originate from an extreme variety of geographical locations and discuss topics that spread over a wide spectrum of scientific interests. The volume starts by presenting some important theoretical considerations of these new substances as bulk media. Various configurations are emphasized, from infinite space, single boundary, double boundary, to closed media. It then continues by analyzing the essential building blocks of the metamaterials, currently implemented as rings and rods. Finally, it presents recent experimental works performed toward the characterization of these new materials, as well as toward some possible applications. Collectively, this volume represents an impressive body of work that reflects the breadth of topics encompassed by these substances, and their reach toward the interest of researchers worldwide. For such a contribution, I would like to thank all the authors.

All the papers in this collection have been peer reviewed. I would therefore like to extend my acknowledgments to all the reviewers for their suggestions and criticisms. Finally, I would like to thank Prof. J. A. Kong, editor of the PIER book series, for allowing me to work on the present issue.

Tomasz M. Grzegorczyk
Cambridge MA, USA
December 2004

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