

Controlling the Optical Bistability and Multistability via Atom Localization

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Abstract—We investigate optical bistability (OB) and optical multistability (OM) behaviors in a triply driven five-level atomic system. It is shown that the system has bistable behavior and can be controlled by intensity of applied fields. We find that OB switches to OM via interference induced among the Rabi-split resonance. We consider a superposed one-dimension standing wave, generated by two optical fields, and it is demonstrated that the OB and OM behaviors depend on the position of localized atoms as well as the relative phase of applied fields.

1. INTRODUCTION

Atomic coherence plays an important role in controlling the optical properties of the mediums because of its potential applications in optical physics. One interesting application is optical bistability (OB) which can be used in all optical switching and optical computing [1]. Optical bistable system exhibits two possible outputs for the same input intensity which are suitable for controlling the light by light. Different mechanisms have been used for preparing OB in various systems. One of these techniques is acousto-optical (AO) interaction which includes an optoelectronics feedback system [2, 3]. In this technique, OM and even chaos have been observed which are useful in the encryption/decryption blocks of a digital communication system [4]. The second mechanism is a simple Fabry-Perot resonator or ring cavity filled with a material whose refractive index is intensity-dependent [5]. Such bistable behavior is the result of nonlinearity of the atomic medium inside the cavity and feedback of the optical field from the cavity mirrors. In past three decades, optical transistors, all-optical switching and all-optical storage devices based on OB in two-level atomic systems have been extensively studied both experimentally and theoretically [1, 6, 7]. The OB in a three-level V -type atomic system in the presence of vacuum quantum interference has been investigated in multi-photon resonance condition [8, 9] and beyond it [10]. Moreover, the double dark resonance has been used for controlling the OB behavior in a four-level atomic system [11, 12]. Recently, we have reported phase-controlled OB via electromagnetically induced absorption in a four-level double V -type closed-loop system, and it was shown that OB switches to OM via applying a microwave field [13].

On the other hand, the optical properties of a triply driven five-level atomic system have been investigated, and the coherent control of narrow structures in absorption and dispersion was reported [14]. In this paper, we study the OB and OM behaviors of such a system, and it is shown that the OB behavior can be controlled by intensity of applied fields. In addition, it is demonstrated that by applying a microwave field to the system, OB switches to OM via interference induced among the Rabi-split resonance. Moreover, the effect of transverse standing cavity field on OB and OM in a unidirectional ring cavity is studied, and it is shown that the position of localized atom plays a major role in determining of the bistability and multistability behaviors of the system.

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2. MODEL AND EQUATIONS

We consider a triply driven five-level atomic system as shown in Fig. 1(a). In this scheme, the probe field is applied to the transition $|1\rangle\text{--}|3\rangle$ of frequency ω_{31} with frequency ω_p and amplitude \vec{E}_p . Two coherent coupling fields with frequency ω_1, ω_2 and amplitude \vec{E}_1, \vec{E}_2 are applied to the transitions $|2\rangle\text{--}|3\rangle$ of frequency ω_{32} and $|4\rangle\text{--}|5\rangle$ of frequency ω_{54} , respectively. All three laser beams can be generated by a single laser, using electro-optical modulators. The transition $|3\rangle\text{--}|5\rangle$ of frequency ω_{53} is excited by a microwave field with frequency ω_m and amplitude \vec{E}_m . The energy levels $|2\rangle$ and $|4\rangle$ are assumed purely metastable states. Such a system can be generated in D_1 transitions of cold ^{87}Rb atoms in a vapor cell. The lower levels are considered as $|1\rangle = 5S_{1/2}(F = 1, m_F = -1)$, $|2\rangle = 5S_{1/2}(F = 1, m_F = 1)$ and $|3\rangle = 5P_{1/2}(F = 2, m_F = 1)$. Upper levels are two hyperfine levels $|3\rangle = 5P_{1/2}(F = 1)$ and $|5\rangle = 5P_{1/2}(F = 2)$ separated by 816 MHz. Here F is the total atomic angular momentum quantum numbers. m_F stands for magnetic quantum number of corresponding state.

The Hamiltonian of the system in the interaction picture by using the rotating wave and dipole approximations are expressed by the following equation

$$H = -\hbar[(\Delta_p - \Delta_1)|2\rangle\langle 2| + \Delta_p|3\rangle\langle 3| + (\Delta_p + \Delta_m - \Delta_2)|4\rangle\langle 4| + (\Delta_p + \Delta_m)|5\rangle\langle 5| + (R_p|1\rangle\langle 3| + R_1|2\rangle\langle 3| + R_m|3\rangle\langle 5| + R_2|4\rangle\langle 5| + H \cdot C)] \quad (1)$$

In this equation, the detuning and Rabi frequency of applied fields are defined as

$$\Delta_1 = \omega_1 - \omega_{32}, \quad \Delta_2 = \omega_2 - \omega_{54}, \quad \Delta_m = \omega_m - \omega_{53}, \quad \Delta_p = \omega_p - \omega_{31}, \quad (2)$$

$$R_1 = \frac{\vec{\mu}_{23} \cdot \vec{E}_1}{2\hbar}, \quad R_2 = \frac{\vec{\mu}_{45} \cdot \vec{E}_2}{2\hbar}, \quad R_m = \frac{\vec{\mu}_{35} \cdot \vec{E}_m}{2\hbar}, \quad R_p = \frac{\vec{\mu}_{13} \cdot \vec{E}_p}{2\hbar}, \quad (3)$$

where $\vec{\mu}_{23}$, $\vec{\mu}_{45}$, $\vec{\mu}_{35}$ and $\vec{\mu}_{13}$ show the dipole moment of transitions $|2\rangle \rightarrow |3\rangle$, $|4\rangle \rightarrow |5\rangle$, $|1\rangle \rightarrow |3\rangle$ and $|3\rangle \rightarrow |5\rangle$ respectively.

The density matrix equations of motion are given by

$$\begin{aligned} \dot{\rho}_{11} &= iR_p(\rho_{31} - \rho_{13}) + \gamma_{31}\rho_{33}, \\ \dot{\rho}_{22} &= iR_1(\rho_{32} - \rho_{23}) + \gamma_{32}\rho_{33}, \\ \dot{\rho}_{33} &= iR_p(\rho_{13} - \rho_{31}) + iR_1(\rho_{23} - \rho_{32}) + iR_m(\rho_{53} - \rho_{35}) - (\gamma_{31} + \gamma_{32})\rho_{33} + \gamma_{53}\rho_{55}, \\ \dot{\rho}_{44} &= iR_2(\rho_{54} - \rho_{45}) + \gamma_{54}\rho_{55}, \\ \dot{\rho}_{55} &= iR_m(\rho_{35} - \rho_{53}) + iR_2(\rho_{45} - \rho_{54}) - (\gamma_{53} + \gamma_{54})\rho_{55}, \\ \dot{\rho}_{21} &= i(\Delta_p - \Delta_1)\rho_{21} + iR_1\rho_{31} - iR_p\rho_{23}, \\ \dot{\rho}_{31} &= -(\Gamma_{31} - i\Delta_p)\rho_{31} + iR_p(\rho_{11} - \rho_{33}) + iR_1\rho_{21} + iR_m\rho_{51}, \\ \dot{\rho}_{32} &= -(\Gamma_{32} - i\Delta_1)\rho_{32} + iR_1(\rho_{22} - \rho_{33}) + iR_p\rho_{12} + iR_m\rho_{52}, \\ \dot{\rho}_{41} &= i(\Delta_p + \Delta_m - \Delta_2)\rho_{41} + iR_2\rho_{51} - iR_p\rho_{43}, \\ \dot{\rho}_{42} &= i(\Delta_1 + \Delta_m - \Delta_2)\rho_{42} + iR_2\rho_{52} - iR_1\rho_{43}, \\ \dot{\rho}_{43} &= -(\Gamma_{43} - i(\Delta_m - \Delta_2))\rho_{43} - iR_p\rho_{41} - iR_1\rho_{42} - iR_m\rho_{45} + iR_2\rho_{53}, \\ \dot{\rho}_{51} &= -(\Gamma_{51} - i(\Delta_m + \Delta_p))\rho_{51} - iR_p\rho_{53} + iR_m\rho_{31} + iR_2\rho_{41}, \\ \dot{\rho}_{52} &= -(\Gamma_{52} - i(\Delta_m + \Delta_1))\rho_{52} - iR_1\rho_{53} + iR_m\rho_{32} + iR_2\rho_{42}, \\ \dot{\rho}_{53} &= -(\Gamma_{53} - i\Delta_m)\rho_{53} + iR_m(\rho_{33} - \rho_{55}) + iR_2\rho_{43} - iR_p\rho_{51} - iR_1\rho_{52}, \\ \dot{\rho}_{54} &= -(\Gamma_{54} - i\Delta_2)\rho_{54} + iR_2(\rho_{44} - \rho_{55}) + iR_m\rho_{34}, \end{aligned} \quad (4)$$

where $\Gamma_{31} = \Gamma_{32} = \Gamma_{43} = \frac{(\gamma_{31} + \gamma_{32})}{2}$, $\Gamma_{51} = \Gamma_{52} = \Gamma_{54} = \frac{(\gamma_{53} + \gamma_{54})}{2}$, $\Gamma_{53} = \frac{(\gamma_{31} + \gamma_{32} + \gamma_{53} + \gamma_{54})}{2}$ are the dephasing rates between corresponding levels. Parameter γ_{ij} denotes decay rate from level $|i\rangle$ to $|j\rangle$.

Now, we put the ensemble of N homogeneously broadened five-level atoms in a unidirectional ring cavity as shown in Fig. 1(b). The intensity reflection (\bar{R}) and transmission (\bar{T}) coefficients of mirror 1 and 2 are related to each other with $\bar{R} + \bar{T} = 1$. It is assumed that both the mirrors 3 and 4 are perfect reflectors. The probe field circulates in the ring cavity while other applied fields do not circulate in the cavity.

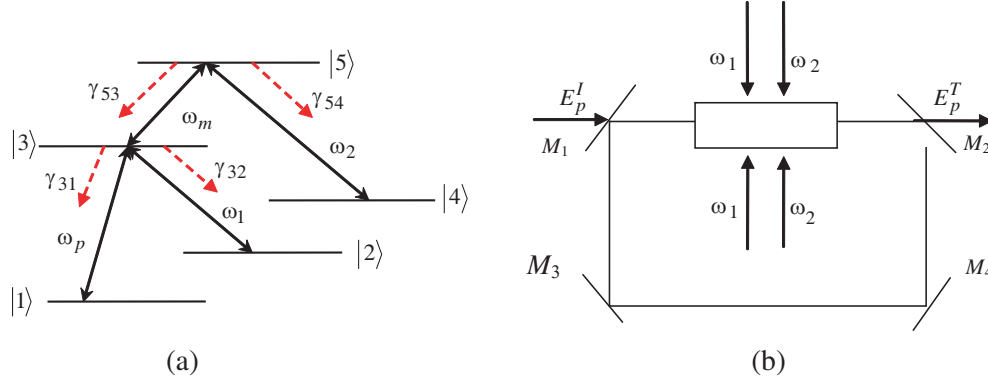


Figure 1. (a) Diagram of five-level atomic system which is driven by a probe field with frequency ω_p and three coherent coupling field with $\omega_i (i = 1, 2, m)$. The red arrows stand for decay rates. (b) Unidirectional ring cavity with atomic sample of length L . E_p^I and E_p^T are the incident and transmitted fields, while ω_1 and ω_2 are the central frequency of coupling fields. For mirrors 1 and 2 it is assumed that $\bar{R} + \bar{T} = 1$ and mirrors 3 and 4 have perfect reflectivity.

Now, we introduce the eigenvalues of dressed states established by the applied fields which have a key role in understanding of the optical properties of the system. For resonance condition, the atom-field eigenvalues can be written as

$$\begin{aligned}
 \Lambda_1 &= 0, \\
 \Lambda_2 &= -\frac{\sqrt{R_1^2 + R_2^2 + R_m^2 - \sqrt{R_1^4 - 2R_1^2(R_2^2 - R_m^2) + (R_2^2 + R_m^2)^2}}}{\sqrt{2}}, \\
 \Lambda_3 &= \frac{\sqrt{R_1^2 + R_2^2 + R_m^2 - \sqrt{R_1^4 - 2R_1^2(R_2^2 - R_m^2) + (R_2^2 + R_m^2)^2}}}{\sqrt{2}}, \\
 \Lambda_4 &= -\frac{\sqrt{R_1^2 + R_2^2 + R_m^2 + \sqrt{R_1^4 - 2R_1^2(R_2^2 - R_m^2) + (R_2^2 + R_m^2)^2}}}{\sqrt{2}}, \\
 \Lambda_5 &= \frac{\sqrt{R_1^2 + R_2^2 + R_m^2 + \sqrt{R_1^4 - 2R_1^2(R_2^2 - R_m^2) + (R_2^2 + R_m^2)^2}}}{\sqrt{2}}.
 \end{aligned} \tag{5}$$

For $R_1 = 0$ the eigenvalues are simplified to

$$\begin{aligned}
 \lambda_1 &= \lambda_2 = \lambda_3 = 0, \\
 \lambda_4 &= -\sqrt{R_2^2 + R_m^2}, \\
 \lambda_5 &= \sqrt{R_2^2 + R_m^2}.
 \end{aligned} \tag{6}$$

Note that in the presence of R_1 , only one zero eigenvalue is obtain and can establish a transparency window in absorption spectrum, accompanied by four peaks. By switching off R_1 , three zero eigenvalues are generated and can generate a sharp peak due to the interacting dark resonance.

Now, we are going to study the optical bistability behavior of the system by considering N such five-level atoms inside the unidirectional optical ring resonator depicted in Fig. 1(b). Then under slowly varying envelope approximation, the dynamic response of the probe field is governed by Maxwell's equation [15]

$$\frac{\partial E_p}{\partial t} + c \frac{\partial E_p}{\partial z} = i \frac{\omega_p}{2\varepsilon_0} P(\omega_p) \tag{7}$$

where c and ε_0 are the light speed and permittivity of free space, respectively. $P(\omega_p)$ is the induced polarization in the transition $|1\rangle$ - $|3\rangle$ and is given by $P(\omega_p) = N\mu_{31}\rho_{31}$.

According to the mean-field limit and using the boundary condition the input-output relationship is given by

$$y = 2x - iC\gamma_{31}\rho_{31}, \quad (8)$$

where $x = \mu_{31}E_p^T / \hbar\sqrt{T}$ and $y = \mu_{31}E_p^I / \hbar\sqrt{T}$ are the normalized output and input fields respectively. The parameter $C = LN\omega_P\mu_{31}^2 / 2\hbar c\varepsilon_0\gamma_{31}\bar{T}$ is the atomic coupling parameter in a ring cavity, and L stands for the length of the atomic sample.

3. RESULTS AND DISCUSSIONS

In this section, we discuss the numerical results for obtaining the optical properties of the system under various conditions. We assume $\gamma_{31} = \gamma_{32} = \gamma_{53} = \gamma_{54} = \gamma = 1$ and all parameters are scaled by γ . We choose a case with symmetric decay rates for reducing the number of parameters in our calculation, and this assumption is not critical for the appearance of the observed multistability in this system. First, we assume that the fields \vec{E}_1 and \vec{E}_2 are in the resonance condition. In Fig. 2, we show the absorption of the probe field versus probe field detuning for different values of Rabi frequency. The selected parameters are $R_m = 3\gamma$, $R_2 = 0.3\gamma$, $R_p = 0.01\gamma$, $\Delta_m = \Delta_1 = \Delta_2 = 0$, $R_1 = 0$ (solid) and $R_1 = 0.3\gamma$ (dashed). An investigation on Fig. 2 shows that the absorption of the probe field is affected by applying the field \vec{E}_1 to the system. An absorption peak due to the constructive interference in the three-photon process is appeared for $R_1 = 0$ at the $\Delta_p = 0$. This structure is explained according to the Equation (6). When field \vec{E}_1 is turned on, the sharp absorption peak splits into a closely spaced absorption doublet, and a central transparent window due to the four-photon resonance is established which is shown by dashed curve in Fig. 2. The results are in good agreement with Fig. 2 of [14]. Note that the position of four peaks can be determined by the four eigenvalues of the system, which have been introduced in Equation (5).

In Fig. 3, we show the OB behavior of the system in resonance condition in (a) absence and (b) presence of the field \vec{E}_1 for different values of the probe field detuning. Used parameters are $C = 200$, $\Delta_p = 0$ (solid), $\Delta_p = 0.025\gamma$ (dashed), $\Delta_p = 0.05\gamma$ (dash-dotted) for (a) $R_1 = 0$ and (b) $R_1 = 0.3\gamma$. Other parameters are the same as in Fig. 2. In Fig. 3(a), it is shown that increase of Δ_p leads to a decrease of the bistability threshold. We find that, in the presence of the field \vec{E}_1 , one can transit between bistability and multistability by adjusting the value of the probe field detuning. Moreover, our results show that the outer peaks in the absorption spectrum (Fig. 2) apply only OB behavior while the inner narrow peaks, due to the four-photon transitions, can induce OM behavior to the system.

Let us introduce another scenario for simple control of OB of the system. We are going to investigate the effect of atom localization due to the transverse standing wave on the OB behavior of the system.

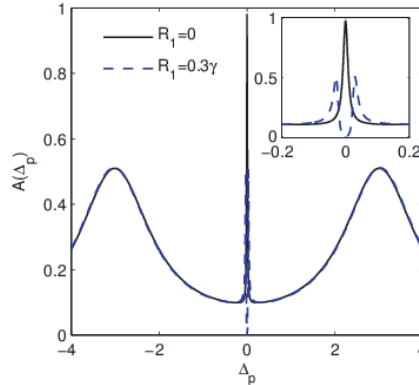


Figure 2. The absorption of the probe field versus the probe field detuning for different values of coupling Rabi frequency. The selected parameters are $R_m = 3\gamma$, $R_2 = 0.3\gamma$, $R_p = 0.01\gamma$, $\Delta_m = \Delta_1 = \Delta_2 = 0$, $R_1 = 0$ (solid) and $R_1 = 0.3\gamma$ (dashed).

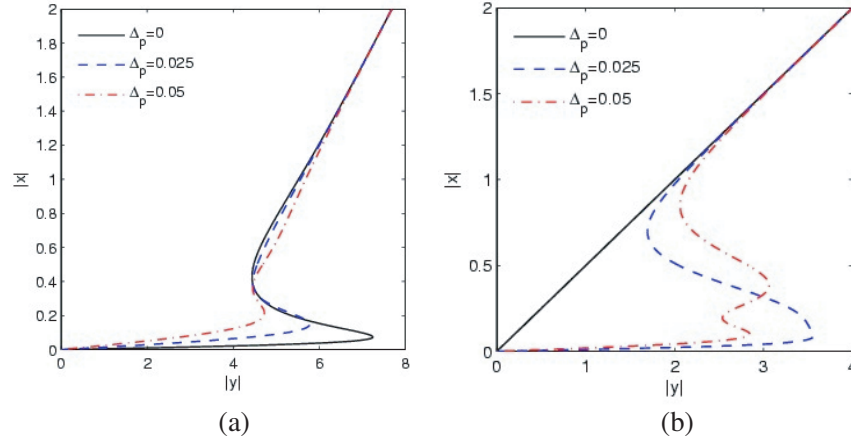


Figure 3. The normalized output field (x) versus input field (y) of the system in resonance condition in the (a) absence and (b) presence of the field \vec{E}_1 for different values of the probe field detuning. Used parameters are $C = 200$, $\Delta_p = 0$ (solid), $\Delta_p = 0.025\gamma$ (dashed), $\Delta_p = 0.05\gamma$ (dash-dotted) for (a) $R_1 = 0$ and (b) $R_1 = 0.3\gamma$. Other parameters are same as in Fig. 2.

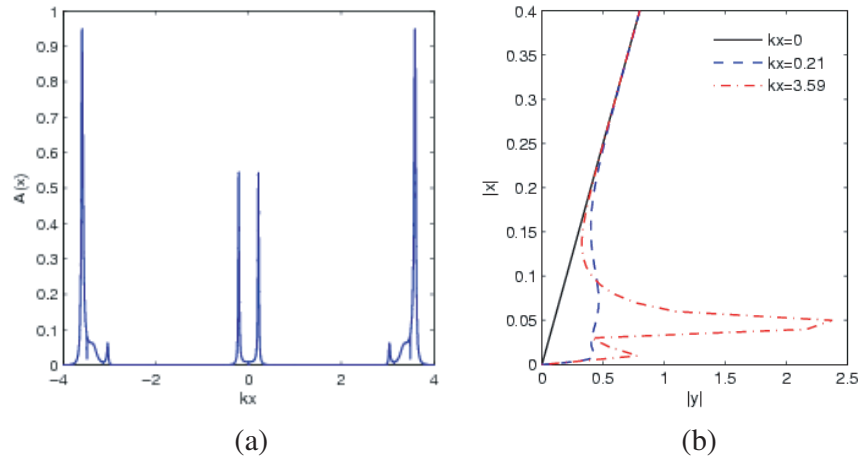


Figure 4. The position dependent absorption (a) $A(kx)$ and (b) the OB curve (x versus y) for different positions of localized atoms. Parameters used are, $R_1 = R_2 = 0.5\gamma$, $R_m = 10\gamma$, $\Delta_m = \Delta_1 = \Delta_2 = 0$, $\Delta_p = 0.001\gamma$, $k_1 = 0.9k$, $k_2 = k$, $\phi = 0$, (a) $R_p = 0.01\gamma$, (b) $C = 200$, $kx = 0$ (solid), 0.21 (dashed), 3.59 (dash-dotted).

The effect of the standing wave on the Fabry-Perot cavity has been investigated [16]. Moreover, atom localization of different systems via absorption spectrum has been studied [17, 18]. We choose the required spatial-field arrangement for \vec{E}_1 and \vec{E}_2 to establish the standing wave along the direction x , which is perpendicular to the probe propagation direction. Then, it is necessary to redefine the space dependent Rabi frequencies as $\Omega_1(x) = R_1 \sin(k_1 x + \phi)$ and $\Omega_2(x) = R_2 \sin(k_2 x)$, where k_i is the magnitude of wave vector of field \vec{E}_i , and ϕ stands for spatial phase shift of two fields. Therefore, the optical properties of the system depend on the transverse position of localized atoms, and then OB behavior can be controlled by position atoms, intensity and phase shift of standing wave.

In Fig. 4, we plot the position dependent absorption (a) $A(kx)$ and (b) the OB curve for different positions of localized atoms. Parameters used are $R_1 = R_2 = 0.5\gamma$, $R_m = 10\gamma$, $\Delta_p = 0.001\gamma$, $\Delta_m = \Delta_1 = \Delta_2 = 0$, $k_1 = 0.9k$, $k_2 = k$, $\phi = 0$, (a) $R_p = 0.01\gamma$, (b) $C = 200$, $kx = 0$ (solid), 0.21 (dashed), 3.59 (dash-dotted). The characteristic and location of absorption peaks depend on the Rabi frequency and detuning of applied fields [14]. It can be seen that for $kx = 0$ (solid), the system

does not show bistable behavior. The atoms located around $kx = 0.21$ show bistable behavior (dashed), while OM behavior is induced by atoms located around $kx = 3.59$ of standing wave (dash-dotted). Then OB and OM behaviors of the system can be controlled by simple shift of the standing wave cavity in x direction.

Now, we are interested in studying the effect of microwave field on OB behavior of the system. In Fig. 5, we plot OB behavior of the system for different values of microwave intensities. Parameters used are $C = 200$, $kx = 0.21$, $R_m = 4\gamma$ (solid), $R_m = 7\gamma$ (dashed), $R_m = 10\gamma$ (dash-dotted). Other parameters are the same as in Fig. 4(a). Fig. 5 shows that the threshold value and hysteresis cycle width of the bistable curve are reduced by increasing the microwave field intensity.

The effect of the intensity of the standing wave on the OB behavior of the system is shown in Fig. 6. We assume that the driving fields \vec{E}_1 , \vec{E}_2 and \vec{E}_m are exactly tuned to the corresponding transitions, and the phase-shift ϕ is set as zero. The input-output curve is plotted for different values of intensity of the driving fields. Used parameters are $kx = 0.21$, $R_1 = R_2 = R = 0.1\gamma$ (dotted), 0.5γ (dashed), 5 (solid). Other parameters are the same as in Fig. 4. We find that OB behavior can be induced to the system by increasing the intensity of standing waves. It is worth noting that the optical properties

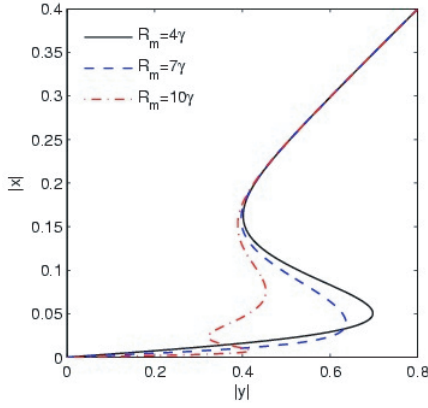


Figure 5. The OB behavior for different microwave field intensities. Parameters used are $kx = 0.21$, $R_m = 4$ (solid), $R_m = 7$ (dashed), $R_m = 10$ (dash-dotted). Other parameters are same as in Fig. 4.

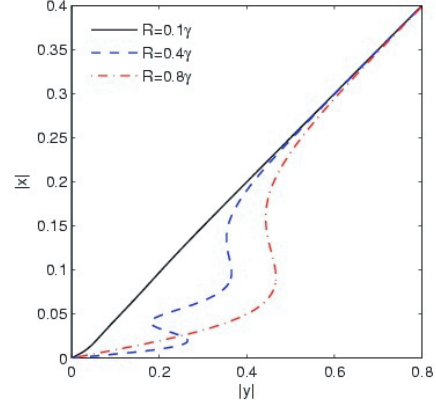


Figure 6. The input-output curve for different values of intensity of the driving standing fields. Used parameters are $kx = 0.21$, $R_1 = R_2 = R = 0.1\gamma$ (solid), 0.4γ (dashed), 0.8γ (dash-dotted). Other parameters are same as in Fig. 4.

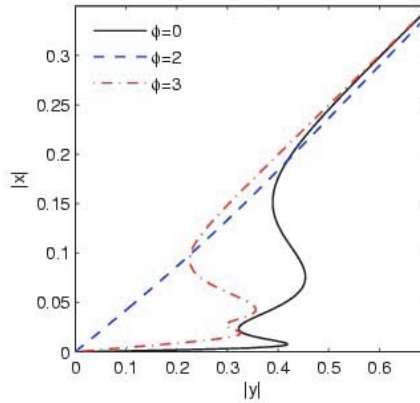


Figure 7. The input-output curve of the system for different values of phase-shift. Selected parameters are $R_1 = 0.1\gamma$, $R_2 = 0.5\gamma$, $R_m = 10\gamma$, $k_2 = k$, $k_1 = 0.9k$, $kx = 1.5$, $\phi = 0$ (solid), 2 (dashed), 3 (dash-dotted). Other parameters are same as in Fig. 5.

of the system depend also on the phase-shift of applied fields. The input-output curves of the system, for different values of phase-shift, are plotted in Fig. 7. Selected parameters are $R_1 = 0.1\gamma$, $R_2 = 0.5\gamma$, $R_m = 10\gamma$, $kx = 1.5$, $\phi = 0$ (solid), 2 (dashed), 3 (dash-dotted). Other parameters are the same as in Fig. 4. It is seen that OB of the system switches to OM just by changing the phase-shift of applied fields. The physical origin lies on the fact that the position of the absorption peaks depends on the phase shift between the two considered standing waves.

Finally, we are going to determine the stable and unstable branches in OM diagrams which are important in all-optical multistate switching or coding elements [19]. Fig. 8 shows the stable (solid) and unstable (dotted) branches in four different OM curves which are selected from Fig. 3(a), Fig. 5(b), Fig. 6(c) and Fig. 7(d). The input-output solutions show two S-type curves, which gives rise to the tristability in certain input intensity region. The jump up and jump down output intensities are shown by dashed arrows.

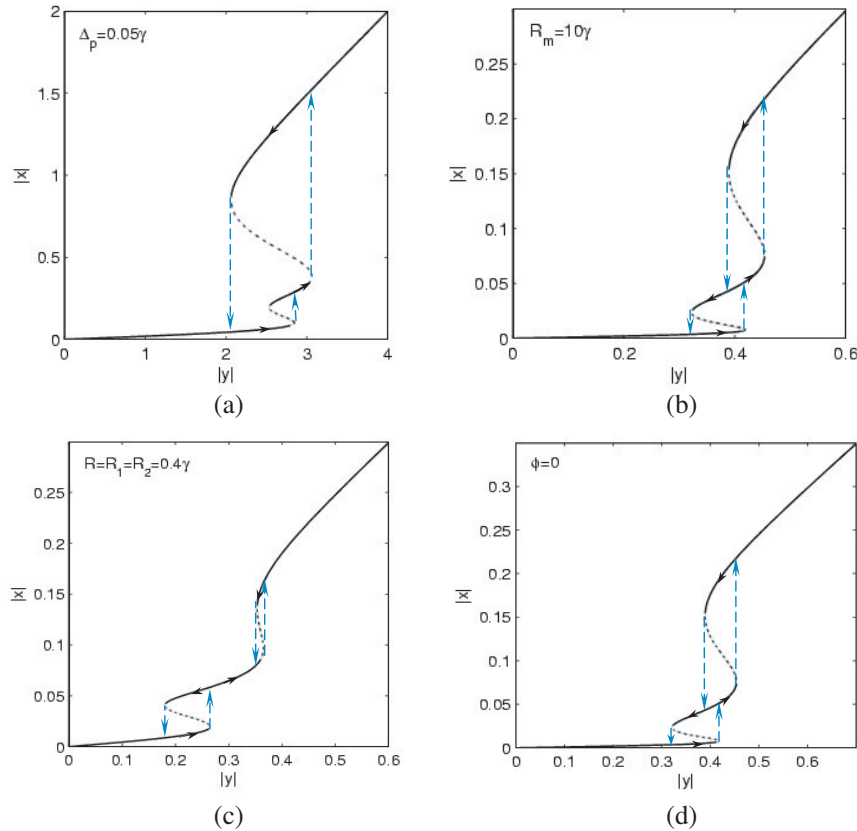


Figure 8. The stable (solid) and unstable (dotted) branches in four different OM curves which are selected from Fig. 3(a), Fig. 5(b), Fig. 6(c) and Fig. 7(d). The jump up and jump down output intensities are shown by dashed arrows.

4. CONCLUSION

In conclusion, we have investigated the OB and OM behaviors in a triply driven five-level atomic system. It was shown that the OB of such a system can be controlled by the characteristic parameters applied fields. We found that the narrow multi-photon absorption peaks, among the Rabi-split resonance induce OM behavior to the system. We have introduced a new scenario, to control OB and OM of the system via atom localization by applying a transverse superposed one dimension standing wave to the system. Then OB and OM can be controlled by simple fine shifting of the standing wave cavity and relative phase of standing waves. Such displacement can be generated by piezoelectric crystals with better than micrometer precision.

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