# LARGE SIGNAL EQUIVALENT CIRCUIT MODEL FOR PACKAGE ALGaN/GaN HEMT 

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#### Abstract

In this paper, a large signal equivalent circuit empirical model based on Anglov model for ceramic package high power AlGaN/GaN HEMT has been proposed. A temperature-dependent drain current model, including self-heating effect, has been presented, and good agreements are achieved between measurement results and calculated results at different temperatures. The nonlinear capacitance models are modeled directly by measured microwave scattering $(S)$ parameters and multi-bias small signal equivalent circuit model (SSECM) of package device is also established based on the measurements. A power amplifier based on large size AlGaN/GaN HEMT with a total gate periphery of 36 mm has been designed by using the proposed model for validation purpose, and the simulation results fit the measurement results well at different temperatures.


## 1. INTRODUCTION

Recently, AlGaN/GaN HEMT is emerging as a frequently employed technology in high power RF devices due to high maximum cut-off frequency ( $f_{T}$ ), high breakdown voltage, high power density and high operating temperature [1]. Accurate large signal model is crucial for GaN power devices and circuit design. Compared with physical based model [2] and table based empirical model [3], empirical large signal equivalent circuit model (LSECM) is more simple and easier to be implemented in microwave commercial simulation software, and has been widely used in GaAs and SiC based devices $[4,5]$. However, accurate LSECM for GaN based devices is still a major topic of
discussion due to the existence of thermal effects and trapping related dispersion in GaN HEMT devices [2,3,6, 7]. A common way to build the LSECM starts from small gate periphery GaN HEMT, and extends it into application of large gate periphery or even multi-cell large size devices by using scalable technique. Because the measurements of microwave scattering $(S)$ parameter are less affected by self-heat effect and the output power character can be easily measured by using load pull measurement for small size device, this method can obtain accurate LSECM for small gate periphery GaN HEMT. However, the accuracy of LSECM is largely limited when it extends to large size device due to the inhomogeneous of heat transportation and trapping distribution induced by processing [8]. Moreover, the prediction performance of package device based on LSECM developed from small size device will become worse duo to the parasitic parameters effect and heat transportation in ceramic cavity.

In this paper, an empirical LSECM for large gate periphery package AlGaN/GaN HEMT device has been developed based on bottom-up technology. A small signal equivalent circuit model (SSECM) is established directly by measured $S$ parameters of package device at different biases [9], and the nonlinear capacitance models are empirically modeled based on multi-bias SSECM. The nonlinear drainsource current $(I-V)$ model is modeled by fitting with measured $I-V$ curve accounting thermal effect.

The thickness of the silicon carbide ( SiC ) substrate of the device is $150 \mu \mathrm{~m}$. The T shape gate is made from $\mathrm{Ni} / \mathrm{Au}$ with $0.5 \mu \mathrm{~m}$ width. The SiNx is used as passivation and encapsulation layer. The whole device contained 18 cells and the gate periphery for each cell is 2 mm , and is packed with ceramic. In band below 3.8 GHz the device could operates normally.

## 2. SMALL-SIGNAL EQUIVALENT CIRCUIT MODEL

In order to include the package effect of large gate periphery device, the parasitic parameters should be taken good consideration for high frequency application. Jarndal and Kompa [10] have studied the 22elements distributed topology and extraction method for AlGaN/GaN HEMT, and Lu et al. [11] proposed a 20-elements topology and extraction method for AlGaN/GaN HEMT. In this paper, we use a compact model with 19 elements as shown in Fig. 1. The parasitic parameters include parasitic inductances and resistances at source ( $L_{s}$ and $R_{s}$ ), drain ( $L_{d}$ and $R_{d}$ ), and gate $\left(L_{g}\right.$ and $\left.R_{g}\right)$ electrodes, parasitic capacitors between gate to source $\left(C_{g s i}\right)$, gate to drain $\left(C_{g d i}\right)$, and drain to source $\left(C_{d s i}\right)$, as well as parasitic capacitors $\left(C_{p g}\right.$ and $\left.C_{p d}\right)$ induced


Figure 1. 19-elements GaN HEMT SSECM.


Figure 2. (a) Equivalent circuits for cold pin-off and (b) unbiased condition.
by package effect. The effects of parasitic capacitor between gate and drain induced by package effect and parasitic parallel resistance between gate and drain are very small and can be negligible if the operation frequency less than 10 GHz , so we ignore them to simplify the parameters extraction method.

Considering the complexity of SSECM, the cold FET method is used to give a few relationships between parasitic parameters before extracting the intrinsic parameters. The equivalent circuit of cold FET with pinch-off bias at low frequencies $(<500 \mathrm{MHz})$ can be simplified (shown in Fig. 2(a) ) and the $Y$-parameters of the equivalent circuit can be written as:

$$
\begin{align*}
\operatorname{Im}\left(Y_{11}\right) & =j \omega\left(C_{p g}+C_{g s i}+C_{g s}+C_{g d i}+C_{g d}\right)  \tag{1}\\
\operatorname{Im}\left(Y_{12}\right) & =-j \omega\left(C_{g d i}+C_{g d}\right)  \tag{2}\\
\operatorname{Im}\left(Y_{22}\right) & =j \omega\left(C_{p d}+C_{d s i}+C_{d s}+C_{g d i}+C_{g d}\right) \tag{3}
\end{align*}
$$

where, $\omega=2 \pi f$ is the angular frequency. At high frequencies
( $f>10 \mathrm{GHz}$ ) the equivalent circuit for unbiased FET is shown in Fig. 2(b). The $Z$-parameter can be written as:

$$
\begin{align*}
& Z_{11}=R_{g}+R_{i}+R_{s}+j \omega\left(L_{g}+L_{s}\right)+\frac{1}{j \omega}\left(\frac{1}{C_{g}}+\frac{1}{C_{s}}\right)  \tag{4}\\
& Z_{12}=R_{i}+R_{s}+j \omega L_{s}+\frac{1}{j \omega C_{s}}  \tag{5}\\
& Z_{22}=R_{d}+R_{i}+R_{s}+R_{g d}+j \omega\left(L_{s}+L_{d}\right)+\frac{1}{j \omega}\left(\frac{1}{C_{d}}+\frac{1}{C_{s}}\right) \tag{6}
\end{align*}
$$

The optimization algorithm based method is adopted to determine all the parameters due to the large number of unknown parameters in Eq. (1)-Eq. (6), First, the parasitic inductances $L_{g}, L_{s}, L_{d}$ can be calculated by the slopes of straight lines interpolating the experimental data of the imaginary parts of the $Z$-parameters multiplied by the angular frequency $\omega$ versus $\omega^{2} . C_{p g}=a C_{g s i}=b C_{g s}, C_{p d}=c C_{d s i}=$ $d C_{d s}, C_{g d}=e C_{g d i}, R_{i}=x R_{g d}$ and $R_{g}=g R_{d}$ are defined based on the geometry of device. Then, the $Y$-parameters of intrinsic $\left(Y_{i n t}\right)$ elements could be extracted after eliminating the effect of the parasitic parameters [12-14]. Finally, the optimization algorithm is used to extract all parameters. In order to improve the optimization efficiency and accuracy, the optimization ranges and steps of the seven ratio parameters $(a, b, c, d, e, x, g)$ are set to reasonable values. The simple genetic algorithm (GA) is used as the optimization algorithm [15]. The extracted parameters are shown in Table 1, and good agreements are achieved between measurement results and calculated results (shown in Fig. 3).

Table 1. The calculated parameters (capacitances in fF , inductances in nH , resistances in Ohm , and conductance in mS ) for 36 mm gate periphery AlGaN/GaN HEMT.

| $C_{p g}$ | $C_{g s i}$ | $C_{g s}$ | $C_{p d}$ | $C_{d s i}$ | $C_{d s}$ | $C_{g d}$ | $C_{g d i}$ | $L_{g}$ | $L_{s}$ | $L_{d}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0.09 | 10.94 | 0.86 | 1.29 | 0.17 | 0.10 | 0.10 | 0.11 | 0.45 | 0.17 | 4.49 |
| $R_{g}$ | $R_{d}$ | $R_{s}$ | $R_{g s}$ | $R_{i}$ | $R_{g d}$ | $G_{d s}$ | $g_{m}$ | $\tau$ | $a$ | $b$ |
| 7.09 | 26.07 | 1.10 | 12.00 k | 0.47 | 1.84 | 0.83 | 278.00 | 1.20 ns | 0.92 | 11.65 |
| $c$ | $d$ | $e$ | $x$ | $g$ |  |  |  |  |  |  |
| 7.87 | 12.49 | 0.97 | 0.26 | 0.27 |  |  |  |  |  |  |



Figure 3. Comparisons of calculated (solid line) and measured $S$ parameters (triangle line) at $V_{g s}=-1.4 \mathrm{~V}, V_{d s}=28 \mathrm{~V}$ in the frequency range from 0.1 GHz to 4.5 GHz .

## 3. LARGE-SIGNAL EQUIVALENT CIRCUIT MODEL

Figure 4 shows the AlGaN/GaN HEMT large-signal equivalent circuit topology. Typically, there are three main nonlinear elements: sourcedrain current $\left(I_{d s}\right)$, gate-source capacitor $\left(C_{g s}\right)$, and gate-drain capacitor $\left(C_{g d}\right)$. A modified $I_{d s}$ model based on the Angelov model is presented

$$
\begin{align*}
I_{d s} & =I_{p k}\left(1+\tanh \left(f_{1}\right)\right)\left(1+f_{2} V_{d s}\right) \tanh \left(D V_{d s}\right)  \tag{7}\\
f_{1} & =p_{1}\left(V_{g s}-v_{p k}\right)+p_{2}\left(V_{g s}-v_{p k}\right)^{2}+p_{3}\left(V_{g s}-v_{p k}\right)^{3}  \tag{8}\\
I_{p k} & =\frac{I_{p k 0}}{A\left(V_{d s}^{p} V_{g s}^{q}\right)+B V_{d s}^{0.6 V_{g s}}+C} \times \frac{K}{\exp \left(\frac{T-300}{200}\right)}  \tag{9}\\
v_{p k} & =F+G V_{d s}  \tag{10}\\
f_{2} & =H \exp \left(M\left|V_{g s}\right|^{Q}\right) \tag{11}
\end{align*}
$$

where, $V_{d s}$ is the drain to source voltage; $V_{g s}$ is the gate to source voltage; $I_{p k}$ is the saturation current and $V_{p k}$ is the knee voltage; $A$, $B, C, D, p_{1}, p_{2}$, and $p_{3}$ are constants; $F$ and $G$ are used to describe the $V_{d s}$ effect on knee voltage caused by short-channel effects. Compared with Angelov model, two main modifications have been added:


Figure 4. AlGaN/GaN HEMT large-signal equivalent circuit topology.


Figure 5. For (a) Comparison between calculated $I-V$ results by using modified model and original model and measurement date on one cell device ( $T=300 \mathrm{~K}$ ). For (b) $I-V$ curve at different ambient temperatures on one cell $\left(V_{g s}=-1.2 \mathrm{~V}\right)$.
a) Self-heating effect. The saturation current decreases duo to the self-heating effect at high bias current, so an compact expression (term including $A, B$, and $C$ ) is added to the denominator of Eq. (9).
b) Temperature dependent effect. $T$ represents the ambient temperature, and $K$ is a correction factor.
Due to the large effect of self-heat and ambient temperature, a small gate periphery device (one cell with 2 mm gate width) is measured and used to validate the proposed model. Fig. 5(a) shows the comparisons of calculated and measured results, and a good agreement has been achieved with consideration of self-heat effect. Fig. 5(b) shows the calculated $I_{d s}$ at different $T$. The results show that even with good
thermal conductivity of AlGaN/GaN HEMT, the self-heat effect and ambient temperature still have important effects on the performance of the device.

The modified model of $C_{g s}$ and $C_{g d}$ based on Angelov model are given below:

$$
\begin{align*}
& f_{a i 1}=M_{1}+P_{11} * v_{g s}+P_{111} * \frac{\left|v_{g s}\right|}{10 * v_{d s}}  \tag{12}\\
& f_{a i 2}=M_{2} * v_{g s}+P_{21} *\left(M_{21}+v_{g s}+\frac{\left|v_{g s} * v_{d s}\right|}{10}\right)  \tag{13}\\
& C_{g s}=C_{g s 0}+C_{g s 0} *\left(1+\tanh \left(f_{a i 1}\right)\right) *\left(1+\tanh \left(f_{a i 2}\right)\right) \tag{14}
\end{align*}
$$

where, $V_{g s}$ and $V_{d s}$ are both added to $f_{a i 1}$ and $f_{a i 2}$ in order to express the dual modulation effect of channel.

$$
\begin{equation*}
C_{g d}=N_{1}+N_{2} *\left(1+\exp \left(N_{3} * v_{g s}+N_{4}\right)\right) * \exp \left(N_{5} * v_{d s}\right) \tag{15}
\end{equation*}
$$

where, the exponent function is used instead of hyperbolic tangent function. Fig. 6 shows the comparison of calculated results and measured results based on multi-bias SSECM.


Figure 6. The fitting curve (solid line) for the (a) $C_{g s}$ and (b) $C_{g d}$ extracted from small-signal model based on measurement dates (triangle).

## 4. POWER AMPLIFIER CIRCUIT DESIGN

The LSECM is implemented in Advanced Design System (ADS) by using symbolic defined devices (SDD). The parasitic parameters are keeping constant extracted from SSECM. In the design of the power amplifier, the frequency range is from 3.3 GHz to 3.8 GHz and the bias conditions are chosen at $V_{g s}=-1.4 \mathrm{~V}$ and $V_{d s}=28 \mathrm{~V}$, which is typical operation bias for class A in the device. By comprehensive consideration of stability, gain and maximum power output, the input


Figure 7. Schematic of input/output matching of (a) the power amplifier circuit, (b) the final power amplifier, and (c) measurement setup for power amplifier.


Figure 8. Gain and Output power characteristic between simulation results and measurements at different ambient temperatures biased at $V_{g s}=-1.4 \mathrm{~V}$ and $V_{d s}=28 \mathrm{~V}$ (for (a) input power $P_{i n}=20 \mathrm{dBm}$, for (b) $f=3.7 \mathrm{GHz}$ ).
impedance is set to $5.8+j * 0.5$ and the output impedance is set to $6.1-j *$ 14.4. The impedance matching circuits are shown in Fig. 7(a), and the final circuit is made on the substrate of ROGERS 4350 [16, 17].

The measurement setup of the power amplifier (DUT) is shown in Fig. 7(c). The input signal was supplied by Agilent N5183 microwave analog signal generator cascaded by an isolator. The output of the amplifier was measured by directional coupler and power meter Agilent E4417. Figs. 8(a) and (b) show the simulated gain and output power characteristic by using proposed LSECM model at different temperatures, respectively. And the results fit the measurements well. In the interested frequency band, the linear gain for the amplifier is about 8.5 dB at 300 K with 46 dBm output power, and they decrease dramatically when ambient temperature go up to more than 350 K .

## 5. CONCLUSION

A LSECM for package large size AlGaN/GaN HEMT is established in this paper. The self-heat and temperature effect are considered in $I-V$ model, and the nonlinear capacitors are extracted from 19 elements SSECM and directly used in multi-bias measurement of large gate periphery device. An amplifier is designed by using the proposed model for validation purpose, and the results show that the simulated results fit the measurements well. The proposed model can be used to analysis temperature effect on AlGaN/GaN power HEMT and design high power GaN HEMT amplifier.

## ACKNOWLEDGMENT

Thanks go to our friend from the 38th research institute of China Electronics Technology Group Corporation (CETC-38), who has given great support on the study. This work is supported by National Science Foundation of China part under Grant 60701017 and part under Grant 60876052.

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