Compact Dual-Band Bandpass Filter Based on Substrate Integrated Waveguide Cavity with High Selectivity

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Abstract—A compact dual-band bandpass filter implemented with an embedded coplanar waveguide (ECPW) resonator and a capacitively loaded resonator (CLR) in substrate integrated waveguide (SIW) cavity is presented and analyzed in this paper. Three transmission zeroes (TZs), of which two are located in the middle of the two passbands and one located in the upper stopband, are obtained to improve the inner-band isolation and the selectivity of the filter. The center frequencies and bandwidths of the two passbands can be easily tuned by changing the geometrical parameters of the two resonators. The proposed dual-band SIW filter is demonstrated with center frequencies located at 8.41/14.29 GHz. The measured insertion loss is $-1.28/ -1.91$ dB with the corresponding fractional bandwidth (FBW) of 21.2%/7.3%. The measured results are in good agreement with the simulated ones.

1. INTRODUCTION

Modern microwave and millimeter-wave filters are oriented towards compact size, sharp selectivity, high integration and easy manufacturability. To meet these requirements, substrate integrated waveguide (SIW) technology has been successfully applied to design filters due to its low loss and easy integration with other planar circuits [1–5]. Moreover, for the efficient utilization of spectrum resources, plenty of dual-band filters based on SIW technology have been proposed and designed [6–15]. In [6–8], several dual-mode SIW resonators are proposed to realize dual-band filters, but the sizes of these filters are relatively large. To achieve filters’ miniaturization, novel structures such as coupled complementary split-ring resonators (CSRR) [9], quadruple-folded SIW [10] and TM dielectric-loaded dual-mode cavities [11] are used to design compact dual-band SIW filters. However, these filters suffer from poor selectivity. Subsequently, many novel structures have been studied to design compact dual-band filters with high selectivity [12–15]. For instance, a dual-resonance SIW resonator structure which combines the miniaturization of the composite right/left-handed SIW with the high selectivity of the CSRR defected ground structure (DGS) is proposed to design a compact dual-band SIW filter [12]. Inverter coupled resonator sections are used in [13, 14] to introduce transmission zeroes into passbands, and dual-band SIW filters with high selectivity are obtained. In [15], a novel DGS structure with two-side loading scheme is proposed for miniaturized dual-band SIW filter designs with high selectivity. However, these proposed filters have relatively high insertion loss.

In this paper, a compact dual-band bandpass filter implemented with an embedded coplanar waveguide (ECPW) resonator and a capacitively loaded resonator (CLR) in SIW cavity is proposed. Three transmission zeroes (TZs) are generated to improve the selectivity and the isolation between the two passbands of the filter. The bandwidths and center frequencies of the two passbands can be adjusted flexibly by changing the geometrical parameters of the proposed resonators. In addition, the designed filter also features low insertion loss and broad bandwidth. Both the simulated analysis and measured results are demonstrated in details.
2. ANALYSIS AND FILTER DESIGN

2.1. The Hybrid Structure of ECPW Resonator and SIW Cavity

The configuration of the hybrid structure of the ECPW resonator and the SIW cavity is shown in Fig. 1(a). The ECPW acts as a quarter-wavelength resonator, and its resonant frequency is mainly determined by the geometrical parameters $L_2$ and $W_3$ [16]. The frequency response of the hybrid structure is simulated by Ansoft HFSS, and the corresponding result is shown in Fig. 1(b). It can be seen that the hybrid structure has three resonant frequencies in the frequency range of 0–18 GHz. The three resonant frequencies successively correspond to the TE$_{101}$ mode of the SIW cavity, the resonant frequency of the ECPW resonator and the TE$_{102}$ mode of the SIW cavity. The coupling effect between such an ECPW resonator and a SIW cavity has been analyzed detailedly in [16]. It has been demonstrated that not only magnetic coupling but also electric coupling exists between the ECPW resonator and the SIW cavity. As a result, a TZ located at finite frequency would be generated due to the mixed magnetic and electric coupling effect [17]. Using the conventional extracting method demonstrated in [18], the corresponding mixed coupling coefficient between the ECPW resonator and the SIW cavity can be extracted precisely, as shown in Fig. 2. It is worth noting that since the resonant frequencies of the ECPW resonator and the SIW cavity are different, one should use the coupling coefficient extracting formula for asynchronously tuned coupled resonators [18]. As can be observed from Fig. 2, the coupling coefficient can be effectively tuned by varying the geometrical parameter $L_3$. It means that the required coupling coefficient can be obtained with proper geometrical parameters.

![Figure 1](image1.png)

**Figure 1.** (a) Configuration of the hybrid structure of the proposed ECPW resonator and the SIW cavity; (b) the corresponding frequency response of the hybrid structure.

2.2. ECPW-Based Filter Design

Based on the analysis above, a three-pole Chebyshev bandpass filter is designed, as shown in Fig. 3(a). The filter consists of one SIW cavity and two ECPW resonators symmetrically arranged along the axial direction of the cavity, and its corresponding coupling scheme is presented in Fig. 3(b). It has been demonstrated that the cross coupling effect between the two ECPW resonators would lead to the split of the TZ and thus two TZs would be generated at the upper stopband [16]. Nevertheless, since the cross coupling between the two ECPW resonators has no effect on the center frequency and bandwidth of the filter, only the mixed coupling between the ECPW resonator and the SIW cavity is considered in the filter design process. Using the conventional Chebyshev bandpass filter design method [18], a Chebyshev bandpass filter with center frequency of 8.8 GHz and fractional bandwidth (FBW) of 20% is designed, and its ideal response is shown in Fig. 4 as the dash-slotted line. It should be noted that...
since the cross coupling between the two ECPW resonators is not considered, there would be no TZ in the ideal response. The corresponding mixed coupling coefficients are calculated as $k_{12} = k_{23} = 0.1594$, and then the key geometrical dimensions of the ECPW resonators can be determined according to the Fig. 2. The geometrical dimensions of the SIW cavity can be determined by its conventional resonant frequency formula [19]. The simulated response of the designed filter is shown in Fig. 4, in which two TZs located at the upper stopband can be observed as expected. The simulated response matches well with the ideal one, indicating that the desired filter response can be realized easily and accurately by using the design procedure above. The optimized geometrical dimension parameters are as follows: $W = 12.5$ mm, $L = 11.8$ mm, $L_1 = 0.8$ mm, $L_2 = 3.2$ mm, $L_3 = 1.12$ mm, $W_1 = 1.09$ mm, $W_2 = 0.2$ mm, $W_3 = 3.05$ mm, $\theta = 105^\circ$.

2.3. The Hybrid Structure of CLR and SIW Cavity

The CLR consists of a via hole and a floating metallic disk, and is slotted in the center of the SIW cavity, as shown in Fig. 5(a). The via hole is connected to the circuit ground at the bottom and to the disk at the top, and the disk is isolated from the top metal layer of the SIW cavity through an annular gap. Such a configuration can be modeled as a TEM-mode combline resonator and its corresponding equivalent transmission line model is shown in Fig. 5(b). The susceptance of the resonator can be
Figure 4. Simulated and analytical response: \(|S_{21}| \& |S_{11}| of the designed ECPW-SIW filter.

Figure 5. (a) Configuration of the hybrid structure of the proposed CLR and the SIW cavity; (b) the corresponding equivalent transmission line model.

expressed as

\[ B(\omega) = \omega C_0 - Y_0 \cot \left( \frac{\omega \sqrt{\varepsilon_r} h}{v} \right) \]  

(1)

where \(C_0\) represents the capacitance between the disk and the top ground plane of the SIW cavity, \(Y_0\) the characteristic admittance of the resonator, \(v\) the speed of the light in vacuum, and \(h\) the substrate thickness. The resonant frequency of the CLR can be obtained when \(B(\omega) = 0\). Fig. 6 shows the frequency response of the hybrid structure of the CLR and the SIW cavity, in which three resonant frequencies are observed. The three resonant frequencies successively correspond to the TE_{101} mode, TE_{102} mode of the SIW cavity and the TEM mode of the CLR.
Figure 6. Frequency response of the hybrid structure of the CLR and the SIW cavity.

Figure 7. (a) Layout of the proposed CLR-SIW filter; (b) the coupling scheme of the CLR-SIW filter.

2.4. CLR-Based Filter Design

Figures 7(a) and (b) present the configuration of the proposed CLR-SIW filter and its corresponding coupling scheme. In such a configuration, the CLR would not be coupled to the TE$_{102}$ mode of the SIW cavity, and this can be clarified through the electric field distributions of the TE$_{102}$ mode. As shown in Fig. 8, the electric fields of the TE$_{102}$ mode are mainly concentrated in two symmetrical areas with respect to the y-axis, and the closer to the symmetrical axis $y'$, the smaller the magnitude of the electric field is. Consequently, when the CLR is placed at the center of the SIW cavity (shown as the red point A), it would not be coupled to the TE$_{102}$ mode because the magnitude of the electric field of the TE$_{102}$ mode reaches its minimum there. As shown in Fig. 7(b), the TE$_{102}$ mode of the SIW cavity ($f_1$) and the TEM mode of the CLR ($f_2$) are individually coupled to the source/load, and thus two non-interacting electrical paths are generated. The two paths can produce two individual 1-pole filter responses to synthetize a desired 2-pole filter response. The corresponding coupling matrix $M$ of the coupling scheme can be expressed as

$$M = \begin{bmatrix}
0 & M_{S1} & M_{S2} & 0 \\
M_{S1} & M_{11} & 0 & M_{1L} \\
M_{S2} & 0 & M_{22} & M_{2L} \\
0 & M_{1L} & M_{2L} & 0
\end{bmatrix} \quad (2)$$

where $M_{S1}(M_{1L})$ and $M_{S2}(M_{2L})$ represent the coupling coefficients between the source (load) and the two resonators. It is worth noting that this coupling scheme can also provide one finite TZ when one of the four coupling coefficients ($M_{S1}$, $M_{S2}$, $M_{1L}$, $M_{2L}$) is negative. For the proposed structure, the
The electric field distribution of the TE\textsubscript{102} mode of the SIW cavity.

negative coupling coefficient can be realized by using the transformation property of the TE\textsubscript{102} mode of the SIW cavity [20], and thus a finite TZ would be generated. The location of the TZ can be determined as [21]

\[ \Omega = \left( \frac{M_{11}M_{22}^2 - M_{22}M_{11}^2}{M_{22}^2S_1 - M_{11}^2S_2} \right) \] (3)

It should be noted that \( \Omega \) is the normalized frequency. The TZ can be placed at either the upper stopband or the lower stopband, depending on the sign of \( \Omega \).

Based on the analysis above, a 2-pole bandpass filter with center frequency of 14.5 GHz and FBW of 15\% is designed. The TZ is placed at the normalized frequency \( \Omega = 3 \). Using the synthesis methods proposed in [22], the corresponding coupling matrix \( M \) is calculated as

\[
M = \begin{bmatrix}
0 & 0.7326 & 0.5215 & 0 \\
0.7573 & 0.9724 & 0 & -0.7573 \\
0.5215 & 0 & -1.1411 & 0.5215 \\
0 & -0.7573 & 0.5215 & 0
\end{bmatrix}
\] (4)

The solid line in Fig. 9 shows the ideal response of the designed filter. It can be seen that the two poles are located at 14.03 GHz and 15.12 GHz, respectively. To obtain the desired response, the CLR structure is removed firstly and thus the filter becomes a 1-pole filter. It should be noted that since only the TE\textsubscript{102} mode of the SIW cavity is used to form the passband, the other modes of the SIW cavity are not considered in this filter design. The center frequency of the 1-pole filter is set at 14.03 GHz, which is consistent with the location of the first pole of the ideal response shown in Fig. 9. The dashed and dash-slotted lines in Fig. 9 show the corresponding frequency response of the 1-pole filter. With this process, the dimensions of the SIW cavity can be specified. Subsequently, the CLR is reintroduced and its geometrical dimensions, namely \( d_1 \), \( r_2 \) and \( s \), are adjusted to make the simulated response of the designed structure match the ideal response synthesized from the coupling matrix \( M \). The circled line in Fig. 9 shows the simulated response of the final 2-poles filter, which matches well with the calculated ideal response. The optimized geometrical dimension parameters of the filter are as follows: \( L = 11.5 \text{ mm}, W = 10 \text{ mm}, W_3 = 2.2 \text{ mm}, d_1 = 0.95 \text{ mm}, s = 0.023 \text{ mm}, r_2 = 1.537 \text{ mm} \). Additionally, to validate the tunable property of the TZ, another demo filter with the TZ located at the lower stopband is designed. This demo filter is centered at 14.5 GHz with FBW of 12.7\%, and the TZ is placed at the normalized frequency \( \Omega = -3 \). Using the same design method above, the frequency response of this filter is easily obtained, as shown in Fig. 10. The optimized geometrical dimension parameters of this filter are as follows: \( L = 10 \text{ mm}, W = 10 \text{ mm}, W_3 = 2.05 \text{ mm}, d_1 = 0.59 \text{ mm}, \)
2.5. Dual-Band Bandpass Filter Design

Based on the proposed ECPW and CLR, a compact dual-band bandpass filter is designed, as shown in Fig. 11(a). In this filter design, the TE\(_{101}\) mode of the SIW cavity and the resonant frequency of the ECPW resonator are utilized to form the first passband while the TE\(_{102}\) mode of the SIW cavity and the resonant frequency of the CLR are used to form the second passband simultaneously. The dual-band bandpass filter is designed on RO4003 with thickness of \(h = 0.508\) mm and dielectric constant of 3.55. 

\(s = 0.031\) mm, \(r_2 = 1.744\) mm. It is demonstrated that the TZ can be placed at either the upper stopband or the lower stopband by properly adjusting the geometrical dimensions of the filter.
The optimized geometrical parameters of the proposed filter are as follows: $L_1 = 0.9$ mm, $L_2 = 3.2$ mm, $L_3 = 0.75$ mm, $W_1 = 1.5$ mm, $W_2 = 0.2$ mm, $W_3 = 4$ mm, $d_1 = 0.4$ mm, $s = 0.015$ mm, $r_2 = 0.705$ mm, $d_2 = 0.55$ mm, $s_1 = 0.6$ mm. The corresponding simulated frequency response of the dual-band filter is shown in Fig. 11(b). The center frequencies of the two passbands are 8.44 GHz and 14.11 GHz, and the corresponding FBWs are 24.2% and 10.1%, respectively. Additionally, it also can be seen that the filter has three TZs, of which two TZs are located in the middle of two passbands and one is located in the right edge of the second passband. These TZs can effectively improve the inner-band isolation and the selectivity of the filter.

The dependence of the performances of the dual-band filter on the geometrical parameters of the ECPW and the CLR are also analyzed, and the corresponding result is shown in Fig. 12. As analyzed in the Section 2.4, the filter response of the second passband is realized by synthetizing two 1-pole filter responses, and thus the bandwidth of the second passband can be effectively tuned by adjusting the resonant frequency of the two resonators. In our design, the diameter of the inner via, namely $d_1$,
is the key parameter which is used to control the resonant frequency of the CLR. Consequently, the bandwidth of the second passband should be varied with \( d_1 \). As shown in Fig. 12(a), when \( d_1 \) increases, the bandwidth of the second passband also increases linearly. The first passband is designed by using the classical Chebyshev filter design method, and its bandwidth is mainly controlled by the coupling coefficients between the resonators [18]. It has been demonstrated in Section 2.1 that the coupling coefficient between the ECPW resonator and the SIW cavity can be tuned by \( L_3 \), and thus \( L_3 \) can be used to change the bandwidth of the first passband. As can be observed from Fig. 12(b), the bandwidth of the first passband decreases with the increase of \( L_3 \). Additionally, since the open stub of the ECPW resonator is close to the feedline, the coupling coefficient between the source/load and the CLR could also be changed by \( L_3 \). Consequently, the performance of the second passband would also be varied with \( L_3 \), as shown in Fig. 12(b).

As shown in Fig. 11(b), the filter suffers from poor out-of-band rejection in the upper stopband due to the higher mode of the SIW cavity. As an attempt to solve this problem, two stepped impedance open stubs lowpass filters (LPFs) are loaded at the input/output of the proposed filter, as shown in Fig. 13(a). The design of the LPFs is based on the analytical synthesis procedure [23] and the cut-off frequency of the LPF is set at 17 GHz. The geometrical parameters of the LPF are as follows: \( W_4 = 1.09 \text{ mm} \), \( W_5 = 0.15 \text{ mm} \), \( W_6 = 0.3 \text{ mm} \), \( L_4 = 0.2 \text{ mm} \), \( L_5 = 1 \text{ mm} \), \( L_6 = 2.3 \text{ mm} \), \( L_7 = 2.4 \text{ mm} \), \( L_8 = 1.5 \text{ mm} \). As shown in Fig. 13(b), the out-of-band suppression of the filter drops below 30 dB when the LPFs are loaded, indicating that the upper stopband characteristic of the filter is effectively improved with the LPFs.

![Figure 13](image-url)

**Figure 13.** (a) Configuration of the final dual-band bandpass filter; (b) simulated results: \(|S_{21}|\) of the filters with/without LPFs.

### 3. SIMULATED AND MEASURED RESULTS

The proposed compact dual-band SIW filter with high selectivity is designed, fabricated and measured. A photograph of the final filter and its corresponding simulated and measured transmission responses are illustrated in Fig. 14. As observed, the measured results agree well with the simulated ones. In the simulated results, the center frequencies of the two passbands are located at 8.48 GHz and 14.29 GHz with FBWs of 24% and 11.3%, respectively. The corresponding insertion loss is \(-0.44\) to \(-1.26\) dB. In the measured results, the two passbands are centered at 8.41 GHz and 14.29 GHz with FBWs of 21.2% and 7.3%. The measured insertion loss is \(-1.28\) to \(-1.91\) dB, respectively. In addition, the upper stopband suppression is better than 30 dB in both simulated and measured results, suggesting a good out-of-band rejection of the proposed filter.

The measured dual-band SIW filter performance is compared with other high performance dual-band SIW filters, as shown in Table 1. It can be seen that the proposed dual-band filter has compact
Figure 14. Simulated and measured results: $|S_{21}|$ & $|S_{11}|$ of the final filter with the photograph of the fabricated filter.

Table 1. Comparison between the proposed filter and previous works.

<table>
<thead>
<tr>
<th>Reference</th>
<th>Size</th>
<th>Insertion loss (dB)</th>
<th>FBW</th>
</tr>
</thead>
<tbody>
<tr>
<td>[12]</td>
<td>$0.28\lambda_g \times 0.27\lambda_g$</td>
<td>$-2.42/-2.62$</td>
<td>$6.25%/5.2%$</td>
</tr>
<tr>
<td>[24] design II</td>
<td>$0.47\lambda_g \times 0.47\lambda_g$</td>
<td>$-1.16/-1.76$</td>
<td>$11.8%/5.4%$</td>
</tr>
<tr>
<td>[24] design III</td>
<td>$0.48\lambda_g \times 0.48\lambda_g$</td>
<td>$-1.8/-1.94$</td>
<td>$6.8%/3.2%$</td>
</tr>
<tr>
<td>This work</td>
<td>$0.33\lambda_g \times 0.33\lambda_g$</td>
<td>$-1.28/-1.91$</td>
<td>$21.2%/7.3%$</td>
</tr>
</tbody>
</table>

Note: $\lambda_g$ is the guide wavelength at the center frequency of the first passband.

size and exhibits good passband performances. Compared with other similar filters, the proposed one offers relatively broad bandwidth and low insertion loss.

4. CONCLUSION

In this paper, a compact dual-band bandpass SIW filter implemented with the ECPW resonator and the CLR is designed, fabricated and measured. The proposed dual-band SIW filter is centered at 8.41/14.29 GHz with FBWs of 21.2%/7.3% and the corresponding insertion loss $-1.28/-1.91$ dB, respectively. Three TZs are introduced in the filter, and thus the high selectivity and good isolation performance are obtained. The measured results are in good agreement with the simulated ones. The designed compact dual-band SIW filter exhibits the characteristics of low insertion loss, good inner-band isolation, high selectivity and good out-of-band rejection, which shows the great potential for dual-band filter applications.

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