# The Response of Layered Materials to EMG Waves from a Pulse Source

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Abstract—The authors present an analysis of conditions on the boundary between layers having varied electromagnetic properties. The research is performed using consistent theoretical derivation of analytical formulas, and the underlying problem is considered also in view of multiple boundaries including the effect of the propagation of electromagnetic waves with different instantaneous speeds. The paper comprises a theoretical analysis and references to the generated algorithms. The algorithms were assembled to enable simple evaluation of all components of the electromagnetic field in relation to the wave propagation speed in a heterogeneous environment. The proposed algorithms are compared by means of different numerical methods for the modelling of electromagnetic waves on the boundary between materials; moreover, the electromagnetic field components in common points of the model were also subject to comparison. When in conjunction with tools facilitating the analysis of material response to the source of a continuous signal, the algorithms constitute a supplementary instrument for the design of a layered material. Such design allows us to realize, for example, a recoilless plane, recoilless transition between different types of environment, and filters for both optical and radio frequencies.

#### 1. INTRODUCTION

Inhomogeneities and regions with different parameters generally appear even in the cleanest materials. During the passage of an electromagnetic wave through a material, we can observe an amplitude decrease and wave phase shift. These phenomena are due to material characteristics, such as conductivity, permittivity, or permeability [1]. If a wave impinges on an inhomogeneity, there occurs a change in its propagation. The change manifests itself in two forms, namely in reflection and refraction. In addition to this process, polarisation and interference may appear in these waves [1–5].

In the Matlab program, algorithms were created that simulate reflection and refraction in a lossy environment on the boundary between two dielectrics. The propagation of the waves is in accordance with Snell's law for electromagnetic waves. This law can be applied in a wide range of cases, starting from the optical principles of reflection and refraction and ending with, for example, the complex phenomena of the interference and propagation of waves. Referring to Snell's law, the reflection and refraction of electromagnetic waves is presented in Figure 1(a) and can be written as shown in [1]:

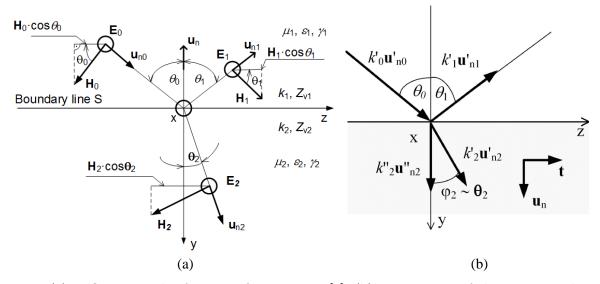
$$\frac{\sin\theta_0}{\sin\theta_2} = \frac{k_2}{k_1} = \frac{\sqrt{j\omega\mu_2 \cdot (\gamma_2 + j\omega\varepsilon_2)}}{\sqrt{j\omega\mu_1 \cdot (\gamma_1 + j\omega\varepsilon_1)}},\tag{1}$$

where k is the wave number,  $\gamma$  the conductivity,  $\varepsilon$  the permittivity,  $\mu$  the permeability,  $\theta_0$  the angle of incidence, and  $\theta_2$  the angle of refraction. The interpretation of the Fresnel equations and Snell's laws is simple in the case of refraction on the boundary line between dielectrics. In the case of refraction in a lossy medium, the angle  $\theta_2$  depends on the wave numbers  $k_1$  and  $k_2$ , which are generally complex.

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**Figure 1.** (a) Reflection and refraction of a TE wave [1]; (b) propagation of the constant phase and amplitude.

Thus, according to Formula (1), the angle  $\theta_2$  lies within complex numbers. Although this condition may appear uncommon, it is physically interpretable. In a lossy medium, planes of constant amplitude and phase propagate in different directions, and the transmission wave is not a plane wave.

The real part of the complex vector k describes the distribution of a wave in space, and simultaneously, it is perpendicular to the constant phase plane. The imaginary part of the same vector k then describes the damping of the wave and is perpendicular to the constant amplitude plane. If both the components of the complex vector k are parallel, the wave is classified as homogeneous; we denote it as inhomogeneous in all other cases.

Snell's law (1) can be expressed in components [6]. The real component of the wave number  $k' \mathbf{u}'_{ni}$  forms the angle  $\varphi$  with the vector  $\mathbf{u}_n$ , and the imaginary component of the wave number  $k'' \mathbf{u}''_{ni}$  makes the angle  $\Phi$  with the same vector  $\mathbf{u}_n$ . If the boundary conditions and the generalised Snell's law (1) are valid, we also have

$$k \mathbf{u}_{ni} = k' (\mathbf{u}_n \cdot \cos \varphi + \mathbf{t} \cdot \sin \varphi) + i \, k'' \left( \mathbf{u}_n \cdot \cos \psi + \mathbf{t} \cdot \sin \psi \right).$$
(2)

After modification, we obtain the formula

$$k \mathbf{u}_{ni} = \mathbf{u}_n \left( k' \cdot \cos \varphi + i \, k'' \cdot \cos \upsilon \right) + \mathbf{t} \left( k' \cdot \sin \varphi + i \, k'' \cdot \sin \upsilon \right), \tag{3}$$

which gives

$$\left(k'_0 \cdot \sin \varphi_0 + i \, k''_0 \cdot \sin \upsilon_0\right) = \left(k'_2 \cdot \sin \varphi_2 + i \, k''_2 \cdot \sin \upsilon_2\right). \tag{4}$$

According to Equation (4), the itemised Snell's law in real variables is expressed as

$$k_1'\sin\varphi_1 = k_2'\sin\varphi_2\tag{5}$$

$$k_1'' \sin v_1 = k_2'' \sin v_2, \tag{6}$$

where  $k'_2$  is the real component, forming the angle  $\varphi_2$  with the perpendicular line at the boundary, and  $k''_2$  is the imaginary component, making the angle  $v_2$  with the perpendicular line at the boundary. It follows from the formulas that v = 0 or  $v = \pi$ , as is obvious from Figure 1(b).

An electromagnetic wave exhibits an electric and a magnetic field intensity. The electric and magnetic components of the incident wave according to Figure 1(a) follow from the related formula specified in [1]:

$$\mathbf{E}_{i} = \mathbf{E}_{0} e^{-jk_{1}\mathbf{u}_{n0}\cdot\mathbf{r}}, \quad \mathbf{H}_{i} = \frac{\mathbf{u}_{n0} \times \mathbf{E}_{i}}{Z_{v1}}, \tag{7}$$

where  $\mathbf{E}_0$  is the amplitude of the electric field intensity on the boundary line,  $\mathbf{r}$  is the positional vector, and  $\mathbf{u}_{n0}$  is the unit vector of the propagation direction.  $Z_v$  is wave impedance:

$$Z_v = \sqrt{\frac{j\omega\mu}{(\gamma + j\omega\varepsilon)}}.$$
(8)

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For simplicity, we will analyze separately the  $\mathbf{E}$  vector parallel to the boundary (the TE wave) as indicated in Figure 1(a) and the magnetic field intensity  $\mathbf{H}$  vector parallel to the interface (the TM wave).

For the TE wave, the electric field intensity of the reflection and refraction beams is expressed according to the formula

$$\mathbf{E}_r = \mathbf{E}_1 e^{-jk_1 \mathbf{u}_{n1} \times \mathbf{r}}, \quad \mathbf{E}_t = \mathbf{E}_2 e^{-jk_2 \mathbf{u}_{n2} \times \mathbf{r}}, \tag{9}$$

where  $\mathbf{E}_1$  is calculated from the intensity on the boundary line  $\mathbf{E}_0$  and the reflection coefficient  $\rho_E$ , and  $\mathbf{E}_2$  is calculated from the intensity on the boundary line  $\mathbf{E}_0$  and the transmission factor  $\tau_E$ :

$$\mathbf{E}_1 = \rho_E \cdot \mathbf{E}_0, \quad \mathbf{E}_2 = \tau_E \cdot \mathbf{E}_0. \tag{10}$$

The magnetic component is obtained from the component of the electrical and wave impedance:

$$H_0 = \frac{E_0}{Z_{v1}}, \quad H_1 = \frac{E_1}{Z_{v1}}, \quad H_2 = \frac{E_2}{Z_{v2}}.$$
 (11)

The calculation of the reflection coefficient  $\rho_E$  and the transmission factor  $\tau_E$  is performed, via utilising the wave impedance  $Z_v$ , as follows:

$$\rho_E = \frac{\mathbf{E}_1}{\mathbf{E}_0} = \frac{Z_{v2}\cos\theta_1 - Z_{v1}\cos\theta_2}{Z_{v2}\cos\theta_1 + Z_{v1}\cos\theta_2}, \quad \tau_E = \frac{\mathbf{E}_2}{\mathbf{E}_0} = \frac{2Z_{v2}\cos\theta_1}{Z_{v2}\cos\theta_1 + Z_{v1}\cos\theta_2}.$$
 (12)

For a more suitable analysis of the dependence of the reflected and refracted waves on the parameters of the medium, we can advantageously use the formula

$$\mathbf{E}_{r} = \frac{\mu_{2}k_{1}\cos\theta_{0} - \mu_{1}\sqrt{k_{2}^{2} - k_{1}^{2}\sin^{2}\theta_{0}}}{\mu_{2}k_{1}\cos\theta_{0} + \mu_{1}\sqrt{k_{2}^{2} - k_{1}^{2}\sin^{2}\theta_{0}}} \mathbf{E}_{0} \cdot e^{-jk_{1}\mathbf{u}_{n1}\times\mathbf{r}},$$

$$\mathbf{E}_{t} = \frac{2\mu_{2}k_{1}\cos\theta_{0}}{\mu_{2}k_{1}\cos\theta_{0} + \mu_{1}\sqrt{k_{2}^{2} - k_{1}^{2}\sin^{2}\theta_{0}}} \mathbf{E}_{0} \cdot e^{-jk_{2}\mathbf{u}_{n2}\times\mathbf{r}}.$$
(13)

The formulas to derive the magnetic component are usually written as

$$\mathbf{H}_{r} = \frac{\mathbf{u}_{n1} \times \mathbf{E}_{r}}{Z_{v1}}, \quad \mathbf{H}_{t} = \frac{\mathbf{u}_{n2} \times \mathbf{E}_{t}}{Z_{v2}}.$$
(14)

In some cases, it can be more effective to directly utilise the basic variables. Thus, if the Poynting vector is applied, we have the following formula:

$$\mathbf{H}_{r} = -\frac{\frac{\mu_{2}}{\mu_{1}}k_{1}\cos\theta_{0} - \sqrt{k_{2}^{2} - k_{1}^{2}\sin^{2}\theta_{0}}}{\mu_{2}\cos\theta_{0} + \frac{\mu_{1}}{k_{1}}\sqrt{k_{2}^{2} - k_{1}^{2}\sin^{2}\theta_{0}}} \frac{\mathbf{E}_{0}}{\omega} \cdot e^{-jk_{1}\,\mathbf{u}_{n1}\cdot\mathbf{r}},$$

$$\mathbf{H}_{t} = -\frac{2k_{2}\cos\theta_{0}}{\mu_{2}\cos\theta_{0} + \frac{\mu_{1}}{k_{1}}\sqrt{k_{2}^{2} - k_{1}^{2}\sin^{2}\theta_{0}}} \frac{\mathbf{E}_{0}}{\omega} \cdot e^{-jk_{2}\,\mathbf{u}_{n2}\cdot\mathbf{r}}.$$
(15)

#### 2. OBLIQUE WAVE INCIDENCE ON A LAYERED MEDIUM

For a layered heterogeneous medium [7], we derive the algorithm according to Figure 2(a). The reflection of the electric component of the electromagnetic field intensity on the first layer is solved via the equations

$$\mathbf{E}_{r0} = \mathbf{E}_{i0}\rho_{E0} \cdot e^{-jk_1\mathbf{u}_{nr0} \times \mathbf{r}_0}, \quad \mathbf{E}_{t0} = \mathbf{E}_{i0}\tau_{E0} \cdot e^{-jk_2\mathbf{u}_{nt0} \times \mathbf{r}_0}.$$
 (16)

The reflection and refraction of the electric component of the electromagnetic field intensity on an arbitrary layer is expressed as

$$\mathbf{E}_{rl} = \mathbf{E}_{il}\rho_{El} \cdot e^{-jk_{(l+1)}\,\mathbf{u}_{nrl}\times\mathbf{r}_l}, \quad \mathbf{E}_{tl} = \mathbf{E}_{il}\tau_{El} \cdot e^{-jk_{(l+1)}\,\mathbf{u}_{ntl}\times\mathbf{r}_l},\tag{17}$$

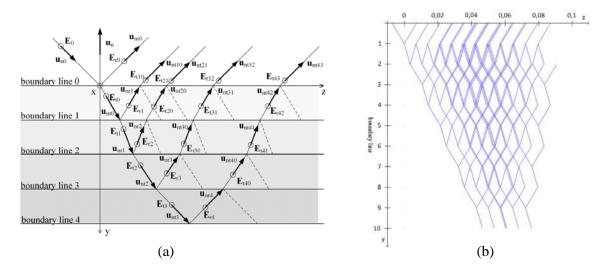


Figure 2. Reflection and refraction of the electric component of an electromagnetic wave on a layered medium: (a) layout; (b) Matlab for 2000 cycles.

where  $\mathbf{E}_{rl}$  a  $\mathbf{E}_{tl}$  are the reflected and refracted electromagnetic waves on the boundary line l (l = 1, ..., max) according to Figure 2(a),  $\mathbf{E}_{il}$  is the maximum value of the electric field intensity on the boundary line l,  $\rho_{El}$  and  $\tau_{El}$  are the reflection coefficient and transmission factor on the boundary line l,  $k_l$  is the wave number of the layer,  $\mathbf{r}_l$  is the wave incidence positional vector on the boundary line l, and  $\mathbf{u}_{ntl}$  and  $\mathbf{u}_{nrl}$  are the unit vectors of the propagation direction.

The magnetic component, or intensity of the magnetic field for the reflection on the first layer, leads to the formulas

$$\mathbf{H}_{r0} = -\mathbf{H}_{i0}\rho_{H0} \cdot e^{-jk_1\mathbf{u}_{nr0} \times \mathbf{r}_0}, \quad \mathbf{H}_{t0} = -\mathbf{H}_{i0}\tau_{H0} \cdot e^{-jk_2\mathbf{u}_{nt0} \times \mathbf{r}_0}.$$
 (18)

The reflection and refraction of the magnetic field intensity on several layers is expressed as

$$\mathbf{H}_{rl} = -\mathbf{H}_{il}\rho_{Hl} \cdot e^{-jk_{(l+1)}\mathbf{u}_{nrl} \times \mathbf{r}_l}, \quad \mathbf{H}_{tl} = -\mathbf{H}_{il}\tau_{Hl} \cdot e^{-jk_{(l+2)}\mathbf{u}_{ntl} \times \mathbf{r}_l}, \tag{19}$$

where  $\mathbf{H}_{rl}$  and  $\mathbf{H}_{tl}$  are the reflection and refraction magnetic components of the EMG wave at the boundary l. The other quantities are denoted similarly to Equation (17).

A Matlab-based analysis using Equations (1)–(19) was carried out to investigate the layered structure. An EMG wave having the frequency of 1.5 GHz impinges on the boundary of the material under the angle  $\theta_0$ , where it reflects and refracts. The wave passes through the material, which comprises ten layers of an identical thickness, namely d = 20 mm (Figure 3). The parameters of material 1 are as follows:  $\varepsilon_{r1} = 1$ ,  $\mu_{r1} = 1$ , and  $\gamma_1 = 1 \cdot 10^{-9} \text{ S/m}$ . The parameters corresponding to material 2 are  $\varepsilon_{r2} = 4$ ,  $\mu_{r2} = 0.999991$ , and  $\gamma_2 = 1 \cdot 10^{-9} \text{ S/m}$ . In the other layers, the material parameters vary regularly. The surrounding medium of the layered sample is defined by the parameters  $\varepsilon_{r0} = 1$ ,  $\mu_{r0} = 1$  and  $\gamma_0 = 1 \cdot 10^{-9} \text{ S/m}$ . During the solution and analysis of the FEM-based model, the high permittivity of a medium resulted in an unfavourable division of the discretised mesh elements with respect to the length of the propagating wave. Considering this fact, we then selected the material parameters; however, these are suitable only for testing purposes and cannot be practically applied. The geometry of the electromagnetic wave propagation inside the medium is represented via the proposed analysis as shown in Figure 2(b).

The evaluated result of the analysis of the described method consists in the modules of the electric field intensity **E** along the boundary between the first layer and the external environment. These values can be, to a certain extent, compared with the results obtained via already known methods, such as the finite element method (FEM) for the analysis of the electromagnetic field. The analysis of the response to the incidence of an electromagnetic wave upon the surface of a layered medium is presented in Figure 4, which shows the module of the electric field intensity **E** in relation to the path from the centre of the model to its edge. In the proposed graph, the thickness of the layers is changed to  $d = 100 \cdot \lambda$ ,

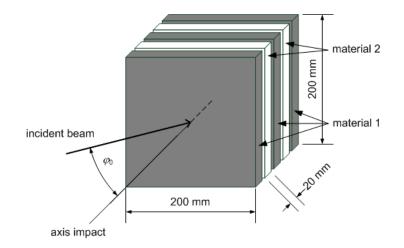
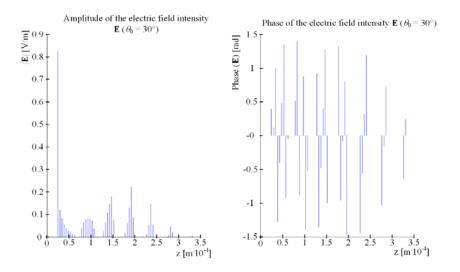


Figure 3. Geometrical model and dimensions of the wave incidence on a layered medium.



**Figure 4.** Oblique incidence on a layered medium for  $d = \lambda \cdot 100$  and t = T (f = 700 THz).

where  $\lambda$  represents the wavelength of the wave emitted by the source; this wave is generated as a single pulse, a single period. The distribution of the modules of the electric field intensity **E** on the surface of the material is obvious from the behaviour of the propagation of the electromagnetic waves inside the layered material indicated in Figure 1(b).

## 3. FEM-BASED MODEL OF A LAYERED MEDIUM

In order to verify the properties of the described analytical analysis, we performed an equivalent comparative evaluation based on the FEM; this analysis exhibited the same parameters as the previous model. As the mathematical expression, we applied the extended wave equation for a lossy environment:

$$\nabla^2 u + f \frac{\partial u}{\partial t} + g \frac{\partial^2 u}{\partial t^2} - f_c(x, y, z, t) = 0, \quad \forall g(x, y, z) \neq 0, \quad \forall f(x, y, z) \neq 0, \quad \text{in } \Omega,$$
(20)

where u is the sought functional, f is the electromagnetic wave damping function, g is the electromagnetic wave excitation function,  $f_c$  is the lossy environment function, and  $\Omega$  is the domain of the definition variables and functions. The distribution of the electric field intensity  $\mathbf{E}$  and its phase is shown in Figure 5. The characteristics in Figure 5 correspond to the axis direction perpendicular to the

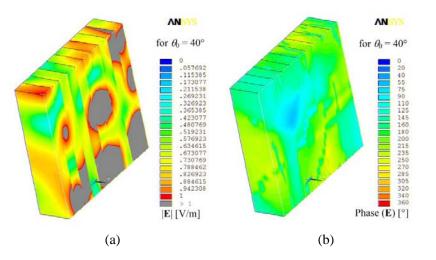


Figure 5. Distribution of the electric field intensity E: (a) the amplitude, and (b) the phase for  $\theta_0 = 40^{\circ}$ .

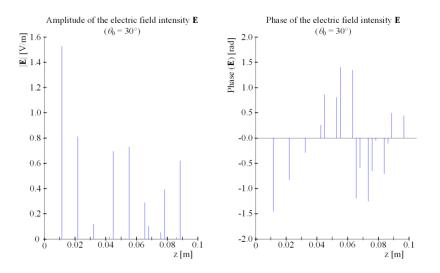


Figure 6. Intensity of the electric component of the TE wave on a layered medium at the angle  $\theta_0 = 30^{\circ}$ .

layer plane (Figure 3). The FEM-based solution in ANSYS limits the resulting values and manifests itself through the non-continuous distribution of values within the model.

## 4. COMPARISON OF THE MODEL RESULTS

Direct comparison of the results of the different analyses [9] obtained via the applied methods can be performed only with substantial difficulty. The results of the designed analytical parameters represent the waveform of the material response to the wave emitted by the pulse source, and changes of the maximum value of the electric field intensity are evaluated. The FEM is employed to represent the behaviour of the electric field intensity inside the examined layered medium; this pattern constitutes the response to the EMG waves from the continuous source.

For this reason, we designed algorithms to evaluate the selected time intervals in the ray-tracing model. The evaluation of the module of the electric field intensity  $\mathbf{E}$  on the surface of the material at these time intervals [10] is indicated in Figure 6.

For the approximation to the continuous function, we applied the Gaussian distribution [8]

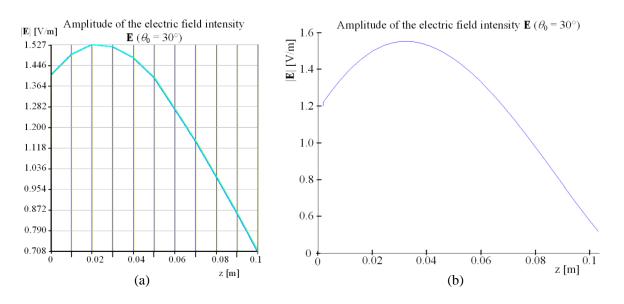


Figure 7. Distribution of the module of the electric field intensity  $\mathbf{E}$  for  $\theta_0 = 30^\circ$  in the plane of the wave incidence on the surface of the material: (a) the behaviour obtained from ANSYS; (b) the amplitude achievable with the designed algorithms.

according to the formula

$$f(x) = |\mathbf{E}| \frac{1}{\sigma\sqrt{2\pi}} e^{-\frac{(x-\Delta x)^2}{2\sigma^2}},$$
(21)

where  $\Delta x$  is the mean value of distribution,  $\sigma$  is the scattering parameter, and |E| is the module of the electric field intensity. The scattering parameter was selected to be  $\sigma = 1$ , and the mean value of distribution was set as  $\Delta x = 0$ . The Gaussian function merely approximates the ray tracingbased evaluation to the FEM, which comprises wave propagation. The radiation source generates a continuous electromagnetic wave. After approximating with the Gaussian function, we obtain the courses in Figure 7(b) from the patterns shown above (Figure 6). A suitably chosen time interval of the approximated response of the medium embodied in the discrete maximum values of the electromagnetic field intensity facilitates comparison with the evaluated continuous instantaneous values acquired via the FEM from Figure 7(a). The diagrams show that the results of the analyses are comparable; however, it is important to note that the module of the electric field intensity **E** evaluated from the ANSYS-based analyses is not represented in the range between 0 and the maximum.

The EMAG module of ANSYS is not applicable as a tool convenient for the evaluation of either the pulse process or the maximum values of an electromagnetic wave in a heterogeneous environment. This drawback stems from the fact that the module is characterised by multiple interferences and various wave propagation velocities, and therefore the behaviour of the phase of the electromagnetic field intensity is not uniform. Moreover, if the parameters described herein are set, the number of the discretisation mesh divisions in the ANSYS-based model will be unfavourable with respect to the wavelength of the propagating wave. For comparison purposes, however, this negative effect is still acceptable. Consequently, the resulting values (and thus also the comparison possibilities) are restricted.

#### 5. CONCLUSIONS

The article presents an analysis of wave propagation in a layered material structure. The authors utilise analytical Formula (1) based on Snell's law, and the analysis-related tasks are solved in the Matlab program. The underlying problem is processed for multiple boundaries, including the effect of the propagation of an electromagnetic wave at different instantaneous speeds. This approach is then compared with the analysis, whose solution is performed via the FEM applied to the wave equation. The FEM-based model was created using the ANSYS system.

It is obvious from the above-shown patterns that the designed algorithms are applicable to a large number of effects characterising the propagation of electromagnetic waves; simultaneously, the algorithms also enable us to define the parameters of both the wave sources and the environment through which the waves propagate. The verified methods facilitate the use of point, planar and pulse sources as well as those generating a continuous EMG wave. The response of the medium can be evaluated as a whole, and it is also possible to select certain points in the geometry or specific time instants. A limitation (but also an advantage for some cases) seems to consist in the possibility of representing the modules and phases instead of the instantanteous values. Principally, we can note that although algorithms based on ray tracing do not comprise the wave character of the propagation of an electromagnetic wave, they represent more illustratively the behaviour of a propagating wave in space and time. This fact may be beneficial for the quantitative approach to analysing the details of the model.

The main obstacle to direct comparison of the described approaches is the dissimilarity of the principles defining the individual analyses. Numerical modelling performed via the wave equation and ANSYS produces a continuous source of electromagnetic waves. Interference effects between the reflected and refracted waves arise on the boundary between the layers. Furthermore, the interference process is also accompanied by the time-delayed waves from the source and by interface reflections [11, 12]. Conversely, however, the designed analytical analysis does not comprise all types of interferences, and it evaluates several time-delayed responses to an EMG wave from the pulse source. The analytical solution and its algorithms process the time-varying phenomena of the pulsed source. This analytical solution includes the time-dependent propagation of electromagnetic waves in a heterogeneous medium and evaluates the distribution of the electromagnetic field on the surfaces of the boundaries at certain moments of time. A complex form of the angle of reflection and refraction is considered in the case of the analytical approach, which allows accurate determination of the size of the intensity of the reflected and refracted waves. In order to determine the direction of the constant phase propagation in a lossy medium, we consider only real parts of the wave number, which must be evaluated separately.

The results obtained from indirect comparison point to general agreement between the analyses. The FEM-based solution in ANSYS is restricted to the spatial distribution of the quantities with distributed parameters. This approach, despite being very robust in the time domain, appears to be inconvenient for the solution of multilayers due to the manner in which the mesh of elements is divided. In FEM-based numerical models, the number of divisions of the discretised mesh assuming the wavelength of the propagating wave can be determined only with difficulty, and a large model is almost unsolvable by common means. Importantly, this drawback is eliminable via the proposed method.

Advantageously, the presented analysis allows us to acquire an accurate solution of the response of an electromagnetic field to very short pulses and transient or continuous exciting electromagnetic sources. In connection with tools facilitating the analysis of the response of the material to a source of a continuous signal, the proposed algorithms constitute a supplementary instrument to enable the design of a layered medium.

The author has theoretically derived the analytical expressions to evaluate both the incidence of an EMG wave upon a boundary between layers with different electromagnetic properties and the behaviour of an electromagnetic wave on/in multilayered structures. The analytical relations have been applied in conjunction with ray-tracing. Finally, the derived formulas were compared with similar, commonly used numerical models.

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