

A Joint Parameter Estimation Method with Conical Conformal CLD Pair Array

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Abstract—A novel direction of arrival (DOA) and polarization estimation method with sparse conical conformal array consisting of concentric loop and dipole (CLD) pairs along the z -axis direction is proposed in this paper. In the algorithm, the DOA and polarization information of incident signals are decoupled through transformation to array steering vectors. According to the array manifold vector relationship between electric dipoles and magnetic loops, the signal polarization parameters are given. The phase differences between reference element and elements on upper circular ring are acquired from the steering vectors of upper circular ring, it can be used to give rough but unambiguous estimates of DOA. The phase differences are also used as coarse references to disambiguate the cyclic phase ambiguities in phase differences between two array elements on lower circular ring. Without spectral peak searching and parameter matching, this method has the advantage of small amount of calculation. Finally, simulation results verify the effectiveness of the algorithm.

1. INTRODUCTION

In the last few years, thanks to the advances in sensor technology, electromagnetic vector sensor (EMVS) array is widely used in communication system due to its polarization diversity. The problem of estimating signal polarizations along with arrival angles has been discussed previously in many articles [1–17]. The first direction-finding algorithms, explicitly exploiting all six electromagnetic components, have been developed by Nehorai and Paldi [1, 2] and Li [4], respectively. The cross-product-based direction of arrival (DOA) estimation algorithm was first adapted to ESPRIT by Wong and Zoltowski [5, 6]. The uni-vector-sensor ESPRIT and MUSIC algorithm were proposed in [7, 8], respectively. In fact, the aforementioned literatures mostly discuss the six collocated and orthogonally oriented electromagnetic sensors, which is called “complete” EMVS. The “incomplete” EMVS antenna configuration has been extensively studied by many authors, such as two identical dipoles [9–11], two identical loops [12, 13], triad dipole or triad loop [14, 15], etc. [16, 17]. In contrast to “complete” and other “incomplete” EMVS as described above, collocated loops and dipoles (CLD) along the z -axis are easier to realize the decoupling of polarization and angle of arrival parameters because of its simple structure. Polarization parameter estimation based on CLD pair is independent of the source’s direction-of-arrival and requires no prior information of azimuth and elevation angles. This independence cannot be applied to other antenna configuration.

Parameter estimation based on conformal antenna array has been a hot topic for a number of years. In particular, conformal array antennas potentially meet the needs of a variety of airborne radar and other defense applications [18, 19]. The benefits include reduction of aerodynamic drag, wide angle coverage, space savings, potential increase in available aperture [20]. Conical conformal array is typical of many conformal arrays. In contrast to planar arrays, when conical conformal array is used

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for wide range (more than 90 degrees) elevation angle estimation, it does not introduce ambiguity in elevation angle. Diversely polarized antenna arrays have been exploited in a number of direction finding algorithms. The proposed work discusses CLD pairs oriented along the z axis of Cartesian coordinate. Compared with “complete” EMVS, mutual coupling between CLD pair component antennas can be greatly decreased.

ESPRIT represents a highly popular eigenstructure based parameter estimation method, which has better performance in narrow-band condition. But in practice, the methods are often demanded to work in a wide frequency band. That means the array will have a large aperture, and result in an improper array configuration. It is well known that the uniform intersensor spacing beyond a half-wavelength will lead to a set of cyclically ambiguous of array manifold matrix [6, 21, 22]. Thanks to the circular symmetry, uniform circular array (UCA) in [23] and uniform concentric circular array (UCCA) in [24, 25] are attractive antenna configurations in the context of DOA estimation. A uniform multiple circular ring CLD arrays arranged on a conical surface is researched in this paper.

The purpose of this paper is to study ESPRIT high-resolution algorithm of estimating parameters with a sparse conical conformal CLD pairs (CCCP) array. The CCCP is a three-dimensional space surrounding the array, which can resolve the signal from all the directions. The main motivation of this paper is to take advantage of the equal central angle of the upper circular ring array elements and the corresponding array element of lower circular ring. The upper circular ring, which suffers no phase ambiguity, is used to find the coarse DOA estimates to disambiguate cyclically ambiguous estimates from the lower circular ring with the larger array aperture.

2. PROBLEM FORMULATION

K narrowband completely polarized electromagnetic plane wave source signals from far-field impinge upon a CCCP array, which is composed of N identical CLD pairs, as shown in Figure 1. For the CLD pairs, the dipoles parallel to the z -axis are referred to as the z -axis dipoles and the loops parallel to the x - y plane as the x - y plane loops, respectively measuring the z -axis electric field components and the z -axis magnetic field components. The CLD pairs' steering vector of the k th ($1 \leq k \leq K$) unit-power electromagnetic source signal is the following 2×1 vector [4, 26]:

$$\mathbf{a}(\theta_k, \gamma_k, \eta_k) = \begin{bmatrix} e_{kz} \\ h_{kz} \end{bmatrix} = \begin{bmatrix} -\sin \theta_k \sin \gamma_k e^{j\eta_k} \\ \sin \theta_k \cos \gamma_k \end{bmatrix} \quad (1)$$

where $\theta_k \in [0, \pi]$ is the signal's elevation angle measured from the positive z -axis, $\gamma_k \in [0, \pi/2]$ the auxiliary polarization angle, and $\eta_k \in [-\pi, \pi]$ the polarization phase difference. The z -axis electric field e_{kz} and z -axis magnetic field h_{kz} both involve the same factor, so polarization estimation based on CLD

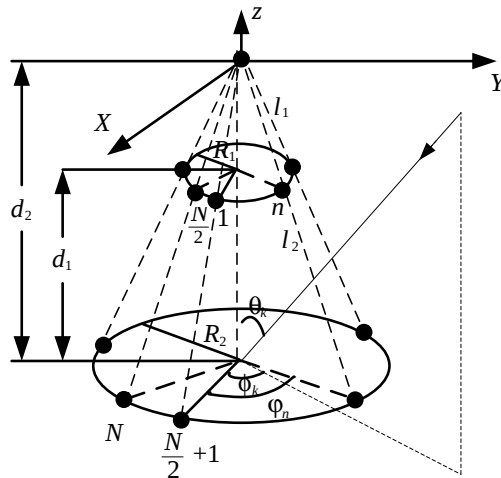


Figure 1. CCCP array geometry.

pairs is independent of the source's direction-of-arrival, and it requires no prior information of azimuth and elevation angles.

Without loss of generality, we assume that the reference element is placed at the conical tip (origin). The distances between the reference element and the upper circular ring elements are equal to l_1 ($l_1 \leq 0.5\lambda_{\min}$), and the distances between the reference element and the lower circular ring elements are equal to l_2 ($l_2 \gg 0.5\lambda_{\min}$) where $\lambda_{\min}$ is the minimal signals' wavelength of the incident signals. On the upper circular ring, there are $N/2$ elements, which have the same angle position as that on the lower circular ring. Then the data collected by the CCCP array at time t can be represented as

$$\mathbf{X}(t) = \begin{bmatrix} \mathbf{A}_1 \\ \mathbf{A}_2 \end{bmatrix} \mathbf{S}(t) + \mathbf{N}(t) = \mathbf{A}\mathbf{S}(t) + \mathbf{N}(t) \quad (2)$$

where $\mathbf{X}(t)$ is the received signal, $\mathbf{A}$ the $(2N+2) \times K$ steering vector matrix of K incident signals, $\mathbf{S}(t)$ the incident signal, and $\mathbf{N}(t)$ the noise. $\mathbf{A}_1$ and $\mathbf{A}_2$ are sub-array steering vectors of $N+1$ loops and $N+1$ dipoles, respectively, which can be expressed as

$$\mathbf{A}_1 = \begin{bmatrix} \sin \theta_1 \cos \gamma_1 \otimes \mathbf{q}(\theta_1, \phi_1) \\ \sin \theta_2 \cos \gamma_2 \otimes \mathbf{q}(\theta_2, \phi_2) \\ \vdots \\ \sin \theta_K \cos \gamma_K \otimes \mathbf{q}(\theta_K, \phi_K) \end{bmatrix}^T \quad (3)$$

$$\mathbf{A}_2 = \begin{bmatrix} -\sin \theta_1 \sin \gamma_1 e^{j\eta_1} \otimes \mathbf{q}(\theta_1, \phi_1) \\ -\sin \theta_2 \sin \gamma_2 e^{j\eta_2} \otimes \mathbf{q}(\theta_2, \phi_2) \\ \vdots \\ -\sin \theta_K \sin \gamma_K e^{j\eta_K} \otimes \mathbf{q}(\theta_K, \phi_K) \end{bmatrix}^T \quad (4)$$

$$\mathbf{q}(\theta_k, \phi_k) = [1, \mathbf{q}_u^T(\theta_k, \phi_k), \mathbf{q}_d^T(\theta_k, \phi_k)] \quad (5)$$

where $\mathbf{q}(\theta_k, \phi_k)$ is the spatial steering vector of whole CCCP array, $\mathbf{q}_u(\theta_k, \phi_k)$ and $\mathbf{q}_d(\theta_k, \phi_k)$ are respectively that of the upper and lower circular ring sub-array.

$$\mathbf{q}_u(\theta_k, \phi_k) = \begin{bmatrix} e^{j \frac{2\pi R_1 (\sin(\theta_k) \cos(\phi_k - \varphi_1) - \frac{d_2 - d_1}{R_1} \cos \theta_k)}{\lambda}} \\ \vdots \\ e^{j \frac{2\pi R_1 (\sin(\theta_k) \cos(\phi_k - \varphi_{\frac{N}{2}}) - \frac{d_2 - d_1}{R_1} \cos \theta_k)}{\lambda}} \end{bmatrix} \quad (6)$$

$$\mathbf{q}_d(\theta_k, \phi_k) = \begin{bmatrix} e^{j \frac{2\pi R_2 (\sin(\theta_k) \cos(\phi_k - \varphi_{\frac{N}{2}+1}) - \frac{d_2}{R_2} \cos \theta_k)}{\lambda}} \\ e^{j \frac{2\pi R_2 (\sin(\theta_k) \cos(\phi_k - \varphi_{\frac{N}{2}+2}) - \frac{d_2}{R_2} \cos \theta_k)}{\lambda}} \\ \vdots \\ e^{j \frac{2\pi R_2 (\sin(\theta_k) \cos(\phi_k - \varphi_N) - \frac{d_2}{R_2} \cos \theta_k)}{\lambda}} \end{bmatrix} \quad (7)$$

with $\varphi_n = 4\pi(n-1)/N$ $n = 1, \dots, N$ are the angular position of array elements, and ϕ_k denotes signal's azimuth angle measured from positive x -axis. The general assumption is that $\mathbf{A}_1$ and $\mathbf{A}_2$ are full-rank matrices. The covariance matrix $\mathbf{R}_x$ is given by

$$\mathbf{R}_x = \mathbf{A}\mathbf{R}_s\mathbf{A}^H + \sigma^2\mathbf{I} \quad (8)$$

where $\mathbf{R}_s$ is the covariance matrix of incident signals and σ^2 the additive white noise power. Let $\mathbf{E}_s$ be the $(2N+2) \times K$ matrix composed of the K eigenvectors corresponding to the K largest eigenvalues of $\mathbf{R}_x$, and $\mathbf{E}_n$ denotes the $(2N+2) \times (2N+2-K)$ matrix composed of the remaining $2N+2-K$

eigenvectors of $\mathbf{R}_x$. According to the subspace theory, the signal subspace can be expressed explicitly as

$$\mathbf{E}_s = \mathbf{A}\mathbf{T} = \begin{bmatrix} \mathbf{A}_1 \\ \mathbf{A}_2 \end{bmatrix} \mathbf{T} \quad (9)$$

$$\mathbf{E}_{s1} = \mathbf{A}_1 \mathbf{T} \quad (10)$$

$$\mathbf{E}_{s2} = \mathbf{A}_2 \mathbf{T} = \mathbf{A}_1 \Phi \mathbf{T} \quad (11)$$

where $\Phi = \text{diag}([-\tan \gamma_1 e^{j\eta_1}, \dots, -\tan \gamma_K e^{j\eta_K}])$ polarization parameters can be got from Φ

$$\begin{cases} \gamma_k = \tan^{-1}(|\Phi_{kk}|) \\ \eta_k = \arg(-\Phi_{kk}) \end{cases} \quad (12)$$

Since both $\mathbf{E}_1$ and $\mathbf{E}_2$ are full-rank, there exists a unique nonsingular matrix Ω such that

$$\mathbf{E}_{s1} \Omega = \mathbf{E}_{s2} \Rightarrow \Omega = (\mathbf{E}_{s1}^H \mathbf{E}_{s1})^{-1} \mathbf{E}_{s1}^H \mathbf{E}_{s2} \quad (13)$$

$$\Omega \mathbf{T}^{-1} = \mathbf{T}^{-1} \Phi \quad (14)$$

Equation (14) implies that Φ is a diagonal matrix whose diagonal elements are composed of the K eigenvalues of space-polarization matrix Ω , and the full-rank matrix $\mathbf{T}^{-1}$ is composed of the K eigenvectors of matrix Ω . Then, $\mathbf{A}_1$ can be calculated by

$$\mathbf{A}_1 = \mathbf{E}_{s1} \mathbf{T}^{-1} \quad \mathbf{A}_2 = \mathbf{E}_{s2} \mathbf{T}^{-1} \quad (15)$$

The space steering vector estimates of upper circular ring is given:

$$\tilde{\mathbf{q}}_u(\tilde{\theta}_k, \tilde{\phi}_k) = \frac{\hat{\mathbf{A}}_1(2 : \frac{N}{2} + 1, k)}{\hat{\mathbf{A}}_1(1, k)} = \frac{\hat{\mathbf{A}}_2(2 : \frac{N}{2} + 1, k)}{\hat{\mathbf{A}}_2(1, k)} \quad (16)$$

Equation (16) can be represented as follows:

$$\tilde{\mathbf{q}}_u(\tilde{\theta}_k, \tilde{\phi}_k) = \begin{bmatrix} e^{j \frac{2\pi R_1 (\sin \tilde{\theta}_k \cos(\tilde{\phi}_k - \varphi_1) - \frac{d_2 - d_1}{R_1} \cos \tilde{\theta}_k)}{\lambda}} \\ \vdots \\ e^{j \frac{2\pi R_1 (\sin \tilde{\theta}_k \cos(\tilde{\phi}_k - \varphi_{\frac{N}{2}}) - \frac{d_2 - d_1}{R_1} \cos \tilde{\theta}_k)}{\lambda}} \end{bmatrix} \quad (17)$$

According to Formula (17), the following relationship can be obtained:

$$\Phi_1 = \arg(\tilde{\mathbf{q}}_u(\tilde{\theta}_k, \tilde{\phi}_k)) = \begin{bmatrix} \frac{2\pi R_1 (\sin \tilde{\theta}_k \cos(\tilde{\phi}_k - \varphi_1) - \frac{d_2 - d_1}{R_1} \cos \tilde{\theta}_k)}{\lambda} \\ \vdots \\ \frac{2\pi R_1 (\sin \tilde{\theta}_k \cos(\tilde{\phi}_k - \varphi_{\frac{N}{2}}) - \frac{d_2 - d_1}{R_1} \cos \tilde{\theta}_k)}{\lambda} \end{bmatrix} \quad (18)$$

The space steering vector estimates of lower circular ring is given:

$$\hat{\mathbf{q}}_d(\hat{\theta}_k, \hat{\phi}_k) = \frac{\hat{\mathbf{A}}_1(\frac{N}{2} + 2 : N + 1, k)}{\hat{\mathbf{A}}_1(1, k)} = \frac{\hat{\mathbf{A}}_2(\frac{N}{2} + 2 : N + 1, k)}{\hat{\mathbf{A}}_2(1, k)} = \begin{bmatrix} e^{j \frac{2\pi R_2 (\sin \hat{\theta}_k \cos(\hat{\phi}_k - \varphi_1) - \frac{d_2}{R_2} \cos \hat{\theta}_k)}{\lambda}} \\ \vdots \\ e^{j \frac{2\pi R_2 (\sin \hat{\theta}_k \cos(\hat{\phi}_k - \varphi_{\frac{N}{2}}) - \frac{d_2}{R_2} \cos \hat{\theta}_k)}{\lambda}} \end{bmatrix} \quad (19)$$

According to Φ_1 , the rough phase estimation of $\hat{\mathbf{q}}_d(\hat{\theta}_k, \hat{\phi}_k)$ is got:

$$\Phi_2 = \Phi_1 \frac{l_2}{l_1} \quad (20)$$

The phase ambiguity number vector meets:

$$\mathbf{m}(n, k) = \argmin \left\{ \arg(\hat{\mathbf{q}}_d(\hat{\theta}_k, \hat{\phi}_k)) + 2\pi \mathbf{m}(n, k) - \Phi_2 \right\} \quad (21)$$

From the value $\mathbf{m}(n, k)$ in (21), the accurate phase vector estimation of $\hat{\mathbf{q}}_d(\hat{\theta}_k, \hat{\phi}_k)$ is obtained:

$$\mathbf{D} = \arg \left(\hat{\mathbf{q}}_d(\hat{\theta}_k, \hat{\phi}_k) \right) + 2\pi \mathbf{m}(n, k) \quad (22)$$

From Formulas (19) and (22), the accurate estimation of Poynting vector is achieved:

$$\hat{\mathbf{P}}_k(\hat{\theta}_k, \hat{\phi}_k) = \begin{bmatrix} \sin \hat{\theta}_k \cos \hat{\phi}_k \\ \sin \hat{\theta}_k \sin \hat{\phi}_k \\ \cos \hat{\theta}_k \end{bmatrix} = \mathbf{C}^{\#} \mathbf{D} \quad (23)$$

where $\mathbf{C}$ is a matrix varying with elements' position of lower circular ring, with

$$\mathbf{C} = \frac{2\pi R_2}{\lambda} \begin{bmatrix} 1 & 0 & -\delta \frac{d_2}{R_2} \\ \cos \left(\frac{4\pi}{N} \right) & \sin \left(\frac{4\pi}{N} \right) & -\frac{d_2}{R_2} \\ \vdots & \vdots & \vdots \\ \cos \left(\frac{4\pi}{N} \left(\frac{N}{2} - 1 \right) \right) & \sin \left(\frac{4\pi}{N} \left(\frac{N}{2} - 1 \right) \right) & -\frac{d_2}{R_2} \end{bmatrix} \quad (24)$$

From Formula (23), the accurate estimates are given:

$$\hat{\theta}_k = \arccos \left(\left[\hat{\mathbf{P}}_k(\hat{\theta}_k, \hat{\phi}_k) \right]_3 \right) \quad (25)$$

$$\begin{cases} \hat{\phi}_k = \arctan \left(\frac{\left[\hat{\mathbf{P}}_k(\hat{\theta}_k, \hat{\phi}_k) \right]_2}{\left[\hat{\mathbf{P}}_k(\hat{\theta}_k, \hat{\phi}_k) \right]_1} \right), & \left[\hat{\mathbf{P}}_k(\hat{\theta}_k, \hat{\phi}_k) \right]_1 \geq 0 \\ \hat{\phi}_k = \pi + \arctan \left(\frac{\left[\hat{\mathbf{P}}_k(\hat{\theta}_k, \hat{\phi}_k) \right]_2}{\left[\hat{\mathbf{P}}_k(\hat{\theta}_k, \hat{\phi}_k) \right]_1} \right), & \left[\hat{\mathbf{P}}_k(\hat{\theta}_k, \hat{\phi}_k) \right]_1 < 0 \end{cases} \quad (26)$$

where $[\cdot]_i$ ($i = 1, 2, 3$) refers to the i th element in the bracketed vector. The formula involves factor $\cos \theta$, which does not introduce an ambiguity in θ , because the θ in the upper hemisphere and the θ in the lower hemisphere give different $\cos \theta$.

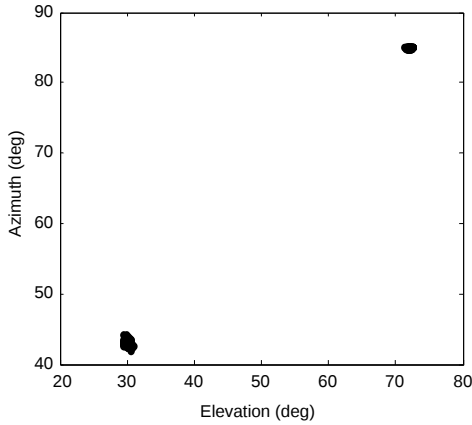


Figure 2. DOA scatter diagram using UCA method.

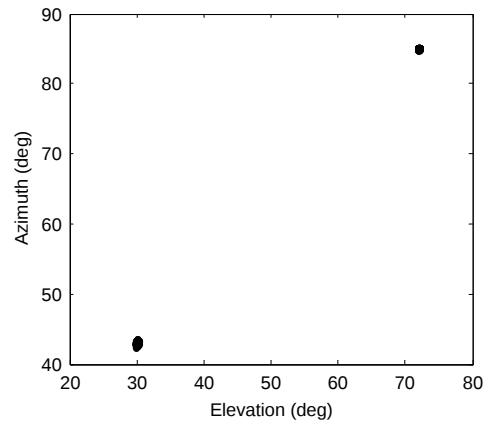


Figure 3. DOA scatter diagram using CCCP method.

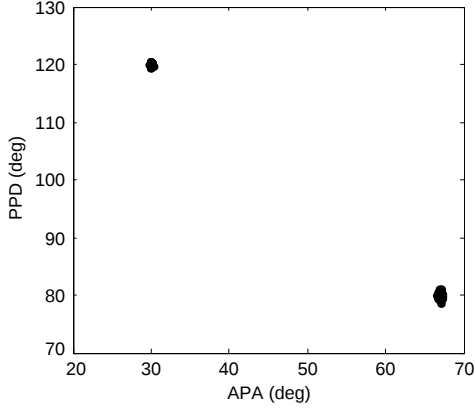


Figure 4. Polarization scatter diagram with UCA method.

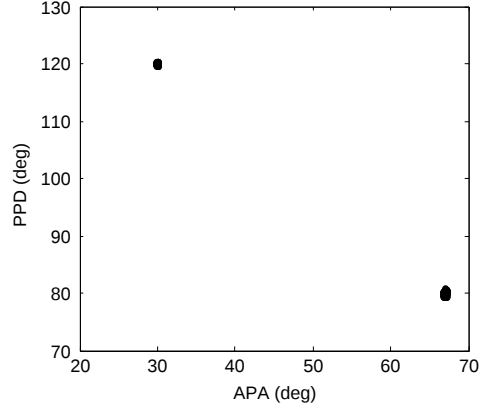


Figure 5. Polarization scatter diagram with CCCP method.

3. NUMERICAL EXAMPLES

To test the effectiveness of the proposed method, the following condition is considered. Two high-frequency incoherent sources impinge respectively on three arrays, viz., UCCA, CCCP and UCA, and there are 16 sensors on each circular ring of the three arrays above mentioned. UCCA has the same radius as CCCP whose inner circular ring radius $R_1 = 0.3\lambda$ and outer circular ring radius $R_2 = 1.5\lambda$. UCA with radius $R = 0.3\lambda$. Two incident signals are taken to have bearing parameters: $[\theta_1, \phi_1] = [30^\circ, 43^\circ]$, $[\gamma_1, \eta_1] = [67^\circ, 80^\circ]$, $[\theta_2, \phi_2] = [72^\circ, 85^\circ]$, $[\gamma_2, \eta_2] = [30^\circ, 120^\circ]$, 512 snapshots per experiment, 100 independent experiments per data point.

In the first experiment, we consider a scenario with 100 independent Monte Carlo trials running on the corresponding CCCP array. The signal-to-noise ratio (SNR) is set to 10 dB. The sets of values of the DOA and polarization variables have been represented in scatter diagrams (Figures 2–5).

From Figure 3, it is shown that almost all estimated values are located in the vicinity of actual values $[\theta_1, \phi_1] = [30^\circ, 43^\circ]$ and $[\theta_2, \phi_2] = [72^\circ, 85^\circ]$ by using CCCP method. The estimated values of $[\hat{\theta}_1, \hat{\phi}_1]$ are in the numerical range $(29.8^\circ, 30.2^\circ)$ and $(42.7^\circ, 43.3^\circ)$. On the contrary, from Figure 2, the estimated values $[\hat{\theta}_1, \hat{\phi}_1]$ using UCA method are distributed in the range of $(29.3^\circ, 30.9^\circ)$ and $(42.2^\circ, 44.2^\circ)$. The estimated error using UCA method is much larger than that of CCCP method.

From Figure 5, it is shown that almost all estimated values are located in the vicinity of actual values $[\gamma_1, \eta_1] = [67^\circ, 80^\circ]$ and $[\gamma_2, \eta_2] = [30^\circ, 120^\circ]$ by using CCCP method. The estimated values of $\hat{\gamma}_2$ and $\hat{\eta}_2$ are in the numerical range $(29.9^\circ, 30.1^\circ)$ and $(119.9^\circ, 120.2^\circ)$, respectively. On the contrary, from Figure 4, the estimated values are distributed in the range of $\hat{\gamma}_2$ $(29.8^\circ, 30.2^\circ)$ and $\hat{\eta}_2$ $(119.4^\circ, 120.6^\circ)$. The estimated error using UCA method is larger than that of CCCP method.

In the second experiment, we compare the performance of CCCP method to UCA method and UCCA method with respect to SNR. The comparison of CRLB and the above algorithms are also given. In the simulations, the SNR is from -6 to 20 dB, and 512 snapshots are used in each of the 100 independent Monte Carlo simulation experiments. The performance of standard deviation is illustrated, and the corresponding results are shown in Figures 6–9.

The solid curves with star, triangle, circular and diamond data points in Figures 6–9 respectively plot the DOA and polarization angles' estimation standard deviation, respectively estimated by the proposed UCA, UCCA, CCCP and CRLB method, at various signal-to-noise ratio (SNR) levels. It is obviously indicated that our proposed method can work well. The performance of the proposed CCCP method is close to that of the CRLB. The proposed CCCP procedure is better than UCA and nearly the same as UCCA. Moreover, CCCP estimating elevation angle by $\cos \theta$ does not introduce ambiguity in θ , but UCCA estimating elevation angle by $\sin \theta$ may introduce ambiguity in θ because the θ in the upper hemisphere and the θ in the lower hemisphere give the same $\sin \theta$. The estimation precision at -6 dB based on the CCCP model has improved larger than 0.35° for azimuth angle, 0.8° for elevation

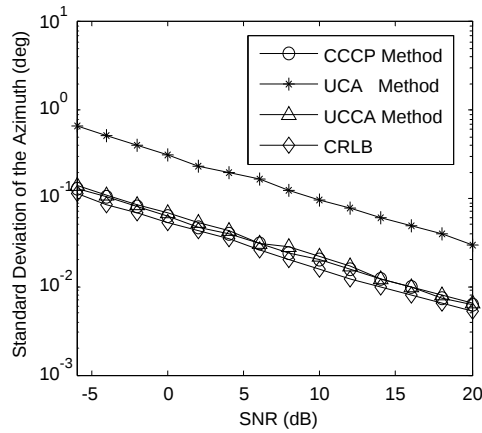


Figure 6. Standard deviation of the azimuth versus SNR.

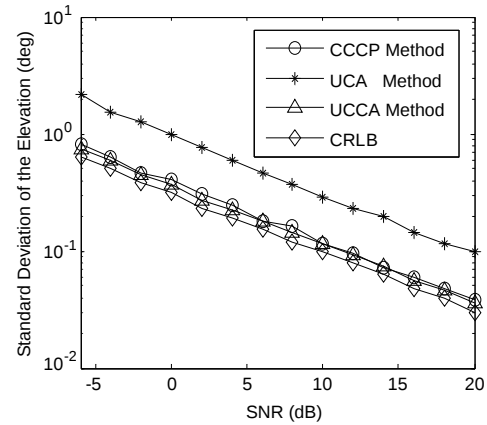


Figure 7. Standard deviation of the elevation versus SNR.

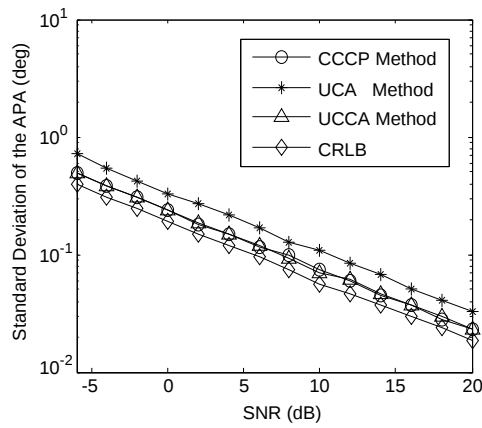


Figure 8. Standard deviation of the APA versus SNR.

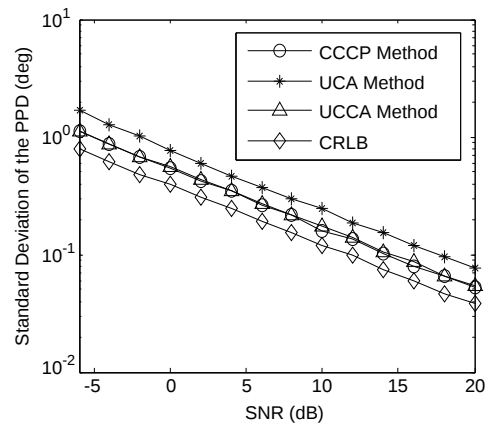


Figure 9. Standard deviation of the PPD versus SNR.

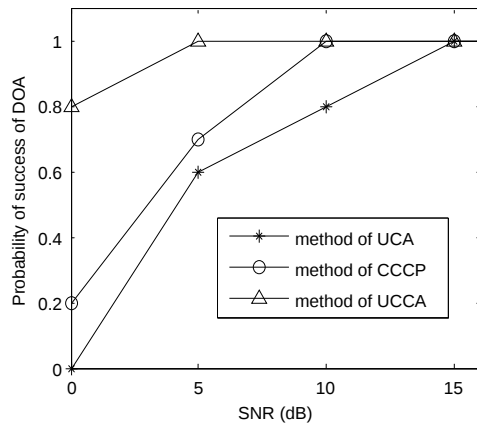


Figure 10. Probability of success of DOA versus SNR.

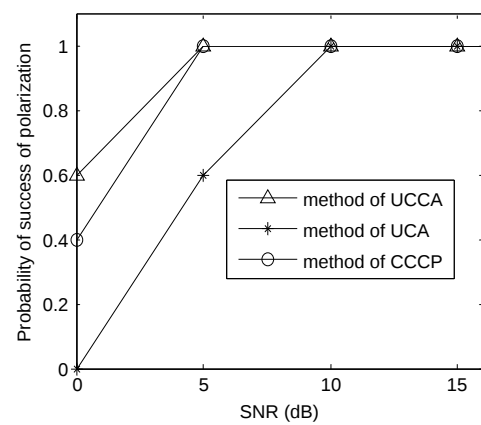


Figure 11. Probability of success of polarization versus SNR.

angle, 0.2° for auxiliary polarization angle (APA), 0.5° for polarization phase difference (PPD) angle, compared with that of the UCA method. The enhanced performance is rooted in the sparse embattle of CCCP. When there is no elevation quadrant ambiguity, UCCA can achieve nearly the same estimation precision as CCCP.

In the last experiment, we consider the probability of success of DOA and polarization estimations. Here we keep the settings unchanged and set the relationship $\sqrt{(\theta - \hat{\theta})^2 + (\phi - \hat{\phi})^2} < 1^\circ$ to be the successful DOA experiment, where θ and ϕ denote the true DOA value and $\hat{\theta}$ and $\hat{\phi}$ represent the corresponding estimated value. The definition of the successful polarization experiment is the same as that of the successful DOA experiment. The result is shown in Figures 10–11.

The curves with star and circular data points in Figures 10–11 respectively plot the probability of success of DOA and polarization, respectively estimated by the UCA, UCCA and the proposed CCCP method, at various signal-to-noise ratio (SNR) levels. The proposed CCCP procedure is better and more robust than the UCA and nearly the same as UCCA procedure.

4. CONCLUSION

A new DOA and polarization estimation method based on CCCP array is proposed, which overcomes the weakness of phase ambiguity of sparse array according to short and long baselines theory. Poynting vector is obtained by the least square method, so the proposed CCCP method overcomes quadrant ambiguity in elevation angle when conical conformal array is used for wide range elevation angle (more than 90 degrees) estimation. In contrast to UCCA, CCCP does not increase computation but eliminates elevation angle quadrant ambiguity and shows better performance than UCA. CCCP has broad application prospects in airborne, missile-borne and other aerospacecrafts.

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