Gas Sensing Using One-Dimensional Photonic Crystal Nanoresonators

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Abstract—In recent years, there has been more research on the use of photonic crystals PCs in the field of detection. The application of these materials as gas sensors seems very promising, because of their miniaturization and high spectral sensitivities. The aim of this work is to contribute to the design and study of a resonant microsystem based on one-dimensional photonic crystals for applications such as optical devices with high quality factor for detecting and measuring the concentration of gas in the air. Indeed, we have proposed a gas monitoring structure. This nanosystem is formed by an alternating stack of silicon Si layers and air with a resonant nanocavity in the middle. The numerical results show that the resonance peak that appears on the Photonic Band Gap (PBG) is caused by the creation of the nanocavity within the periodic 1D structure. This resonance peak can be used as a reference for real-time detection and environmental monitoring. In addition, we theoretically studied the relevance of these photonic systems and analyzed the effect of the intrinsic and extrinsic parameters of this device on the detection performance. We have also tried to improve the performance of such a device for the effect study of the inclination variation of the radiation incidence source on the selectivity of the detector.

1. INTRODUCTION

Photonic crystals (PCs) are artificial materials made from periodic arrays of dielectric or metallic building blocks. The existence of photonic band gaps (PBGs) has brought about an unprecedented power to control and manipulate the propagation of electromagnetic (EM) waves [1–3]. The simplest form of a photonic crystal is a one-dimensional periodic structure. It is known as the Bragg mirror. It consists of a stack of alternating layers having a low and a high refractive indices whose thicknesses satisfy the Bragg condition: $n_H \cdot d_H = n_L \cdot d_L = \frac{\lambda}{4}$, where λ is the reference wavelength [4]. In contrast to the two- and three-dimensional cases, the one-dimensional photonic crystal is attractive since its production is more feasible at any wavelength scale. The first function of a PBG is to be an excellent reflective mirror (more than 99(%)). Therefore, one option for providing a more flexible design of band gap structures could be to increase the width of the PBGs. In recent years, there have been several research works on the use of photonic crystals on the topic of sensor [5–7]. The application of photonic crystals as gas sensors in the area of research seems very promising due to their miniaturization and high spectral sensitivity. In this work we will show that one-dimensional (1D) photonic crystal formed by alternating layers of Silicon (Si) and Air with an empty "defect" layer in the middle can be used as an optical sensor for measuring the concentration of gases in air when it is illuminated by light in normal incidence.

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2. FORMULATION METHOD

The Transfer Matrix Method (TMM) approach is a matrix method particularly well suitable for the study of PBG materials, which can solve the standard problem of the photonic band gap structures and the scattering (transmission, reflection, and absorption) spectrum [8]. It is based on the Abeles approach in terms of forward and backward propagating electric fields, E_0^+ and E_0^- , which are introduced to calculate the reflection and transmission. The optical configuration used for incident and reflected fields is described in Fig. 1.



Figure 1. Incident and reflected fields for a 1D multilayer structure.

Abeles showed that the relation between the amplitudes [8] of the electric fields of the incident wave E_{m+1}^+ is expressed as the following matrix for stratified films within *m* layers:

$$\begin{pmatrix} E_0^+\\ E_0^- \end{pmatrix} = \begin{pmatrix} T_{11} & T_{12}\\ T_{21} & T_{22} \end{pmatrix} \begin{pmatrix} E_{m+1}^+\\ E_{m+1}^- \end{pmatrix}$$
(1)

Equation (1) holds whatever the boundary conditions. The reflection and transmission coefficients in complex amplitude are, from the left to the right (By setting, because there is no reflection from the final phase) [9].

$$r = \frac{E_0^-}{E_0^+}\Big|_{E_{m+1}^-=0} = \frac{T_{21}}{T_{11}}, \quad t = \frac{E_{m+1}^+}{E_0^+}\Big|_{E_{m+1}^-=0} = \frac{1}{T_{11}}$$
(2)

and from the right to the left $(E_0^+ = 0)$:

$$r' = \frac{E_{m+1}^+}{E_{m+1}^-} \bigg|_{E_0^+ = 0} = \frac{-T_{12}}{T_{11}}, \quad t' = \frac{E_0^-}{E_{m+1}^+} \bigg|_{E_0^+ = 0} = \frac{det[T]}{T_{11}}$$
(3)

Unless specified otherwise, we limit ourselves to the case where the two semi-infinite media surrounding the structure are identical $(n_0 = n_m + 1)$, in which case, det[T] = 1. From a physical point of view, this restriction does not change anything but presents the advantage of keeping formal expressions simpler to handle [9]. In intensity, the transmittance and reflectance are accordingly:

$$T = T' = |t|^2 = \left|\frac{1}{T_{11}}\right|^2 \tag{4}$$

$$R = |r|^2 = \left|\frac{T_{21}}{T_{11}}\right|^2 \tag{5}$$

$$R' = |r'|^2 = \left|\frac{T_{12}}{T_{11}}\right|^2 \tag{6}$$

3. RESULTS AND DISCUSSIONS

3.1. Effects of the Number of Layers

In this part, using a simulation script based on the TMM method we study the effects of the variation of the repetition number J of the pattern (LH) on the spectral behavior of a periodic multilayer system of the form $H(LH)^J$ (Fig. 2), where H denotes the layer of Titanium Dioxide (TiO₂) with refractive index $n_H = 2.3$ and thickness $d_H = \frac{\lambda_0}{4n_H}$, and L is the Silicon Dioxide (SiO₂) layer with $n_L = 1.45$ and thickness $d_L = \frac{\lambda_0}{4n_L}$. This structure is illuminated in normal incidence with a NIR laser diode with central wavelength $\lambda = 1.573 \,\mu\text{m}$ [10] which sweeps between 6349 and 6365 cm⁻¹.



Figure 2. Bragg mirror constructed with two types of layers, with indices of refraction respectively $n_L(L)$ and $n_H(H)$ according to the distribution $H(LH)^J$ where J presents the number of period of the pattern (LH).

Fig. 3 shows the spectra of optical reflections, in the spectral domain $[1 \,\mu\text{m}, 3 \,\mu\text{m}]$ with normal incidence and for variables repetitions numbers J.

The spectra presented in Fig. 4 show the system performance to know; a total reflection of 100% in the vicinity of the reference wavelength $\lambda_0 = 1.573 \,\mu\text{m}$ with an increase in the widths of these PBGs, as a function of the repetition number J of the elementary patterns (LH) of the photonic structure.

In fact, from the 7th iteration, we observe a remarkable increase in the maximum reflection $R_{\text{max}}(\%)$ R over the entire spectral domain (Fig. 5), consequently the appearance of a perfect PBG covering the neighborhood of the reference wavelength $\lambda_0 = 1.573 \,\mu\text{m}$.

Moreover, it can be seen that the PBG is centered around $\lambda_0 = 1.573 \,\mu\text{m}$, and its width expands exponentially as a function of the number of iterations of bi-layers J (Fig. 6). We notice that from the 7th iteration to the 30th iteration, the reflection is maximum and almost constant ($R_{\text{max}} \approx 100\%$).



Figure 3. Reflection spectra for periodic systems for different repetitions numbers J.



Figure 4. Presentation of the maximum reflection $R_{\max}(\%)$ on an optical spectrum.



Figure 5. Variation of the maximum reflection $R_{\max}(\%)$ according to the number of repetitions J.

Hence, in the rest of this work, we consider J = 7, and our study structure becomes $H(LH)^{\gamma}$, which has a minimum number of layers and a maximum reflection.

3.2. Effect of Index Contrast

The index contrast or optical contrast is defined as the ratio between the high and low refractive indices constituting the network. For a one-dimensional structure, the index contrast is given by [11] $\delta = \frac{n_H}{n_I}$.

The objective of this part is to check the correlation between the width of the PBG and the index ratio. In this case, we studied the reflection of 1D multilayer structures as a function of the index contrast. First, we set the low refractive index to $n_L = 1$, the number of bi-layers to J = 7, and



Figure 6. Variation of the PBG width as a function of the number of repetitions J.

the high refractive index n_H varied from 1 to 5. Then, we represented the optical reflections of the photonic structure. Also, we project the optical spectra obtained on the plane (OXY) to obtain the PBG mapping of the PBGs as a function of the index contrast δ .

Fig. 7 illustrates the optical reflections as a function of index contrast and wavelength as well as the maps of the corresponding bands, where the blue zone has the band gaps and the white zone the permitted bands.



Figure 7. Spectral appearance as a function of the index contrast variation for a periodic multilayer structure $H(LH)^{J}$: (a) Variation of reflection spectra as a function of index contrast, (b) Maps of PBGs as a function of the index contrast.

On the one hand, we note more particularly that the first PBG appears around $\lambda_0 = 1.573 \,\mu\text{m}$ with index contrast $\delta \approx 1.602$. On the other hand, we find that the widths of the PBGs increase considerably with the index contrast. Also, a distance (divergence) of the backgrounds of the PBGs (λ_m) of the reference wavelength $\lambda_0 = 1.573 \,\mu\text{m}$ as a function of the index contrast is observed. Table 1 gives the variation of the width and position of the PBG in the vicinity of $\lambda_0 = 1.573 \,\mu\text{m}$, with λ_{\min} presenting the lower limit of the band and λ_{\max} being the upper limit.

3.3. The Choice of the Initial Multilayer Structure

The choice of the geometrical parameters of the multilayer structure is determined in order to obtain the best optical performance of the device, namely a wide bandgap for a small number of layers.

$\delta = \frac{n_H}{n_L}$	2	2.5	3	3.5	4	4.5	5
$\lambda_{ m max}~(\mu{ m m})$	1.875	2.105	2.293	2.460	2.617	2.763	2.898
$\lambda_{ m min}~(\mu{ m m})$	1.355	1.258	1.195	1.155	1.125	1.097	1.063
$\lambda_m \; (\mu { m m})$	1.615	1.681	1.744	1.8075	1.871	1.93	1.980
$\Delta\lambda_{PBG}$ (µm)	0.520	0.847	1.098	1.305	1.492	1.666	1.835

Table 1. Variation of the widths of the PBGs as well as their positions according to the index contrast.

In the previous parts we have shown that the number of optimal bilayers of the structure is equal to 7. Moreover, we have found that the width of the PBG increases according to the index contrast, so we can select the refractive index so that they provide a high contrast taking into account the availability of materials and their dielectric natures. So we chose the Silicon Si and the Air with refractive indexes respectively $n_H = 3.4$ and $n_L = 1.000256$ (Fig. 8).



Figure 8. The chosen multilayer structure of type $H(LH)^7$ with the elementary layers, respectively, Si $(n_H = 3.4)$ and air $(n_L = 1.000256)$.

Fig. 9 shows the reflection spectrum of the structure $H(LH)^7$ with $n_H = 3.4$ and $n_L = 1.000256$ where we note that the PBG is wider than that for the multilayer with the same number of layers $H(LH)^7$ but with the refractive indices $n_H = 2.3$ and $n_L = 1.000256$.



Figure 9. Reflection spectra of the structure $H(LH)^7$ with: (a) Si $(n_H = 3.4)$ and air $(n_L = 1.000256)$, (b) SiO₂ $(n_H = 2.3)$ and air $(n_L = 1.000256)$.

3.4. Effect of Creating a Defect in 1D Periodic Multilayer Structure

3.4.1. Influence of the Presence of a Resonant Cavity on the Optical Properties in a Periodic 1D Multilayer Structure

We consider a one-dimensional periodic photonic system of type H(LH)J, with J keeping the optimal value J = 7. This structure is composed of a stack of silicon Si and Air layers which respectively correspond to the high and low index layers. In what follows, we introduce a defect, in the middle of the structure in the form of a thickness defect of the cavity (Fig. 9). In particular, we study the photometric properties of such type of hybrid system: $H(LH)^k C H(LH)^k$ with k = 3, where C denotes an air cavity of thickness d_C . In another way, as shown in Fig. 10, this system can be considered as two parallel Bragg mirrors arranged and spaced apart from each other by a distance d_C .



Figure 10. One-dimensional photonic structure with the presence of a defect in the form of an air cavity.

To analyze this new hybrid nanosystem, we used the transfer matrix method (TMM), where we chose: The thickness of the high index layer (Si) and the low index layer (air), respectively:

$$d_H = \frac{\lambda_0}{4n_H} = \frac{1.573}{4 \times 3.4} = 114.31 \,\mathrm{nm}$$
$$d_L = \frac{\lambda_0}{4n_L} = \frac{1.573}{4 \times 1.000265} = 393.14 \,\mathrm{nm}$$

In order to see the influence of the thickness on the spectral behavior of such a nanosystem, we have varied the cavity width from 600 nm to 800 nm. The transmission of the structure in question is shown in Fig. 11, for different widths of the cavity.

We can notice that the insertion of a cavity between two Bragg mirrors, the present case, results in the appearance of a resonance peak, characterizing a defect mode, which is positioned in the photonic band gap with a maximum intensity of 100%. It is also clear that as the width of the cavity dC increases, the position of the peak moves towards the high wavelengths (Table 2).

Table 2. Position of the resonance peak according to the width of the cavity.

Width of cavity d_C (nm)	600	650	700	750	800
Position of the resonance peak (μm)	1.3157	1.382	1.4511	1.5215	1.5924

3.4.2. Choice of Parameters of the Detection Nanostructure

As we saw in the preceding parts, the geometrical parameter of the initial nanostructure (Fig. 10) namely the thicknesses of the layers of high index H and low index L are fixed so that the condition of Bragg is satisfied, $n_H \cdot d_H = n_L \cdot d_L = \frac{\lambda}{4}$. In addition, we have to determine the optimal width of the



Figure 11. Transmission spectra of a 1D structure with air cavity, for $d_H = 114.31 \text{ nm}$ and $d_L = 393.14 \text{ nm}$ with different width of the cavity: $d_C = 600 \text{ nm}$, $d_C = 650 \text{ nm}$, $d_C = 700 \text{ nm}$, $d_C = 750 \text{ nm}$ and $d_C = 800 \text{ nm}$.

resonant cavity d_C . In addition, we proceeded to solve the problem from a point of view "purpose of use" of this optical device, that is to say, it is necessary to find a width d_C to ensure a good detection quality. Indeed, like any resonant structure, our nanosystem will be characterized by a quality factor, generally denoted as Q. This quantity is defined as the ratio of the resonant wavelength peak λ_{peak} by the Full Width at Half Maximum FWHM of the resonance peak peak $\Delta \lambda_{peak}$

$$Q = \frac{\lambda_{peak}}{\Delta\lambda_{peak}} \tag{7}$$

For this purpose, we measured the values of the peak position and the FWHM of the resonance peak, for each d_C value which varies between 500 nm and 1100 nm. Similarly, we have calculated the quality factor Q on a step of 20 nm (Fig. 12).

From Fig. 12 we note that a slight variation in the width of the cavity d_C causes a shift in the position of the resonance peak λ_{peak} with an increase of the quality factor Q, until reaching a significant



Figure 12. Variation of the quality factor Q and the peak position λ_{peak} according to the width d_C of the cavity for $d_H = 114.31$ nm, $d_L = 393.14$ and varied from 500 nm to 1100 nm.

value: $Q_{\text{max}} = 21343$ for a critical value $d_C = 780 \text{ nm}$ which corresponds to resonance wavelength $\lambda = \lambda_0 = 1.573 \text{ \mum}$. In addition, the quality factor Q decreases when the width of the cavity d_C exceeds the critical value. In sum, the position of the defect mode moves linearly towards the high wavelengths as a function of the width of cavity d_C . Also, the quality factor decreases as the wavelength moves towards edges of the PBG.

These characteristics and this choice of geometrical parameters make the system a good candidate for the design of a high quality optical sensor with high sensitivity. So given all the above we can define the optimal geometrical parameters of our nanoresonator as:

- The thickness of the high index layer (Si): $d_H = 114.31$ nm.
- The thickness of the low index layer (air): $d_L = 393.14$ nm.
- The width of the nanocavity: $d_C = 780$ nm.

3.5. Application of the Nanostructure for Gas Detection

After having shown that the photonic nanosystem in the previous part which presents a default mode is a monochromatic interference filter of "good quality", we tried to apply this structure for the detection of gases. Indeed, we studied by simulating the effect of evacuation of a gas in the nanostructure cavity on the spectral behavior of the nanosystem. In other words, we analyzed the consequences of the change of air in the cavity by another polluting gas, i.e., the variation of the refractive index of the medium.

3.5.1. Result of the Detection Analysis

To study the mode of detection of the resonant cavity, we consider the most dominant pollutant gases in the nature of different refractive indices such as carbon monoxide CO ($n_{\rm CO} = 1.0003360$), carbon dioxide CO₂ ($n_{\rm CO_2} = 1.000407$), and nitrogen NO₂ ($n_{\rm NO_2} = 1.0005087$). As a result, we illustrate in Fig. 13, with a normal incidence, the transmission of the cavity mode for each type of gas as a function of displacement $\Delta\lambda$ relative to the resonance wavelength of air that corresponds to the reference wavelength: $\Delta\lambda = \lambda - \lambda_0$.



Figure 13. Transmission of the cavity mode for different gases where the air is a reference medium as a function of displacement $\Delta \lambda = \lambda - \lambda_0$.

The transmission spectra denote, respectively, in black the resonance peak or the cavity mode for the reference medium (Air), in red the carbon oxide (CO), in green the carbon dioxide (CO₂), and in blue the nitrogen dioxide (NO₂). Thus we observe a very small shift of the resonant peaks from the reference position (Air) as a function of the pollutant gas index n_p (Table 3), which creates a detector selectivity problem. **Table 3.** The displacement of the cavity mode $\Delta \lambda$ according to the nature of the polluting gas.

Gas	Air	CO	$\rm CO_2$	NO_2
Displacement $\Delta\lambda$ (nm)	0	0.0634	0.1255	0.2156

3.5.2. Improvement of the Selectivity

In order to improve the spectral selectivity of the nanostructure, we note that any modification of the incident angle of the incoming beam causes a decrease in the full width at half maximum (FWHM) and a displacement of the resonance peaks in the band gap. Based on this effect we calculated the FWHM of the reference peak (Air) as a function of the incident angle with a step of $\frac{\pi}{40}$ (Fig. 14).



Figure 14. Full width at half maximum of the defect mode (resonance peak) as a function of the incident angle varied from 0 rad to $\frac{14\pi}{40}$ rad.

We notice that the FWHM decreases as the angle of incidence θ increases, and the resonance peaks become narrower. Thus, the optical device becomes more selective than the use of the laser source in normal incidence. In addition, the FWHM of the resonance peak reaches a minimum of 0.08 nm for any angle of incidence greater than a critical angle $\theta_c = \frac{11\pi}{40}$. In the rest of this part we consider θ_c as the angle of incidence of the laser source beam (Fig. 15).



Figure 15. The nanosystem of detection with oblique incidence of d_C .

The cavity modes for the incidence angle $\theta = \theta_c = \frac{11\pi}{40}$ with air as a reference medium are shown in Fig. 16. We observe that the nanocavity has only one resonance peak (single defect mode) that corresponds to the refractive index of the gas injected into it. This peak shifts in the PBG as a function of the refractive index, i.e., according to the nature of the pollutant gas. Table 4 lists the displacement $\Delta \lambda$ and the FWHM of the resonance peak for different gases, i.e., air, CO, CO₂, and NO₂.



Table 4. The displacement of the cavity mode $\Delta \lambda$ according to the nature of the polluting gas.



The FWHM of the cavity mode for the gases used has low values and varies as the nature of the gas: 174 pm for air, 160 pm for CO, 170 pm for CO₂, and 184 pm for CO₂. Therefore, by using a small number of periodic layers in the proposed structure, it is possible to obtain a very narrow resonance peaks, i.e., the detection device has a good theoretical selectivity.

3.5.3. The Detection Efficiency

In what follows, we give an estimate of the efficiency of the sensor, by fixing the length of the resonant nanocavity d_C at 780 nm, which offers the greatest sensitivity of the mode to the variation of the refractive index. We report the evolution of the transmission curves for a variation of the refractive index of the air polluted by nitrogen dioxide NO₂ ($n_{\rm NO_2} = 1.0005087$) with a step of 10^{-5} ($n_p = 1.0005087$ to $n_p = 1.0005387$) (Fig. 17).



Figure 17. The transmission spectra of the sensor with four different refractive indices varying from $n_p = 1.0005087$ to $n_p = 1.0005387$ with incrementation of 0.00002.

We show that a variation of 10^{-5} of the refractive index results in a shift of the cavity mode position equal to 132 pm. Thus we observe a good accuracy for cavity mode shift detection. In other words, a high accuracy of detection of change in the index of the cavity, i.e., the nature of the pollutant gas, is achieved.

3.5.4. Concentration and Sensitivity of Detection

In what follows and referring to the studies of Bouzidi et al. [12], we applied the previous analysis to a practical situation, by fixing the parameters of the resonant structure: $d_H = 114.31 \text{ nm}$, $d_L = 393.14 \text{ nm}$, $d_C = 780 \text{ nm}$, and $\theta_c = \frac{11\pi}{40}$. With these parameters, the operating wavelength of the sensor will be set to the reference wavelength $\lambda_0 = 1.573 \mu \text{m}$. The most common way to estimate the efficiency of a sensor is to calculate its sensitivity given by the following expression:

$$S = \frac{\Delta \lambda_{peak}}{\Delta_n} \,(\mathrm{nm/RIU}) \tag{8}$$

In the following, we calculate the response of the sensor for the detection of the polluted air composed of different concentrations of Methane CH_4 and Ethane C_2H_6 . The refractive indices of different concentrations are shown in Tables 5 and 6 of [13].

Fig. 18 represents the dependence of the resonance wavelength λ_{peak} with respect to the refractive index of the air polluted with methane (Fig. 18(a)) and ethane (Fig. 18(b)) for different concentrations.

Table 5. Refractive index of Methane n_{mix} in air for different concentrations of Methane gaz CH₄.

Methane	$C_{\rm CH_4}$	C_{air}	n_{mix}
5%	0.05	0.95	1.0000222
15%	0.15	0.85	1.0000666

Table 6. Refractive index of Ethane n_{mix} in air for different concentrations of Ethane gaz C₂H₆.

Methane	$C_{\rm C_2H_6}$	C_{air}	n_{mix}
3%	0.03	0.97	1.0000228
12.5%	0.125	0.875	1.000095



Figure 18. The resonance wavelength as a function of the concentration of the polluting gas in the air: (a) Methane, (b) Ethane.

Note that the resonance wavelength varies linearly with the refractive index where the slope represents the sensitivity with a value of 21688 nm/RIU. Indeed, a slight variation in the concentration of a polluting gas in the air can be detectable. So this type of sensor can be used to monitor the level of gas concentration in the ambient air.

4. CONCLUSION

In this paper we have studied firstly the periodic multilayer structures, and the chosen system is a periodic multilayer system of type $H(LH)^J$ $(H = \text{TiO}_2 \text{ and } L = \text{SiO}_2$ are respectively dielectric layers of high and low indices). Indeed we analyzed the effect of variation of number of dielectric layers and the contrast of index to determine the optimal number of elementary motifs of the structure (J = 7). Secondly, we inserted a defect, in the form of a resonant nanocavity in the initial structure (replacing the high index layers by the silicon (H = Si) and the low index layers by the air (L = air)), where we are able to determine the best width needed to ensure a high quality factor and a good detection sensitivity $(Q_{\text{max}} = 21343 \text{ for } d_C = 780 \text{ nm})$. Thirdly, we tried to improve the performances of such a device for the study of the effect of change of the inclination of the radiation source on the selectivity of the detector. Lastly, the detection efficiency and the sensitivity of the detection of the concentration of a pollutant gas in the air have been highlighted.

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