

DIRECTION OF ARRIVAL AND STATE OF POLARIZATION ESTIMATION USING RADIAL BASIS FUNCTION NEURAL NETWORK (RBFNN)

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Abstract—A Neural Network architecture is applied to the problem of Direction of Arrival (DOA) and state of polarization estimation using a uniform circular cross and tri-crossed-dipoles antenna array. A three layer Radial Basis Function Network (RBFN) is trained with input output pairs. The network is then capable of estimating DOA not included in the training set through generalization and the corresponding state of polarization. This approach reduces the extensive computations required by conventional super resolution algorithms such as MUSIC and is easier to implement in real-time applications. The results suggest that the performance of the RBFNN method approaches the exact values. In real time, fast convergence rates of neural networks will allow the array to track mobile sources.

1. INTRODUCTION

Super-resolution algorithms have been successfully applied to the problem of Direction of Arrival (DOA) estimation to locate radiating sources with additive noise, uncorrelated and correlated signals. MUSIC [1] and [2] and ESPRIT [3] and [4] are some of the popular conventional methods of DOA estimation. They have the advantage of high resolution for signals with small angular separation (few degrees to few tenths of a degree). However, one of the main disadvantages of these algorithms is that they require extensive computation and are difficult to implement in real-time.

Recently, neural networks have been proposed as successful candidates to carry on the computational tasks required in several array processing and real-time DOA estimation applications is

presented in [5–10]. The main advantages of the neural network methods are that they outperform conventional linear algebra based methods in both speed and accuracy. Since neural methods avoid the cumbersome eigen-decomposition process, they are found to be far quicker than conventional methods. Apart from being computationally efficient, neural methods have been observed to be more immune to noise and are found to yield better performance in the presence of correlated arrivals. However, a drawback of the neural schemes is the selection of the network size which is usually done by trial and error.

In this paper, the application of neural networks to handle the computational problem of the DOA estimation step is approached as a mapping problem which is modeled using a Radial Basis Function Network or (RBFN) that can be trained with input output pairs [11–13]. The network is then capable of estimating or predicting outputs not included in the learning phase through generalization. Moreover, one of the main advantages of neural networks is that they can be implemented in analog circuits with time constants in the order of nanoseconds and consequently they have fast convergence rates. Thus DOA estimation problem is viewed as a function approximation problem, and the RBFNN is trained to perform the mapping from the space of the sensor array output to the space of DOAs. It exploits the universal function approximation capability of RBFNN to estimate the DOA and the state of polarization and a successful classification of closely separated sources (3 degrees) has been reported.

2. DOA ESTIMATION USING REAL ELEMENT ARRAYS

The signal processing algorithms proposed for DOA estimation provides accurate estimates, even in moderate signal to noise (SNR) conditions, but generally ignore the electromagnetic behavior of the receiving antenna. The receiver is assumed to be an ideal, equispaced, linear array of isotropic point sources and does not reradiate the incident signals. In practice, this ideal situation cannot be met. The elements mutual coupling distorts the linear phase front of the incoming signal, significantly degrading performance. Thus any practical implementation of DOA estimation requires compensation for mutual coupling. The compensation of mutual coupling using effective techniques has been reported in [14–16].

By using impedance load at each element port as shown in Fig. 1, the measured voltage at the port of the n th receiver antenna is given by

$$V_{meas_m} = Z_L I_{port} = Z_L I_{(P+1/2),m} \quad (1)$$

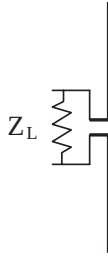


Figure 1. The compensation for mutual coupling in real array elements using load at terminal point $Z_L = 50 \Omega$.

i.e., the measured voltage at a port of the array is directly proportional to the coefficient of the basis function corresponding to that port.

3. RBFNN MODEL FOR DOA PROBLEM

The DOA problem is approached as a mapping which can be modeled using a suitable neural network (NN) trained with input output pairs. The network capable of estimating or predicting outputs not included in the learning through generalization. The advantages of NNs are that it can be implemented in real time. The adaptive antenna array can be linear array or circular array with isotropic or real elements. Neural networks based direction finding algorithms have been proposed for single and multiple source direction finding [17]. It has been shown that the neural networks have the capability to track sources in real time. It has been suggested that a radial basis function neural network (RBFNN) could be used to track the locations of mobile users [18].

RBFNNs are member of a class of general purpose methods for approximating nonlinear mappings since the DOA problem is of nonlinear nature. The mapping from the input space to the output space may be thought of as a hypersurface Γ representing a multidimensional function of the input. During the training phase, the input-output patterns presented to the network are used to perform a fitting for Γ . The generalization phase represents an interpolation of the input data points along the surface built as an approximation for Γ . The architecture considered in this paper involves three layers, the input layer (sensory nodes), a hidden layer of high dimension, and an output layer, as shown in Fig. 2. The transformation from the input space to the hidden-unit space is nonlinear, whereas the transformation from the hidden layer to the output space is linear.

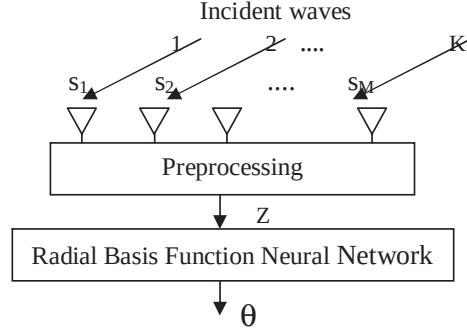


Figure 2. Proposed architecture of DOA estimate using neural network.

4. DATA PREPROCESSING

It considers a linear array composed of M elements (point sources), and let $K (K \leq M)$ be the number of plane waves, centered at frequency ω_o impinging on the array from directions $\{\theta_1 \theta_2 \dots \theta_K\}$. It performs the mapping $G: R_K \rightarrow C_M$ from the space of DOA, $\{\theta = [\theta_1, \theta_2, \dots, \theta_K]\}$ to the space of sensor output $\{s = [s_1, s_2, \dots, s_M]\}$, where s_M is the source output at element m , namely

$$s_m = \sum_{k=1}^K a_k e^{j(m(\omega_o/c)d \sin \theta_k + \alpha_k)} \quad (2)$$

where a_k represents the complex amplitude of the k th signal, α_k the initial phase, and ω_o is the center frequency. Based on the information theoretic criteria for model selection [19], one can estimate the number of signals K a priori.

The RBFNN is used to perform the inverse mapping $F: C_M \rightarrow R_K$. The network is to be trained by N patterns generated by using Eq. (2) so that it can associate the output vectors $s(1), s(2), \dots, s(N)$ with the corresponding DOA vectors $\theta(1), \theta(2), \dots, \theta(N)$. Input vectors s are mapped through the hidden layer then each output node computes a weighted sum of the hidden layer outputs. We can write for a set data $\{(s(i), \theta(i)), i = 1, 2, \dots, N\}$. The output of the neural is given by

$$\theta_k(j) = \sum_{i=1}^N w_i^k f_h(\|s(j) - s(i)\|^2) \quad (3)$$

For $k = 1, 2, \dots, K$, and $j = 1, 2, \dots, N$, where w_i^k represents the i th

weight of the network. Using the Gaussian function for hidden nodes f_h , we can rewrite Eq. (3) as

$$\theta_k(j) = \sum_{i=1}^N w_i^k e^{-\|s(j)-s(i)\|^2/\sigma_g^2} \quad (4)$$

the parameter σ_g controls the influence of each basis function.

The main advantage of using an RBFNN over other approaches is that it does not require training the network with all possible combinations of input vectors. For the network to generalize it is sufficient to perform the training with vectors that span the expected range of input data.

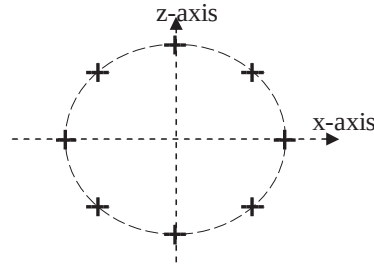


Figure 3. 16-elements uniform circular array (crossdipole) geometry in x - z plane.

5. NUMERICAL RESULTS

5.1. The Uniform Circular Array Geometry

In many applications, to provide full azimuthal coverage several uniform linear arrays (ULA) arranged in triangular or rectangular shapes are used. But the drawback of this solution is the requirement of using several ULA, and hence increasing the cost, as well as the collection and processing of additional data. The natural choice of uniform circular array (UCA) which provides entire azimuthal coverage and certain degree of source elevation information [20]. Referring to Fig. 3 and Fig. 4, we assumed that a UCA with radius “ a ” and consisting of “ N ” uniformly distributed antenna elements, assumed to be identical, is located in the x - z plane and is illuminated by an impinging planer wavefront. A spherical coordinate system is used to represent the DOA from the incoming plane waves. The origin of the

coordinate system is located in the center of the array. The angular position of the n th element of the array is given by [20]

$$\theta_n = 2\pi \left(\frac{n}{N} \right), \quad n = 1, 2, \dots, N. \quad (5)$$

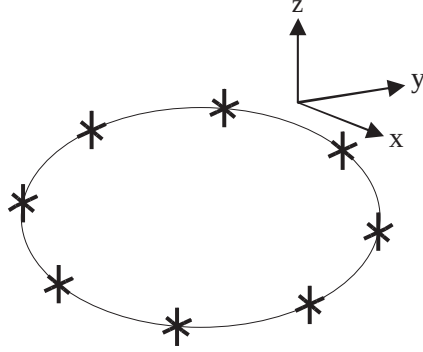


Figure 4. 24-elements uniform circular array (tri-crossed-dipoles).

The narrowband plane wave with wavelength λ (and corresponding wave number $k = 2\pi/\lambda$) arrives at the antenna from elevation angle θ and azimuthal angle φ . The using of cross-dipoles and Tri-crossed-dipoles as a UCA elements are useful in obtaining different states of polarization ant different planes of incidence [21].

5.2. Example (1) Cross-dipole Uniform Circular Array

A circular array of $M = 16$ cross-dipoles each of length $\lambda/2$, are terminated in loads $Z_L = 50$ ohm is used. Therefore, the dimension of the input layer of the neural network was set to 16 nodes (magnitude of the input vector $V_n(n)$). The array receives signal with different state of polarization (including linear θ -polarized, linear φ -polarized, right-hand circular polarization and left-hand circular polarization) from different directions. The results in Fig. 5 show that the network successfully produced actual outputs very close to the desired DOA at different incidence angles in the x - y plane. Also, the state of polarization is detected clearly. The array is then exposed by eight uncorrelated sources separated by $\Delta\varphi = 3^\circ$ in the x - y plane. Fig. 6 shows the DOA estimation of the first source.

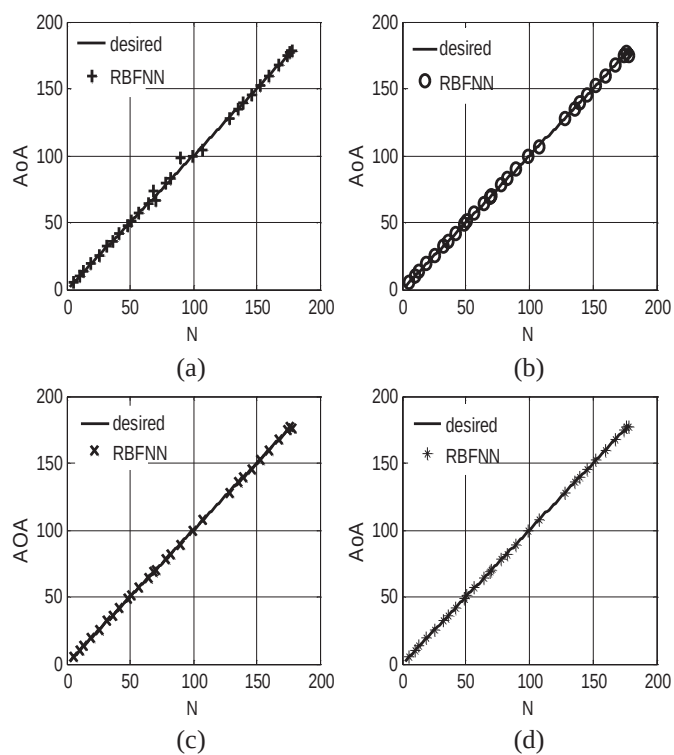
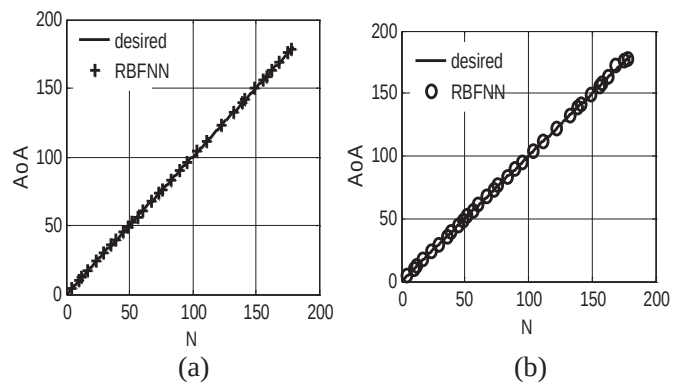


Figure 5. DOA estimates versus number of samples N for cross-dipole array. Incident Source (1) φ is varied from 0° to 180° and $\theta = 90^\circ$ when (a) linear- θ polarized, (b) linear- φ polarized, (c) right-hand circular polarized, (d) left-hand circular polarized.



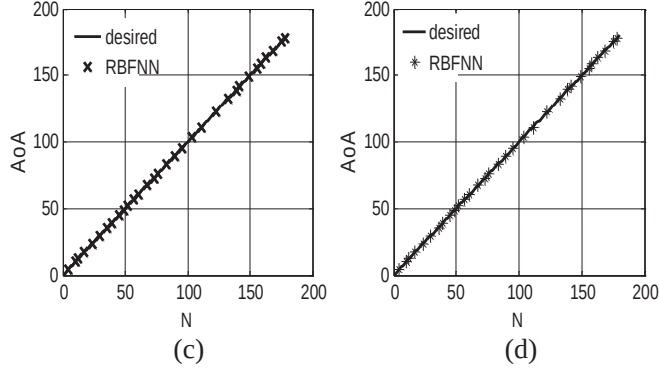


Figure 6. DOA estimates versus number of samples N for cross-dipole array. 8-Uncorrelated sources used with ($\Delta\varphi = 3^\circ$). Source (1) φ is varied from 0° to 180° and $\theta = 90^\circ$.

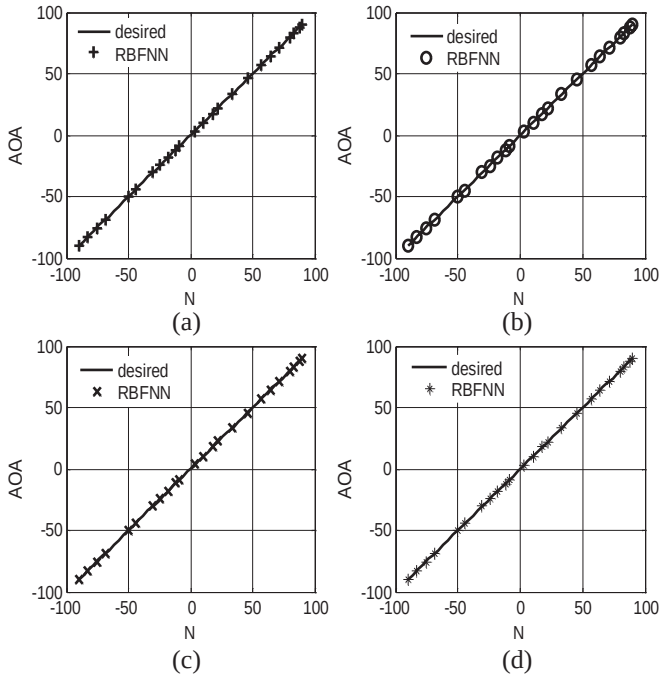


Figure 7. DOA estimates versus number of samples N for tripole array. Incident Source (1) θ is varied from -90° to 90° and $\varphi = 0^\circ$.

5.3. Example (2) Tri-crossed-dipoles Uniform Circular Array

A circular array of $M = 24$ tri-crossed-dipoles array each of length $\lambda/2$, are terminated in loads $Z_L = 50$ ohm is used. The array receives signal with different state of polarization. The array is exposed by incident plane wave source in different planes and the performance of the RBFNN is shown in the figures. Figs. 7, 8, and 9 shows the RBFNN performance with DOAs were assumed to be uniformly distributed from -90 to 90 in both the training and testing phases in the planes $\varphi = 0, 45^\circ$, and 90° respectively. Fig. 10 shows the RBFNN performance with DOAs assumed to be uniformly distributed from 0° to 180° in both the training and testing phases in the x - y plane. Similarly Fig. 11 and Fig. 12 shows the network performance when the array receives eight uncorrelated signals with different angular separations ($\Delta\theta = 5^\circ$ and $\Delta\varphi = 3^\circ$) at different planes respectively. The results show that the network successfully produced actual outputs very close to the desired DOA.

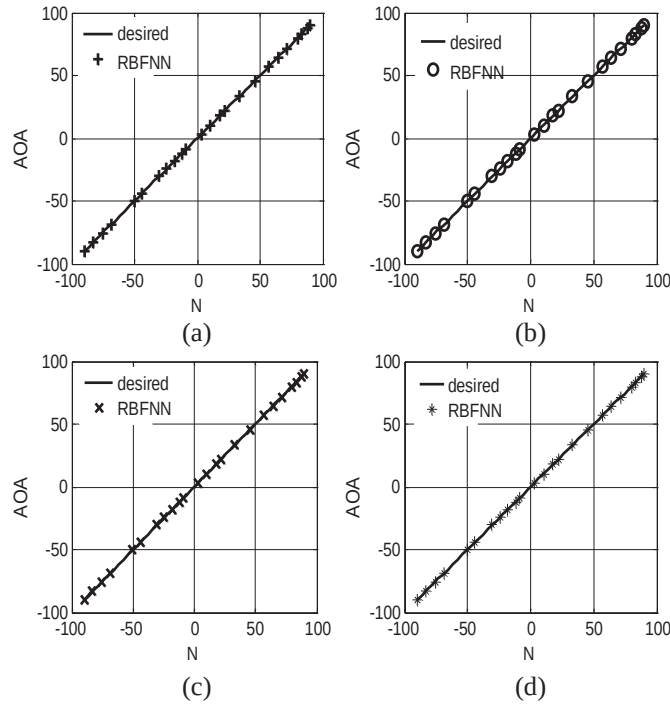


Figure 8. DOA estimates versus number of samples N for tripole array. Incident Source (1) θ is varied from -90° to 90° and $\varphi = 45^\circ$.

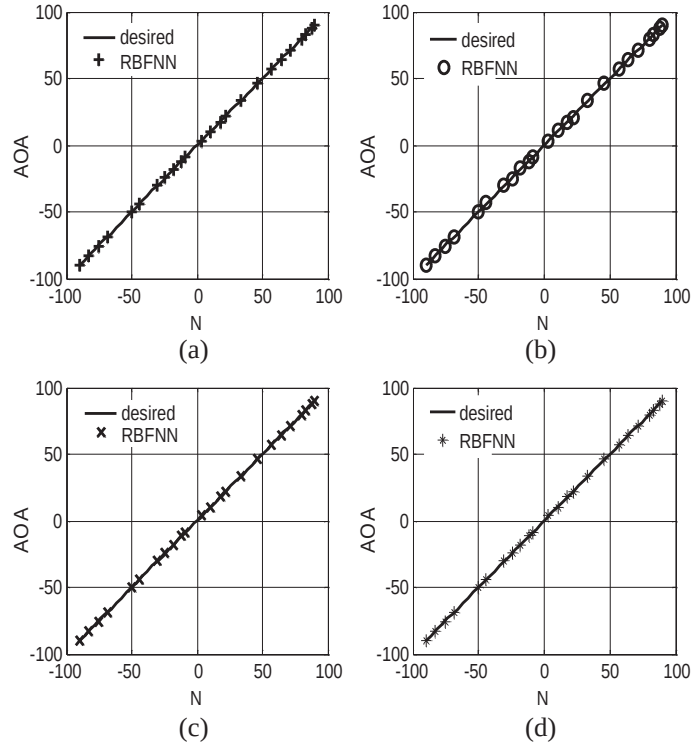
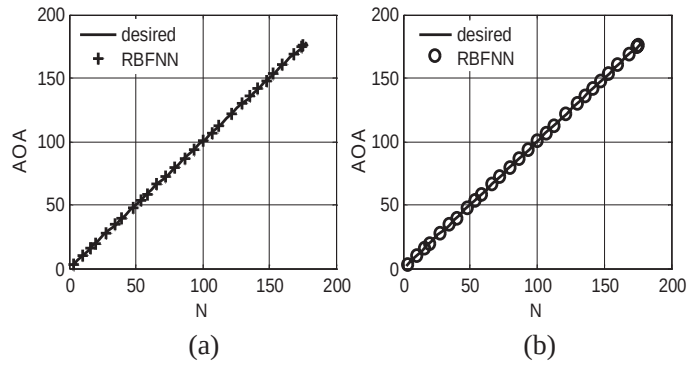


Figure 9. DOA estimates versus number of samples N for tripole array. Incident Source (1) θ is varied from -90° to 90° and $\varphi = 90^\circ$.



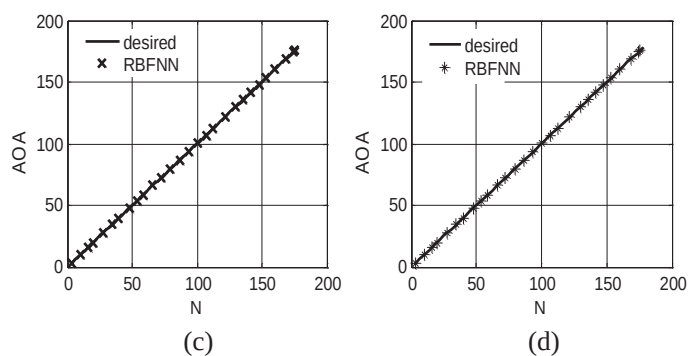


Figure 10. DOA estimates versus number of samples N for tripole array. Incident Source (1) φ is varied from 0° to 180° and $\theta = 90^\circ$.

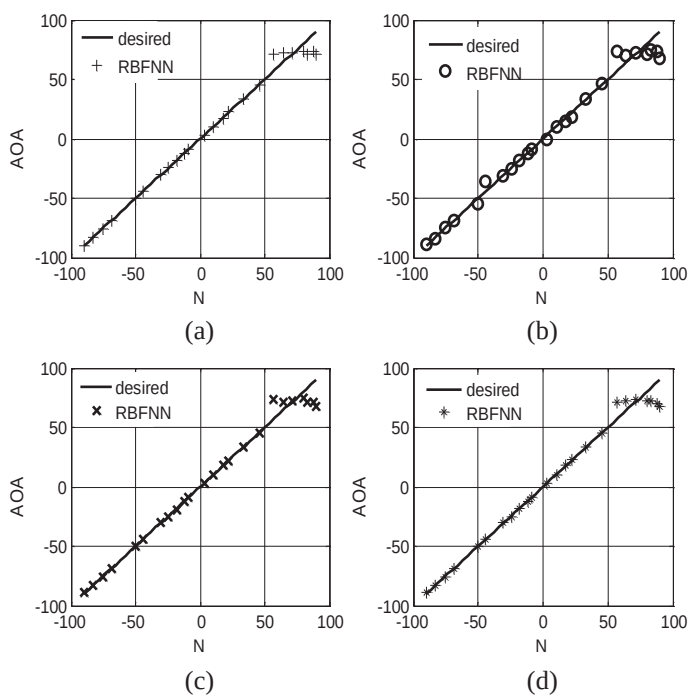


Figure 11. DOA estimates versus number of samples N for tripole array. 8-Uncorrelated sources used with $(\Delta\theta = 5^\circ)$. Source (1) θ is varied from -90° to 90° and $\varphi = 0^\circ$.

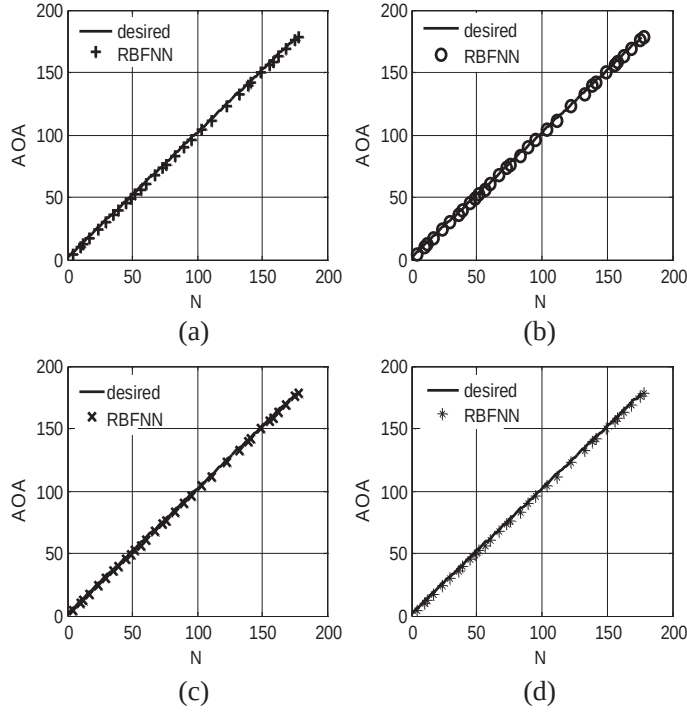


Figure 12. DOA estimates versus number of samples N for tripole array. 8-Uncorrelated sources used with ($\Delta\varphi = 3^\circ$). Source (1) φ is varied from 0° to 180° and $\theta = 90^\circ$.

6. CONCLUSION

The neural network is used to estimate the direction of arrival with different arrays such as circular arrays with real elements of cross-dipoles and tri-crossed-dipoles elements, where the RBFNN is trained by input-output pairs to estimate the DOA with different separated angles and tested with samples are not included in the learning phase. Good agreement between the results using the RBFNN model, and the exact values.

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