## DUAL-MODE CPW-FED DOUBLE SQUARE-LOOP RESONATORS FOR WLAN AND WIMAX TRI-BAND DESIGN

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Abstract—An improved CPW-fed configurations with dual-mode double-square-ring resonators (DMDSRR) for tri-band application is proposed in this paper. The resonant frequency equations related to DMDSRR geometry are introduced for simply designing tri-band bandpass filter (BPF). Resonant frequencies and transmission zeroes can be controlled by tuning the perimeter ratio of the square rings. To obtain lower insertion loss, higher out-of-band rejection level and wider bandwidth of tri-band, the improved coplanar waveguide (CPW) fed and the step impedance resonator (SIR) and meander line dual-mode perturbations are designed. The effective design procedure is provided. The proposed filter is successfully simulated and measured. It can be applied to WLAN (2.45, 5.20 and 5.80 GHz) and WiMAX (3.50 GHz) systems.

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#### 1. INTRODUCTION

The increasing demand for multi-band applications has required a single wireless transceiver to support multi-band operations. The multi-band BPFs play an important role in a multi-band transceiver, such as dual-band [1-4], tri-band [5-19] and quad-band [20-22] filters.

Recently, a new excitation for DMDSRR with CPW was proposed for dual-band applications [1]. The square ring resonators with backto-back and concentric configurations were presented. Due to the effect of the CPW input/output structure, performance with low insertion loss and high out-of-band rejection level was achieved. In [5], the even/odd-mode method with equivalent circuit was proposed and designed with the split-ring resonator (SRR) to obtain three controllable resonant frequencies. In [6], the coupling-matrix design for tri-band filter was presented. In [7], the authors developed the frequency transformation for finding the locations of poles and zeros of specific tri-band filters. Moreover, various filters have been realized with the basic SIR and their variety to exhibit tri-band responses [8– 13.15]. Recently, for tri-band filter design, the stub-loaded resonators (SLR) and half-wavelength resonators were presented [16]. And a microstrip and a defeated ground structure (DGS) slot were used [17]. Applied for WLAN and WiMAX tri-band systems, the open and short stubs loaded crossed resonator were designed [14]. And the SLR and DGS resonator were used [18].

Whether the combined quarter-wavelength SIR or assembled halfwavelength SIR was used, the impedance ratio computation and tuning the stub were needed [9–12, 19]. For SLR filter, the stub length was tuned for the desired responses [12, 16–18]. On the other hand, in [8], three closed-form equations related to the resonant frequencies of the tri-band were deduced for simple design. Similarly, in [21], four simple equations related to the perimeters of the concentric rings were approximated for the quad-band design.

Based on [1] and [21], this paper proposes a novel way with the resonant frequency equations related to DMDSRR geometry for simply designing tri-band BPF. It can be applied to WLAN (2.45, 5.20 and 5.80 GHz) and WiMAX (3.50 GHz) tri-band systems. Tuning the perimeter ratios of the rings presents the controllable resonant frequencies. For excitation of DMDSRR, the filter is fed by an improved CPW-fed line. The improved CPW-fed line consists of a twin-T feed line and the branches with slits. In addition, by using novel SIR and square perturbations, the novel dual-mode DMDSRR is proposed. The simulation and measurement results, including frequency responses and tri-band versus perimeter ratio, are presented to analyze the tri-band characteristic.

### 2. FILTER CONFIGURATIONS AND BASIS

The perimeters of the square rings are related to the guided wavelength at corresponding resonant frequencies. Thus, the resonant frequencies of the tri-band can be approximately expressed as [21, 23]:

$$f_1 = \frac{c}{4L_1\sqrt{\varepsilon_{eff}}} \tag{1}$$

$$f_2 = \frac{c}{(4L_2 + \Delta\ell)\sqrt{\varepsilon_{eff}}} \tag{2}$$

$$f_{3a} = \frac{c}{2L_1\sqrt{\varepsilon_{eff}}} \tag{3}$$

$$f_{3b} = \frac{c}{(2L_2 + \Delta\ell)\sqrt{\varepsilon_{eff}}} \tag{4}$$

$$\Delta \ell = W_3 + W_4 - g_1 \tag{5}$$

where c is the speed of light in free space,  $L_1$  and  $L_2$  denote the side lengths of the two rings, and  $\varepsilon_{eff}$  represents the effective permittivity of the substrates.

The ring related to the larger side-length  $(L_1)$  decides the resonant frequencies  $f_1$  in first band and the  $f_{3a}$  in third band, and the ring related to the smaller side-length  $(L_2)$  represents the resonant frequencies  $f_2$  in second band and the  $f_{3b}$  in third band shown in Fig. 1(a). The electrical length of  $\Delta \ell$  related to the meander line is used to increase the perimeter of the smaller ring. Both  $f_{3a}$  and  $f_{3b}$ are the lower and upper resonant frequencies in the third band. The ring perimeters will be utilized to control the center frequencies. It can be obtained from (1), (2), (3) and (4) as follows:

$$\frac{L_2}{L_1} = \frac{f_1}{f_2} = \frac{f_{3a}}{f_{3b}} \tag{6}$$

Based on (6), two perimeters can be properly selected to facilitate the filter design.

Obviously, it is difficult to feed the square rings if the length difference of the two side lengths is quite large. Therefore, the CPW with parallel couplings is preferred. For dual-band responses, the square rings were fed by a twin-T CPW [1]. For excitation of triband responses, the square rings are fed by an improved twin-T CPW. The improved twin-T CPW consists of a feed-line and the branches with the slits shown in Fig. 1(b). The widths of the slits are expressed by  $W_{q1}$ , and the length is  $L_{q1}$ . Transmission zeros can be obtained



**Figure 1.** CPW-fed DMDSLR configurations. (a) Top view DMDSLR. (b) Bottom view twin-T CPW.

by tuning  $W_{g1}$ , and  $L_{g1}$ . The width of 50  $\Omega$  line is given by  $W_{s1}$ , and the spacing is given by  $g_{b1}$ . Impedance matching can be improved by adjusting  $W_{s1}$  and  $g_{b1}$ .

Physical dimensions are stated:

- (a) Tri-band DMDSLR with  $L_1 = 20.2 \text{ mm}$ ,  $L_2 = 12.5 \text{ mm}$ , S = 3.54 mm,  $W_1 = 2.5 \text{ mm}$ ,  $W_2 = 3.0 \text{ mm}$ ,  $W_3 = 3.5 \text{ mm}$ ,  $W_4 = 3.55 \text{ mm}$ ,  $P_1 = 3.3 \times 3.3 \text{ mm}^2$ , and  $g_1 = 1.17 \text{ mm}$ .
- (b) twin-T CPW<sub>1</sub> configuration with  $d_{b1} = d_{b3} = 6.045 \text{ mm}, d_{b2} = 3.15 \text{ mm}, g_{b1} = 0.2 \text{ mm}, g_{b2} = 0.4 \text{ mm}, g_{b3} = 0.4 \text{ mm}, W_{s1} = 2.4 \text{ mm}, W_{s2} = 0.5 \text{ mm}, W_{b1} = 1.4 \text{ mm}, W_{b2} = 2 \text{ mm}, W_{g1} = 0.4 \text{ mm}, L_{g1} = 4.8 \text{ mm}, \text{ and } W_{t1} = 0.33 \text{ mm}.$

#### **3. SIMULATION AND MEASUREMENT RESULTS**

The simulations for dual-mode DMDSRR are achieved with IE3D [24]. The Roger-3003 substrate with dielectric constant  $\varepsilon_r = 3.0$ , loss tangent  $\delta = 0.0013$  and thickness h = 1.57 mm is used. For the 50  $\Omega$  line, the width is 2.8 mm, length is 16.70 mm, effective dielectric constant  $\varepsilon_{eff} = 2.48$  and guided wavelength  $\lambda g = 73 \text{ mm}$ , 5 mm and 37 mm for the frequencies  $f_0 = 2.45 \text{ GHz}$ , 3.50 GHz and 5.20 GHz respectively.

Since the central frequencies of the responses are decided by the square loop dimensions, and the fractional BW are mainly related to the size of perturbation and the width of SIR, the variations of the parameters are investigated. The size of perturbation increases, the fractional BW in the first band increases slightly, and  $P_1 = 3.3 \times 3.3 \text{ mm}^2$  is chosen at first. Then, the width of SIR decreases, the fractional BW in the second band increases slightly, and  $g_1 = 1.17$  is determined. Consequently, tri-band adjustment related to perimeter ratio, tuning is needed. The perimeter ratio can be represented with the side-length ratio ( $t = L_1/L_2$ ). If tuning in the range of  $1.30 \leq t \leq 1.33$ , and tri-band response is obtained.

#### **3.1. Frequency Responses**

The proposed tri-band BPF is simulated and measured with  $S_{21}$  and  $S_{11}$  frequency responses in Fig. 2. Clearly, both the simulated and measured results have good agreement. The dual-mode behaviors are presented in each band. All the tri-band responses are listed in Table 1. The lower insertion loss and higher out-of-band rejection level and wider band of the responses are obtained and it is suitable for tri-band applications. Calculation by (1) to (5), the tolerances (less than 10%) related to the measurements are also listed. The resonated frequencies shift down slightly due to the perturbation included environmental effects (temperature and interference possible).



Figure 2. Frequency responses of tri-band.

Tri-band	Band-I	Band-II	Band-III
Frequency (GHz)	2.48	349	4.97
$-3 \mathrm{dB} \mathrm{BW} \mathrm{(MHz)}$	130	240	1820
Fractional BW (%)	5.2	6.9	36.6
Maximum insertion loss (dB)	188	165	0.93
Resonances (GHz)	2.45/2.51	3.43/3.55	4.55/4.76/5.19/5.76
Transmission zero level (dB)	-48.3/-51.7	-51.7/-36.9	-36.9/-22.6
Calculation (GHz)	2.36	3.41	5.39
Tolerance (%)	4.8	2.3	8.5

Table 1. Results of tri-band responses.

#### 3.2. Surface Current Distributions

Figure 3 presents the surface current distribution of tri-band DMDSRR with even and odd-modes. At the resonated frequencies in band I and II, in left column, the outer and inner rings exhibit the identical surface current distributions according to  $TM_{110}$  configuration with two more coupled magnitudes (red color) and two less coupled magnitudes (blue color) individually. Each band involves the even and odd-modes. Among the even-mode, the perturbation effects occur and the resonated frequency shifts down slightly.

In middle column, four more coupled magnitudes (red color) and four less coupled magnitudes (blue color) correspond to  $TM_{210}$  configurations are observed. The four resonated frequencies are presented in band III. Similarly, dual-mode and perturbation effects are viewed. In right column, four transmission zeroes are presented less coupled magnitudes (blue color) less coupled magnitudes (blue color) in output port. Fig. 4 presents the photograph of the proposed tri-band filters.

#### 3.3. Comparison

When compared with the SLR filters at the same design frequency of WLAN and WiMAX system [14, 18], the performance of three filters are listed in Table 2. All filters cover the required bandwidths for WLAN band (2.4–2.48 GHz and 5.15–5.35 GHz) and WiMAX (3.4–3.6 GHz) applications. The proposed filter in this paper can significantly expend the 5.2 GHz response up to 5.8 GHz (Fractional BW = 36.6%). It covers the complete WLAN band (2.4–2.48 GHz,



Figure 3. Surface current distribution of tri-band DMDSRR.

5.15–5.35 GHz, and 5.725–5.825 GHz). The frequency response and bandwidth in the third band are improved in the proposed filter. The return loss with in the passband is better than 20 dB and the maximum insertion losses are 1.88, 165, and 0.93 dB in the proposed filter. The maximum attenuation between the first and second passbands is 51.7 dB. The compact size is  $28 \times 28 \times 1.57$  mm<sup>3</sup> which is smaller the work of [18].



Figure 4. Photography of the proposed tri-band filters.

Tri-band	Short/open	SLR and	This proposed
filters	SLR [11]	DGS [15]	DMDSLR
Resonance			
frequency	2.4, 3.5  and  5.2	2.44, 3.53, and 5.26	2.44,  3.5,  5.2,  and  5.8
(GHz)			
$-3\mathrm{dB}$	180 410 and 210	300, 22, and 170	130, 24, and 1820
BW(MHz)	160, 410, and 210		
Fractional	75, 117, and 4.03	123 62 and 33	5260 and $366$
BW (%)	<i>1.5</i> , 11.7, and 4.05	12.5, 0.2, and 5.5	5.2, 0.9, and 50.0
Maximum			
insertion	1.4, 1.1, and 1.7	0.9, 1.7, and 2.1	1.88, 1.65, and 0.93
loss (dB)			
Attenuation	50 43 46 and 35	32, 14, 18, and 27	48.3, 51.7, 36.9,
(dB)	50, 45, 40, and 55		and 22.6
Size $(mm^3)$	$17.1\times17.4\times0.8$	$32 \times 39.5 \times 2.7$	$28\times28\times1.57$

Table 2. Three tri-band filters for comparison.

# 3.4. Design Procedure

For accurate design, the effective procedure is described as follows:

Step 1. Determine the center frequency  $f_1$ ,  $f_2$  and  $(f_{3a} + f_{3b})/2$  of each band.

Step 2. Select the substrate with dielectric constant, loss tangent and thickness.

Step 3. Calculate the larger side-length  $(L_1)$  and the smaller side-length  $(L_2)$  of DMDSLR by (1)–(4).

Step 4. Tune the ring perimeters to control the center frequencies by (5).

Step 5. Adjust the SIR size and meander-line width of perturbation.

Step 6. Check if perturbation could satisfy the factional bandwidth BW.

Step 7. Modify the I/O twin-T couplings structure.

Step 8. Carry out the tri-band filter.

# 4. CONCLUSIONS

The CPW-fed DMDSRR and the resonant frequency equations for triband BPF propose a viable alternative to current multi-band filter design techniques. Based on the inherent high-Q characteristics of the ring resonators, it is found that the CPW-fed DMDSRR filter can successfully present good tri-band pass-band performance, high stopband rejection and deep transmission zeros between pass-bands. The resonant frequency equations and the design procedure are available and useful for simply designing tri-band BPF. Tuning the perimeter ratios of the rings provides four controllable resonant frequencies. Transmission zeros can be obtained by tuning the slits in the branch of the twin-T CPW.

The proposed filter has three good response bandwidths  $(S_{11}$  better than 10 dB) of 160 MHz (about 6.3% centered at 2.44 GHz), 250 MHz (about 7.3% centered at 3.50 GHz) and 1400 MHz (about 26.8% centered at 5.18 GHz), which make it easily cover the required bandwidths for WLAN band (2.4–2.48 GHz, 5.15–5.35 GHz, and 5.725–5.825 GHz) and WiMAX (3.4–3.6 GHz) applications.

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