

## The Image Phase Approach for the Design of RF MEMS Shunt Switches

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**Abstract**—In this paper a new method to solve the microwave matching problem of MEMS shunt connected switches is proposed, as an extension of a previously presented approach based on the image parameter formulation. The image phase concept is used to impose the matching condition in the “ON” state of the device, which is the most critical one. Two different configurations are investigated: a single basic cell and double basic cell topologies. For both of them an analytic modeling procedure is developed, and the equations for the synthesis of the structures are derived. In order to provide some examples, the method has been applied to a previously realized MEMS shunt variable capacitor.

### 1. INTRODUCTION

RF MEMS coplanar waveguide (CPW) shunt connected capacitive switches are two state devices typically composed by a metal bridge which is actuated by means of a bias voltage [1–7]. The “UP” configuration of the bridge corresponds to the “ON” state whereas the “DOWN” configuration is associated to the “OFF” one. In order to have good electric performance the impedance matching in the “ON” state is required. In many cases due to technological reasons this result cannot be achieved with just a bridge. Two topologies have been proposed in literature to overcome this problem. The first one, shown in Figure 1, is obtained by adding two equal transmission lines, with suitable values of the characteristic impedance and of the electric length, to the CPW metallic membrane. Another possible structure is composed by two MEMS bridges spaced by a uniform transmission line. For both these two solutions analytic design procedures have been provided in [2, 4], modelling the MEMS device by a simple shunt connected capacitance. However in some cases a more general equivalent circuit should be used for the accurate characterization of the component. This issue has been dealt with in [8], where for the CPW flexible membrane a T-network has been adopted. In this paper, we present a novel method, based on the image parameter representation of two port networks, to improve the microwave matching in the synthesis of the transmission lines depicted in Figure 1. The basic idea was to impose the matching in the “ON” state of the switch by means of the image impedance but unfortunately, with this approach the physical feasibility of the transmission lines is ensured for a limited range of values of the T-network elements, as discussed in [8]. In order to solve this problem, in this contribution the matching condition is imposed by using the image phase.

It is worth noting that the image phase concept has been employed in the past for the design of distributed phase shifters and amplifiers [9–11]. The organization of this paper is as follows. Section 2 deals with the definition of the image parameters and their use to impose the matching condition on a lossless reciprocal and symmetrical two-port network. In Section 3 these results are applied for the development of an analytic model for the MEMS switch in the “ON” state. Section 4 gives a

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comparison with the design method based on the image impedance presented in [8]. Section 5 concerns the experimental characterization of a previously manufactured MEMS coplanar bridge, which is used in this work to provide design examples corresponding to actual devices. In Section 6 numerical results of circuital simulations are illustrated, and considerations on the switch optimization in terms of electric performance and size reduction are discussed. Finally, in Section 7, we summarize some conclusions.

## 2. THE IMAGE PARAMETER MATCHING CONDITION

For a reciprocal symmetrical lossless two-port network an image impedance  $Z_i$  and an image phase  $\phi_i$  can be defined as [12, 13]:

$$Z_i = \sqrt{\frac{B'}{C'}}, \quad (1)$$

$$\cos \phi_i + j \sin \phi_i = \sqrt{AD} + j\sqrt{B'C'} \quad (2)$$

being  $A, B, C, D$  the transmission matrix elements and  $A = D, B = jB', C = jC'$ .  $A, B'$  and  $C'$  are real numbers. According to [9, 11] the scattering parameter  $S_{11}$  of the network can be expressed as:

$$S_{11} = \frac{j \left( \frac{B'}{Z_0} - C'Z_0 \right)}{2A + j \left( \frac{B'}{Z_0} + C'Z_0 \right)} = \frac{j \left( \frac{Z_i}{Z_0} - \frac{Z_0}{Z_i} \right) \sin \phi_i}{2 \cos \phi_i + j \left( \frac{Z_i}{Z_0} + \frac{Z_0}{Z_i} \right) \sin \phi_i} \quad (3)$$

Thus the matching condition  $S_{11} = 0$  can be fulfilled imposing:

$$Z_i = Z_0 \quad (4)$$

or

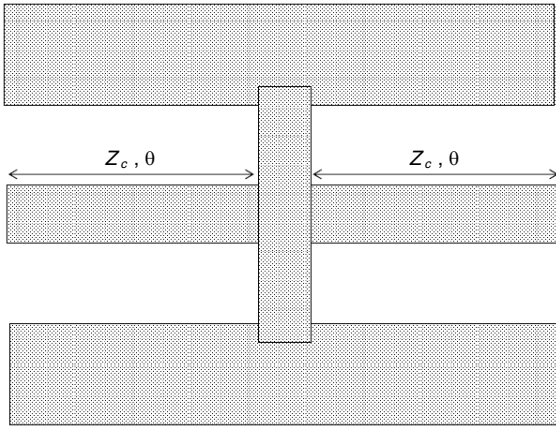
$$\phi_i = k\pi \quad (5)$$

with  $k = 1, 2, 3, \dots$

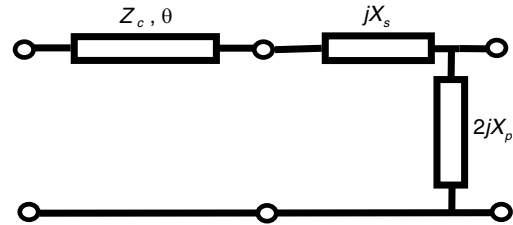
It can be easily demonstrated that Equation (5) is equivalent to the following condition:

$$B' = C' = 0 \quad (6)$$

A comparison between the use of Equation (5) or Equation (6) will be discussed in another section of this paper.



**Figure 1.** The basic cell composed by the MEMS coplanar bridge and two equal uniform transmission lines.



**Figure 2.** The basic half-cell circuital model obtained replacing the coplanar MEMS bridge by a lossless reciprocal and symmetrical T-network.

### 3. THE ANALYTIC MODEL WITH THE BRIDGE IN THE “UP” POSITION

As discussed in the introduction, the most critical configuration for the RF MEMS shunt connected switch is with the electrostatically actuated membrane in the “UP” position, resulting often too high reflection values due to some technological mismatch between the designed geometrical values (length, width, ...) and the manufactured ones. Thus, to reduce this drawback improving the matching, the structure in Figure 1 has been proposed and extensively studied. In particular, for such a component, the matching condition has been imposed in [8] by means of Equation (4). In this section Equation (5) will be used to achieve the same result, characterizing the component in terms of the above defined image phase. To this end the proper modeling of the membrane plays a crucial role. A number of papers have been published on this topic in literature [14–19]. Recently a general and accurate equivalent circuit has been developed in [8] for the coplanar bridge in the “up” position. More in detail, neglecting losses, the bridge has been modeled by means of a T-network with two equal series connected  $X_s$  reactances and a shunt connected  $X_p$  reactance. The values of  $X_s$  and  $X_p$  can be provided by experimental measurements or by electromagnetic simulations. The same topology is adopted in this paper. Therefore the model of the structure in Figure 1 is obtained by replacing the membrane with its T-network. The symmetry property of this circuit allows analyzing only the half-cell topology depicted in Figure 2. Since the half-cell is a non-symmetric network, for its characterization two image impedances  $Z_{ihc1}$  and  $Z_{ihc2}$  must be defined together with the image phase  $\phi_{ihc}$ . These parameters are related to the elements of the half-cell transmission matrix as follows:

$$A_{hc} = \cos \phi_{ihc} \sqrt{\frac{Z_{ihc1}}{Z_{ihc2}}} = \left(1 + \frac{X_S}{2X_P}\right) \cos \theta + \frac{Z_c}{2X_P} \sin \theta \quad (7)$$

$$B'_{hc} = \sin \phi_{ihc} \sqrt{Z_{ihc1} Z_{ihc2}} = X_S \cos \theta + Z_c \sin \theta \quad (8)$$

$$C'_{hc} = \frac{\sin \phi_{ihc}}{\sqrt{Z_{ihc1} Z_{ihc2}}} = \left(1 + \frac{X_S}{2X_P}\right) \frac{\sin \theta}{Z_c} - \frac{\cos \theta}{2X_P} \quad (9)$$

$$D_{hc} = \cos \phi_{ihc} \sqrt{\frac{Z_{ihc2}}{Z_{ihc1}}} = \cos \theta - \frac{X_S}{Z_c} \sin \theta \quad (10)$$

For a well-known property of the image parameter, since two half-cells equal between them compose the basic cell, its image phase  $\phi_{ic}$  is related to  $\phi_{ihc}$  by the formula:

$$\phi_{ic} = 2\phi_{ihc} \quad (11)$$

Two configurations will be considered: the first one utilizes a single basic cell (Figure 1), whereas the second one is realized by the cascaded connection of two basic cells (Figure 3). Thus for the image phases of these two structures we obtain:

$$\phi_i = \phi_{ic} = 2\phi_{ihc} \quad \text{for the single basic cell configuration (Figure 1)} \quad (12)$$

$$\phi_i = 2\phi_{ic} = 4\phi_{ihc} \quad \text{for the double basic cell configuration (Figure 3)} \quad (13)$$

Forcing the phase  $\phi_i$  to the values provided by (5) we have a matched switch when the bridge is in the “up” position. Because of the periodic behavior of the trigonometric functions we shall assume for  $k$  the two values  $k = 1, 2$ , thus writing for  $\phi_i$ :

$$\phi_i = \pi, 2\pi \quad (14)$$

It is important noting that the use of the image phase condition in Equation (5) instead of the transmission matrix element condition in Equation (6) allows a remarkable reduction of the analytic effort. In fact, the calculation of  $B'$  and  $C'$ , even only for the entire single cell is quite intricate. Much worse it is to obtain  $B'$  and  $C'$  for the double cell configuration, resulting in a long and tedious procedure. Actually, for a network composed by a number of equal basic cells the use of the image parameters provides simple and straightforward mathematical relationships between the representation of the elementary cell and the representation of the entire structure. The latter consideration suggests a further application of the presented approach to another MEMS component. In fact, the topology of a binary distributed phase shifter is basically the same of the double cell switch, and thus (4) and (5) can be used to achieve a non-conventional design methodology for this kind of phase shifter. This aspect will be investigated in future research activity.

In the following part of this section a detailed analysis for the single and double cell switches will be presented.

### 3.1. The Single Cell Configuration

According to Equations (12) and (14) two cases will be considered:

$$\text{a) } \quad \phi_i = \phi_{ic} = 2\phi_{ihc} = \pi \quad \Rightarrow \quad \phi_{ihc} = \frac{\pi}{2}$$

Inserting this  $\phi_{ihc}$  value in (7) and (10) we have:

$$A_{hc} = \left(1 + \frac{X_S}{2X_P}\right) \cos \theta + \frac{Z_c}{2X_P} \sin \theta = 0 \quad (15)$$

$$D_{hc} = \cos \theta - \frac{X_S}{Z_c} \sin \theta = 0 \quad (16)$$

After calculation, one may obtain the following relations for the characteristic impedance  $Z_c$  and for the electric length of the transmission lines, termed in this case  $\theta_1$ :

$$Z_c = \sqrt{-X_S(X_S + 2X_P)} \quad (17)$$

$$\tan \theta_1 = \frac{Z_c}{X_S} \quad (18)$$

$$\text{b) } \quad \phi_i = \phi_{ic} = 2\phi_{ihc} = 2\pi \quad \Rightarrow \quad \phi_{ihc} = \pi$$

Substituting this  $\phi_{ihc}$  value in Equations (8) and (9), we obtain  $B'_{hc} = 0$ ,  $C'_{hc} = 0$ , which provide for  $Z_c$  the same expression (17). Moreover, for the electric length, defined  $\theta_2$ , we find:

$$\tan \theta_2 = -\frac{X_S}{Z_c} \quad \Rightarrow \quad \theta_2 = \theta_1 + \frac{\pi}{2} \quad (19)$$

In actual MEMS shunt varactor typically we have:

$$X_S > 0, \quad X_P < 0, \quad |X_S| < |X_P| \quad \Rightarrow \quad -X_S(X_S + 2X_P) > 0$$

Therefore  $Z_c$  is a real number. We can infer from Equation (19) that case a) ( $\theta = \theta_1$ ) requires quite shorter transmission line sections in comparison to case b) ( $\theta = \theta_2$ ), resulting in a remarkable size reduction. Moreover, both the solutions do not allow choosing the characteristic impedance value, being this parameter fixed for given  $X_s$  and  $X_p$  reactances.

### 3.2. The Double Cell Configuration

The same procedure used for the single cell configuration will be adopted here. Therefore, according to Equations (16) and (17), two cases will be studied:

$$\text{a) } \quad \phi_i = 2\phi_{ic} = 4\phi_{ihc} = \pi \quad \Rightarrow \quad \phi_{ihc} = \frac{\pi}{4} \quad (20)$$

Equations (7), (8), (9) and (10) provide the relationship:

$$\sqrt{\frac{B'_{hc}C'_{hc}}{A_{hc}D_{hc}}} = \tan \phi_{ihc} = \sqrt{\frac{(X_S + U) \left( \frac{U}{Z_c^2} \left( 1 + \frac{X_S}{2X_P} \right) - \frac{1}{2X_P} \right)}{\left( 1 + \frac{X_S}{2X_P} + \frac{U}{2X_P} \right) \left( 1 - \frac{X_S U}{Z_c^2} \right)}} \quad (21)$$

where

$$U = Z_c \tan \theta \quad (22)$$

Imposing in Equation (21) the  $\phi_{ihc}$  value given by Equation (20), after some algebra, the following quadratic equation in the unknown  $U$  is obtained:

$$-\frac{U^2}{Z_c^2} \left[ \left( 1 + \frac{X_s}{X_p} \right) \right] + U \left[ \frac{1}{X_p} - \frac{2X_s}{Z_c^2} \left( 1 + \frac{X_s}{2X_p} \right) \right] + \frac{X_s}{X_p} + 1 = 0 \quad (23)$$

The solutions of this equation can be written as:

$$U_1 = \frac{\frac{1}{X_p} - \frac{2X_s}{Z_c^2} \left(1 + \frac{X_s}{2X_p}\right) - \sqrt{\Delta}}{\frac{2}{Z_c^2} \left[1 + \frac{X_s}{X_p}\right]}, \quad (24)$$

$$U_2 = \frac{\frac{1}{X_p} - \frac{2X_s}{Z_c^2} \left(1 + \frac{X_s}{2X_p}\right) + \sqrt{\Delta}}{\frac{2}{Z_c^2} \left[1 + \frac{X_s}{X_p}\right]} \quad (25)$$

where:

$$\Delta = \left[ \frac{1}{X_p} - \frac{2X_s}{Z_c^2} \left(1 + \frac{X_s}{2X_p}\right) \right]^2 + \frac{4}{Z_c^2} \left(1 + \frac{X_s}{X_p}\right)^2 \quad (26)$$

$$\text{b) } \phi_i = 2\phi_{ic} = 4\phi_{ihc} = 2\pi \quad \Rightarrow \quad \phi_{ihc} = \frac{\pi}{2}$$

This case has been previously studied in the single cell configuration analysis.

#### 4. COMPARISON WITH THE IMAGE IMPEDANCE APPROACH

For the single cell configuration the design of the transmission lines can be even carried out by means of the image impedance method. As it results from [8], with that approach the calculation of the electric length of the lines is achieved by solving a quadratic equation, whose unknown is the same variable  $U$  defined in (22). The discriminant  $\Delta_1$  of that equation is re-written here for convenience of the reader [8]:

$$\Delta_1 = \left[ (X_p + X_s) \left(1 - \frac{Z_0^2}{Z_c^2}\right) \right]^2 - 4 \left[ \frac{1}{2} + \left(X_p + \frac{X_s}{2}\right) X_s \frac{Z_0^2}{Z_c^4} \right] \left[ \left(X_p + \frac{X_s}{2}\right) X_s + \frac{Z_0^2}{2} \right] \quad (27)$$

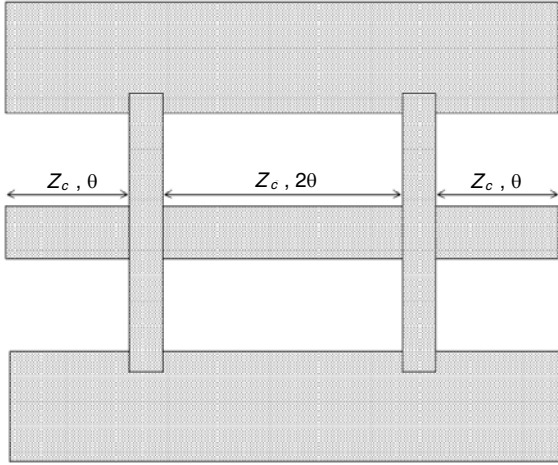
We can note that, since it could be  $\Delta_1 < 0$ , the image impedance approach does not always ensure the existence of the problem solution. A similar event occurs even for the single cell topology, by using the image phase matching method, because of the technological limits on the characteristic impedance values. Conversely, for the above studied double cell configuration the condition  $\Delta > 0$  is always fulfilled, and furthermore the designer can choose the  $Z_c$  value. For this case, from (26), we find:

$$\left| \frac{1}{X_p} - 2\frac{X_s}{Z_c^2} \left(1 + 2\frac{X_s}{X_p}\right) \right| < \sqrt{\Delta} \quad (28)$$

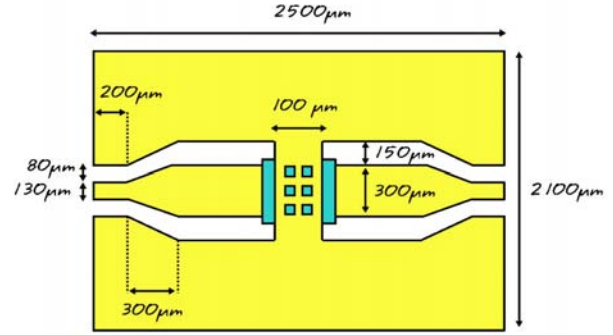
Since the denominator of Equations (24) and (25) is typically a positive number, it can be inferred that in most cases  $U_2 > 0$  and  $U_1 < 0$ , being otherwise  $U_2 < 0$  and  $U_1 > 0$ . Thus, in conclusion, the image phase approach applied to the double cell configuration always provides a feasible solution of the design problem, irrespective of the  $X_s$  and  $X_p$  values.

#### 5. CHARACTERIZATION OF THE REALIZED MEMS BRIDGE

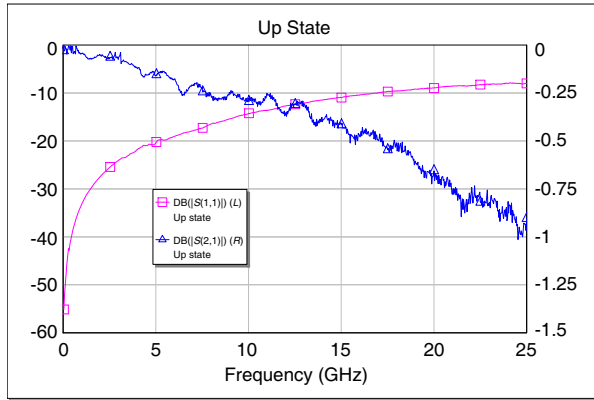
Microwave MEMS shunt coplanar varactors typically include a thin flexible metal bridge which is suspended across the central conductor of the transmission line and is electrostatically actuated. In [20] the authors have recently presented a novel process based on SU-8 for the fabrication of MEMS shunt capacitive devices. SU-8 is a negative photoresist, and has been used both for the lateral supports for the suspended membrane and as sacrificial layer. In that paper [20] all the technological aspects concerning the fabrication of such a component have been discussed, and therefore for sake of brevity will not be presented here again. The final structure is depicted in Figure 4. We can note that transmission line sections are added to the coplanar bridge to characterize the MEMS device by means of microwave probes connected to a network analyzer. Since the characteristic impedance of these coplanar lines is 50 ohm their presence does not affect the magnitude of the scattering parameters. The frequency



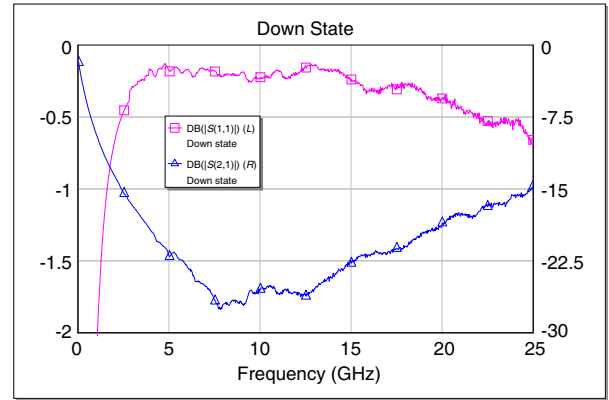
**Figure 3.** The double basic cell configuration.



**Figure 4.** Schematic of the RF MEMS bridge.



**Figure 5.** Magnitude of the  $S_{11}$  and  $S_{21}$  parameters with the bridge in the UP state.



**Figure 6.** Magnitude of the  $S_{11}$  and  $S_{21}$  parameters with the bridge in the DOWN state.

behaviors of the measured  $|S_{11}|$  and  $|S_{21}|$  are plotted in Figures 5 and 6 for the membrane in the up and down position respectively. In particular, from these experimental results we can infer that for frequency values higher than 10 GHz the device in the ON state exhibits high reflection losses. To solve this problem the above developed approach will be used in the next section for the synthesis of the matching transmission lines.

## 6. DESIGN CONSIDERATIONS, SIMULATION RESULTS AND DISCUSSION

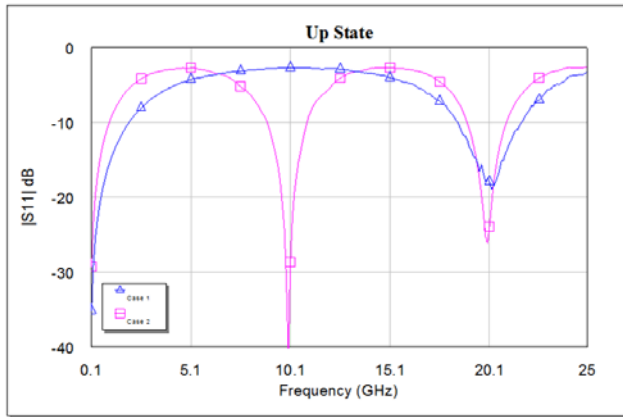
The first step of the design procedure of the switch is to choose the central operating frequency  $f_0$ . We assume  $f_0 = 20$  GHz. According to the described analytic model, the second step is to obtain the  $X_s$  and  $X_p$  values at  $f_0$  for the MEMS coplanar bridge in the UP position. In order to remove the effects of the 50 ohm coplanar lines from the  $X_s$  and  $X_p$  reactances a simple de-embedding method can be used, shifting the reference planes of a distance corresponding to the electric length of these transmission lines. More in detail, as shown in Figure 4, the bridge is inserted between two 50 ohm lines, each one with a geometric length of 1200  $\mu\text{m}$ , that is  $72.6^\circ$  at  $f_0$ . Therefore, the phase of each scattering parameter measured at  $f_0$  has been changed by adding  $145.2^\circ$ . The so obtained scattering parameters are used in the conversion relations from  $S$  matrix to  $Z$  matrix, having eventually the following values for  $X_s$  and  $X_p$ :  $X_s = 3.4 \Omega$ ,  $X_p = -56.6 \Omega$ . These reactances must be inserted in the synthesis equations derived in Section 3 for the single and double cell configurations.

### 6.1. The Single Cell Configuration

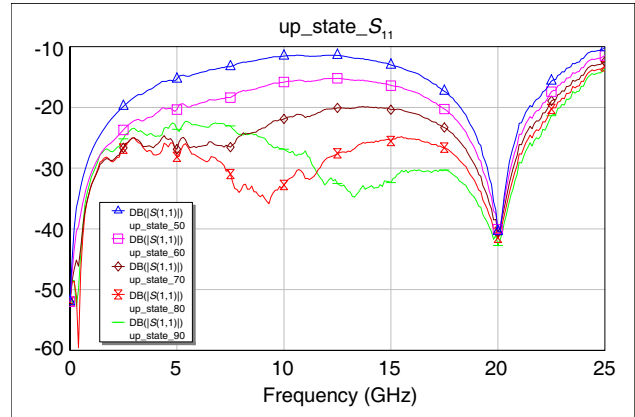
By substituting the achieved  $X_s$  and  $X_p$  reactances in Equations (17) and (18) we find  $Z_c = 19.3\Omega$  and  $\theta_1 = 80^\circ$ . It is worth noting that such a characteristic impedance value is not easy to realize in coplanar technology [21,22]. As discussed above, in addition to this first case, another single cell structure should be considered. The second solution employs transmission line sections with the same characteristic impedance value  $Z_c$  of the first case, and electric length  $\theta_2$  given by Equation (19):  $\theta_2 = 170^\circ$ . Both the structures have been simulated by means of the software package AWR Microwave Office, using a black box model for the MEMS bridge in the up position, in which the de-embedded scattering parameters are inserted. The model is obtained by subtracting from the measured data the effect of an input line and an output line with 50 ohm characteristic impedance and electrical length  $72.6^\circ$  at  $f_0$ , that is adding two lines with negative lengths. The behaviors of the reflection coefficient amplitudes versus frequency are shown in Figure 7, where case 1 corresponds to the electric length  $\theta_1$  and case 2 corresponds to  $\theta_2$ . Satisfactory values for  $S_{11}$  are obtained at  $f_0$  for case 2, although the switch appears to be too long. The other structure (case 1) is quite shorter, but exhibits not adequate values for the reflection coefficient.

### 6.2. The Double Cell Configuration

By using the above given extracted reactances  $X_s$  and  $X_p$ , the denominator of Equations (24) and (25) is a positive number, and therefore, according to the results of Section 4, we obtain:  $U_1 < 0, U_2 > 0$ . Let us assume for the characteristic impedance  $Z_c$  a range from  $50\Omega$  to  $90\Omega$ . In order to have a short component we shall adopt the solutions with  $\theta < \pi/2$ . Hence, for the physical realization of the



**Figure 7.** Magnitude of the  $S_{11}$  parameter with the bridge in the UP position for two single cell configurations corresponding respectively to the electric length values  $\theta_1$  (case 1) and  $\theta_2$  (case 2).

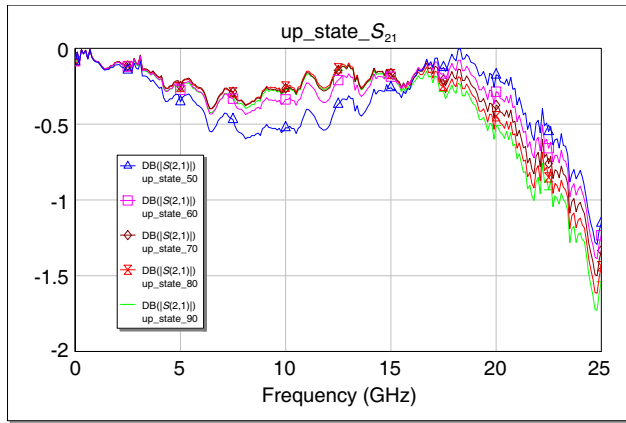


**Figure 8.** Magnitude of the  $S_{11}$  parameter with the bridge in the UP position (ON state) for different double cell configurations. Five cases are considered, characterized by the  $Z_c$  and  $\theta$  values reported in Table 1.

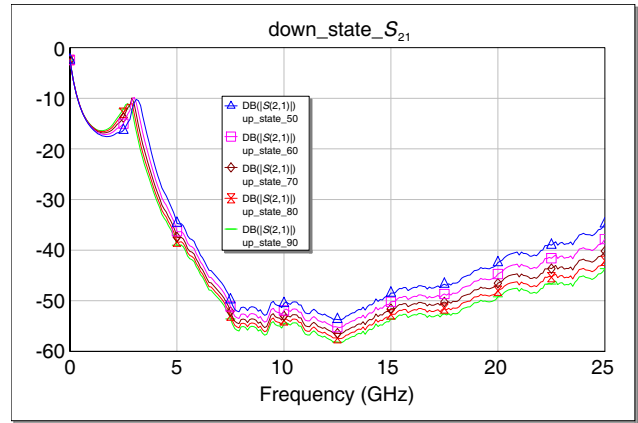
**Table 1.** Characteristic impedance  $Z_c$  of the double switch configuration and corresponding electrical lengths of the uniform line sections.

$Z_c$ (ohm)	$\theta$ (degrees)
50	30.8
60	29
70	27.3
80	25.7
90	24.2

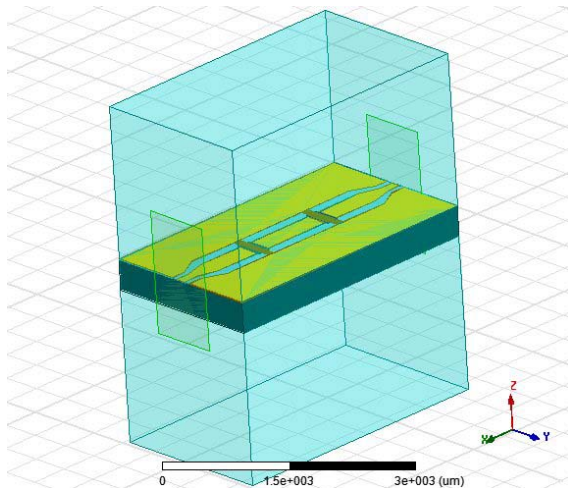
structure  $U$  must be a positive number. Consequently, only  $U_2$  can be chosen. The electric lengths  $\theta$ , computed by means of Equation (22), are summarized in Table 1 for different values of the characteristic impedance  $Z_c$ . The results of the simulations of these five switches, performed by AWR Microwave Office utilizing the previously presented black box model for the MEMS membrane in the on configuration, are illustrated in Figures 8 and 9. In particular, the amplitude of  $S_{11}$  as a function of frequency is plotted in Figure 8 for characteristic impedance values ranging from  $50\ \Omega$  to  $90\ \Omega$ . The amplitude of  $S_{21}$  is shown in Figure 9. For sake of completeness for the switch in the OFF state the isolation ( $|S_{21}|$ ) versus frequency is presented in Figure 10. These last behaviors have been obtained using the same procedure adopted for the simulation of the switch in the ON state, but inserting in the black box model the de-embedded measured scattering parameters for the bridge in the down position.



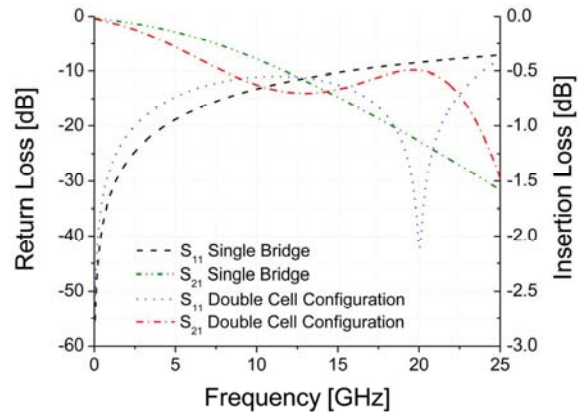
**Figure 9.** Magnitude of the  $S_{21}$  parameter with the bridge in the UP position (ON state) for different double cell configurations. Five cases are considered, characterized by the  $Z_c$  and  $\theta$  values reported in Table 1.



**Figure 10.** Isolation (magnitude of  $S_{21}$  with the bridge in the DOWN position, OFF state) for different double cell configurations. Five cases are considered, characterized by the  $Z_c$  and  $\theta$  values reported in Table 1.



**Figure 11.** Layout of the double cell switch ( $Z_c = 50\ \Omega$ ) in the ON state for the electromagnetic simulation by means of the Ansoft HFSS 3D software package.



**Figure 12.** Behaviour of  $|S_{11}|$  and  $|S_{21}|$  versus frequency for the switch in the on state. The Ansoft HFSS 3D software package has been used for the electromagnetic simulation of the MEMS single bridge structure and of the double cell configuration with  $Z_c = 50\ \Omega$ .



The main considerations suggested by the presented results can be summarized as follows:

- increasing the characteristic impedance  $Z_c$  the electric length  $\theta$  decreases;
- in the ON state the switch exhibits a broadband frequency behavior for the  $S_{11}$  parameter for  $Z_c > 80 \Omega$ ;
- in the OFF state high isolation values are obtained;
- The choice of  $Z_c = 50 \Omega$  allows to have a remarkable size reduction. In fact, the external transmission line sections are not needed. Hence, neglecting the bridge contribution to the overall size of the switch, the electric length of the component is halved, in comparison with the other possible solutions, passing from  $4\theta$  to  $2\theta$ . Moreover, there is no discontinuity due to the presence of an impedance change from  $Z_c$  to  $Z_0$  and therefore of a step in width in the central conductor or in the lateral ground planes of the coplanar waveguide. In order to check the validity of the presented approach the structure with  $Z_c = 50 \Omega$  has been simulated in the ON state by means of the Ansoft HFSS 3D electromagnetic simulator. The box with the layout of the double cell switch is depicted in Figure 11. Numerical values are shown in Figure 12, where  $|S_{11}|$  and  $|S_{21}|$  are plotted as a function of the frequency even for the case of the single MEMS coplanar bridge. A good agreement with the results in Figures 5, 8 and 9 has been obtained.

### 6.3. Final Discussion

In this part of the paper, we shall present a final discussion on the structures proposed for the solution of the design problems of the MEMS shunt capacitive switches. The first step is to compare the coplanar single bridge configuration with the double bridge one. It is obvious that the use of only one MEMS device is an important advantage. However, the single bridge component exhibits poor electric performance together with a total length of the transmission line sections quite higher than that one needed for the double bridge structure. Therefore, in our opinion the single bridge configuration is not suitable for the realization of the switch. For the other topology, two different solutions can be adopted. The first one is characterized by  $Z_c = 50 \Omega$ . In this case, the main advantage is the remarkable reduction of the size. An alternative possibility is to use a high value for the characteristic impedance ( $Z_c > 80 \Omega$ ), obtaining a quite short component with very good electric performance in terms of reflection losses frequency behavior.

## 7. CONCLUSION

In this paper, it has been described as a novel approach to analytically design the transmission line sections used in RF MEMS shunt switches to have a matched component in the “ON” state. The method is based on the image parameter characterization of the switch. In particular, the image phase has been utilized to impose the matching condition. Two topologies, characterized by a different number of basic cells, have been studied. Original closed-form expressions for the synthesis of the component have been given. Experimental data of a previously realized MEMS coplanar bridge have been used to produce design examples. A detailed discussion on these results has been presented. The effectiveness of the proposed approach has been finally demonstrated.

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