

## Design of a Novel Multi-Layer Wideband Bandpass Filter with a Notched Band

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**Abstract**—A wideband filter with a notched band is presented. The proposed filter is formed by cascading three coupling units, and each coupling unit is composed of two curved T-shaped microstrip patches at the top and bottom layers and a circular coupling slot at the mid layer. Overlapping three coupling units could result in a wideband filter with a tunable notched band. To analyse the resonance characteristics, the equivalent circuit model is presented. The notched frequency is 5.8 GHz, and within the passband, the insertion and return losses are better than  $-2$  dB and  $-15$  dB, respectively. The group delays are 0.08 ns and 0.12 ns correspondingly, and the upper stopband reaches 15 GHz. The multi-layer structure leads to a compact size and tight coupling characteristics, and the feasibility and excellent performance of the design is verified.

### 1. INTRODUCTION

With development of modern wireless systems, demands for wireless communication change from initial voice transmission to high-speed transmissions such as files, images, and multimedia. However, narrow-band communication systems could not satisfy those demands anymore, thus the research of broadband has been an inevitable trend. Wideband filters, especially ultra-wideband (UWB) filters [1], have been attracting more and more attention in industry and academia. Meanwhile, most of the WLAN systems are designed to operate in the 2.4 GHz (IEEE 802.11b and g) and 5.0 GHz frequency bands, e.g., 5.15 to 5.35 GHz (IEEE 802.11a lower bands) and 5.725 to 5.825 GHz (IEEE 802.11a upper bands) are used in the USA. For eliminating the interference of these WLAN radio signals in UWB services, the wideband filter with notched characteristic comes to be a requirement.

UWB [2, 3] and notched filters [4] with multiple-mode resonator (MMR) can generate multiple transmission poles in the band to enhance circuit coupling, while the high fabricated precision of 0.05 mm is hard to realize [2, 4]. Other filters with defected ground structure (DGS) [5, 6] and triangular ring loaded stub resonator (TRLSR) [7] have a very narrow notched band, but they are not suitable for eliminating all WLAN signals in 5–6 GHz.

[8] proposes a three-layer ultra-wideband coupler. There is a broadside coupling between the elliptical patches at the upper and bottom layers and the elliptical slots at the mid ground layer, and the coupling characteristics are analyzed. Based on this structure, [9, 10] propose a UWB filter. These designs have realized tight coupling and miniaturization, and the fabrication difficulties as in [2–4] are avoided simultaneously.

In this paper, a novel resonator is proposed by utilizing broadside coupling between the two curved T-shaped microstrip patches at the top and bottom layers and a circular coupling slot at the mid layer. Cascading three resonators could lead to UWB characteristics, as well as a notched band if those three

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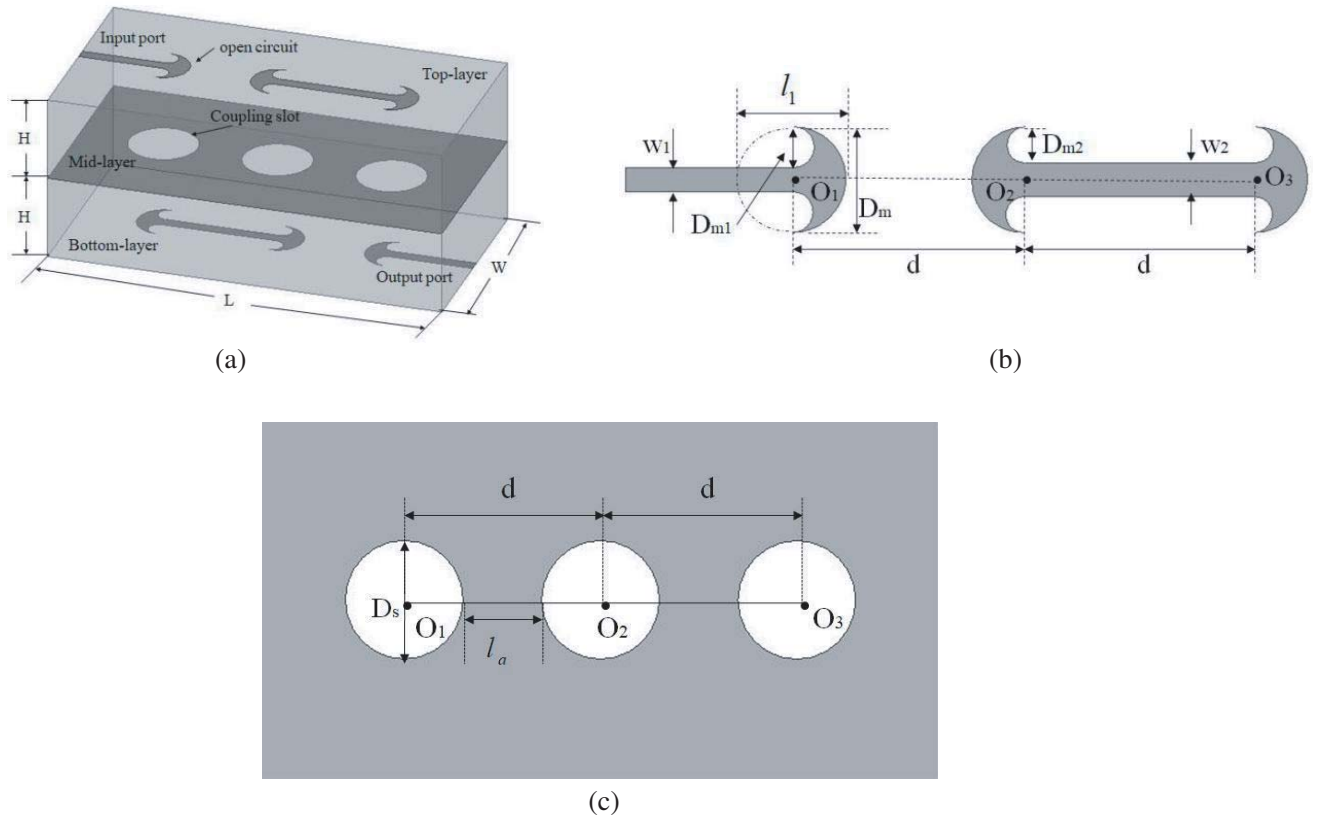
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coupling units are close to each other to be partially overlapped. The equivalent circuit and methods to adjust the notched band are given, and consequently the characteristics of UWB and notched band have been analyzed. Finally, a prototype with notched band of 5.8 GHz is fabricated, validating an excellent circuit performance. Compared with [9, 10], the novel broadside coupling circuits could be used to design UWB devices, as well as a wideband filter with notched band which could eliminate all the WLAN signals within 5–6 GHz.

## 2. THE DESIGN OF FILTER

### 2.1. The Design of UWB Filter

The structure of the proposed filter is shown in Fig. 1. Fig. 1(a) depicts the 3-D view. The circuit consists of three coupling units, and each one includes two curved T-shaped microstrip patches at the top and bottom microstrip layers and a circular coupling slot at the mid ground layer. The curved T-shaped microstrip patch is composed of a large semicircle with diameter of  $D_m$ , where two small semicircles with diameters of  $D_{m1}$  and  $D_{m2}$  are removed. Those parameters follow  $D_{m1} = (D_m - w_1)/2$ ,  $D_{m2} = (D_m - w_2)/2$ , where  $w_1$  and  $w_2$  are the widths of two microstrip lines. Fig. 1(c) exhibits the circular coupling slot with diameter of  $D_s$  at mid ground layer.  $O_1$ ,  $O_2$ , and  $O_3$  are centers of three coupling slots, and parameter  $d$  is the distance between either two adjacent centers.



**Figure 1.** The structure and configuration of the proposed filter. (a) 3-D view. (b) The curved-T-shaped structure. (c) Coupling slot on the ground.

The edges of the curved T-shaped microstrip patches are open circuits, and the curved T-shaped microstrip patches at the top and bottom layers are coupled with the coupling slots at the mid common ground. The coupling unit belongs to a microstrip-slot broadside coupled structure [11], which could be equivalent to a two-port network, and its reflection coefficient  $S_{11}$  of the input and insertion loss  $S_{21}$

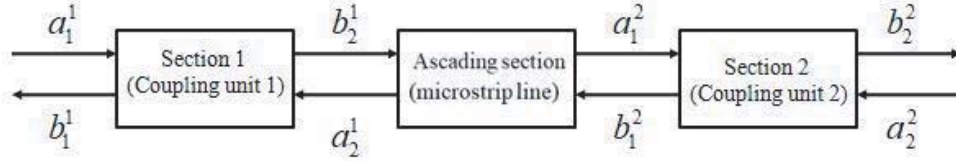
of the output can be calculated as follows [9]:

$$S_{11} = \frac{1 - K^2 [1 + \sin^2(\beta_{ef}l_1)]}{\left[ \sqrt{1 - K^2} \cos(\beta_{ef}l_1) + j \sin(\beta_{ef}l_1) \right]^2} \quad (1)$$

$$S_{21} = \frac{j2K\sqrt{1 - K^2} \sin(\beta_{ef}l_1)}{\left[ \sqrt{1 - K^2} \cos(\beta_{ef}l_1) + j \sin(\beta_{ef}l_1) \right]^2} \quad (2)$$

where  $K$  is the coupling coefficient of the curved T-shaped patches between top and bottom layers,  $\beta_{ef}$  the effective phase constant in the medium of the coupled structure, and the electrical length is  $\beta_{ef}l_1 = \pi/2$ . The length of coupling region  $l_1$  is chosen by the one-quarter of guide wavelength at the center of the expected passband (6.85 GHz), here,  $l_1 = D_m = 4.5$  mm.

The schematic diagram of the signal flow between them when two coupling units are cascaded is shown in Fig. 2.



**Figure 2.** The schematic diagram of the signal flow between two coupling units.

Assume that  $a_i^j$  and  $b_i^j$  are the incident and reflected signals at the  $i$ th port of the  $j$ th section, respectively, and the microstrip lines are lossless and perfectly matched with the two coupling units. After two coupling units are cascaded, the return loss ( $S_{11} = b_1^1/a_1^1$ ) and insertion loss ( $S_{21} = b_2^2/a_1^1$ ) as a function of the  $S$ -parameters of its sections are equal to [9, 12]

$$S_{11} = S_{11}^1 + \frac{(S_{21}^1)^2 S_{11}^2 e^{-j2\beta_m l_a}}{1 - S_{11}^1 S_{11}^2 e^{-j\beta_m l_a}} \quad (3)$$

$$S_{21} = \frac{S_{21}^1 S_{21}^2 e^{-j\beta_m l_a}}{1 - S_{11}^1 S_{11}^2 e^{-j\beta_m l_a}} \quad (4)$$

where  $\beta_m$  is the phase constant of the microstrip line, and  $l_a$  is the physical length correspondingly, shown in Fig. 1(c), i.e.,  $l_a = d - D_s$ . In order to minimize the unexpected mutual coupling between the top (or bottom) layers of those units, both input and output microstrip lines are  $50 \Omega$ , thus  $w_1 = w_2 = 1.15$  mm. Fig. 3(a) shows the effect of  $l_a$  on the UWB filter's performance.

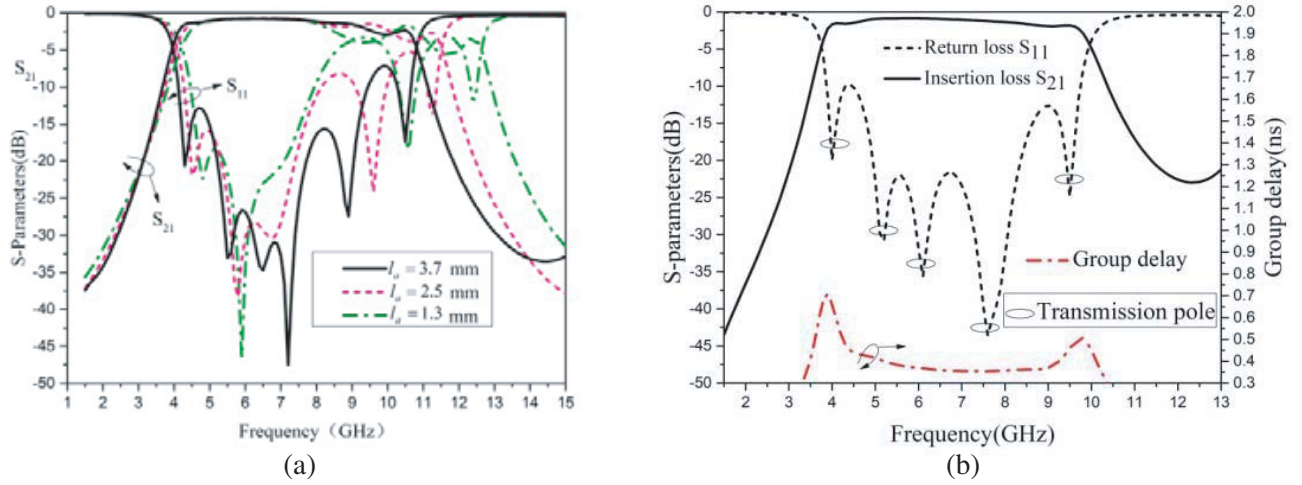
In fact, Eqs. (3) and (4) can be generalized for more ( $n$ ) sections as follows

$$S_{11} = S_{11}^{eff(n-1)} + \frac{(S_{21}^{eff(n-1)})^2 S_{11}^n e^{-j2\beta_m l_a}}{1 - S_{11}^{eff(n-1)} S_{11}^n e^{-j\beta_m l_a}} \quad (5)$$

$$S_{21} = \frac{S_{21}^{eff(n-1)} S_{21}^n e^{-j\beta_m l_a}}{1 - S_{11}^{eff(n-1)} S_{11}^n e^{-j\beta_m l_a}} \quad (6)$$

where  $(S_{11}^{eff(n-1)}, S_{21}^{eff(n-1)})$  and  $(S_{11}^n, S_{21}^n)$  are  $S$ -parameters of the first ( $n - 1$ ) sections and the last section, respectively.

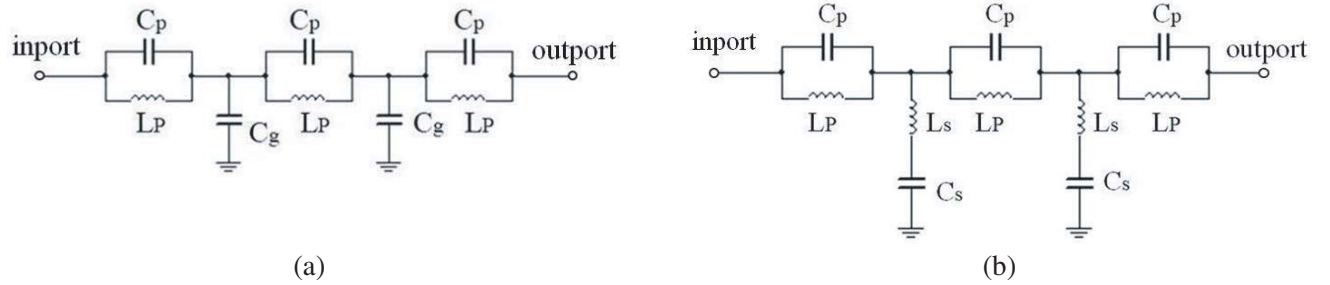
We can see from above analysis that  $f_0$  is decided by  $l_1$ , and the best  $S$ -parameters after cascading coupling units are decided by  $l_a$ . Fig. 3(b) shows the performance of the UWB filter when taking  $D_m = 4.5$  mm,  $l_a = 5.1$  mm. The lower and upper frequencies are 4.4 GHz and 9.5 GHz. The insertion loss  $S_{21}$  and return loss  $S_{11}$  are better than  $-3$  dB and  $-15$  dB, respectively. The passband has the 3 dB fractional bandwidth (FBW) of 88.2%, and the variation of group delay is 0.2 ns. There are five transmission poles generated within the passband, thus the coupling degree is enhanced.



**Figure 3.** The  $S$  parameters of UWB filter, where  $D_m = 4.5$  mm,  $D_s = 5.3$  mm,  $w_1 = w_2 = 1.15$  mm,  $H = 0.508$  mm,  $L = 38$  mm,  $W = 15$  mm. (a) The effect of  $l_a$  on the UWB filter's performance. (b) The  $S$  parameters of UWB when  $l_a = 5.7$  mm.

## 2.2. Implementation of Notched Filter

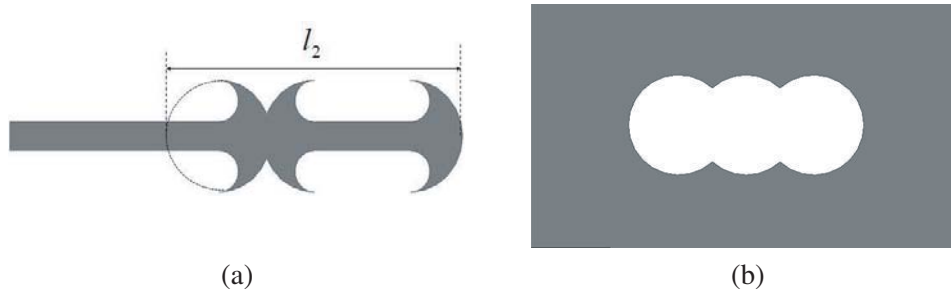
As depicted in Fig. 1(a), each coupling unit could be regarded as a parallel resonator consisting of an inductor  $L_P$  and a capacitor  $C_p$ . The whole circuit is formed by connecting three identical resonators in series, and the approximate equivalent circuit is shown in Fig. 4(a). Because the microstrips at the top and bottom layers have the common ground plane at the mid layer,  $C_g$  is the grounding capacitor shared by the adjacent resonators.



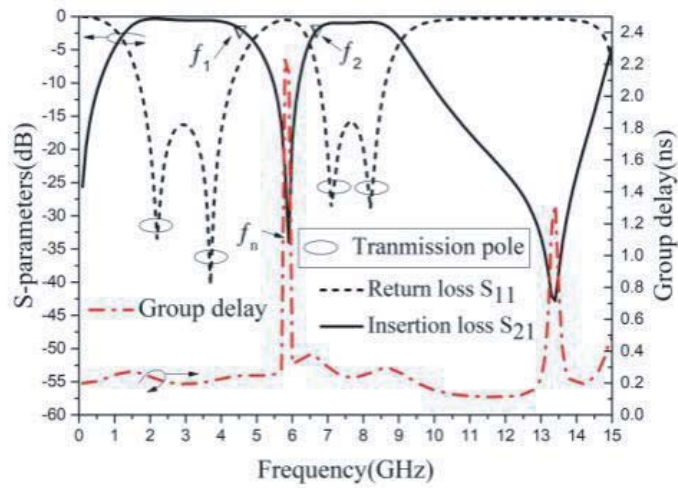
**Figure 4.** Equivalent circuit of notched filter with curved-T-shaped. (a) The equivalent circuit of UWB filter. (b) The equivalent circuit of notched filter.

If a notched band is needed, we should introduce a stopband within the expected passband, thus the filter shown in Fig. 1(a) should be modified. Keep the other parameters of Fig. 3(b) unchanged, and let three coupling units be close enough to each other and partly overlapped, just as shown in Fig. 5, where  $d = 4.12$  mm, and  $l_2$  is the physical length of the coupled slot. The  $S$  parameters are shown in Fig. 6, where  $f_n$  is the notch frequency;  $f_2$  and  $f_1$  are the upper and lower stopband frequencies of the notch, respectively; and the width of notched-band below  $-10$  dB is 800 MHz. Two transmission poles in passband before and after the notch band enhance the coupling degree. Insertion loss  $S_{21}$  and return loss  $S_{11}$  are better than  $-2$  dB and  $-15$  dB, and group delays are 0.08 ns and 0.12 ns. Compared with the UWB filter shown in Fig. 1, the whole passband moves to a lower band because the coupling length  $l_2$  is much longer than  $l_1$ .

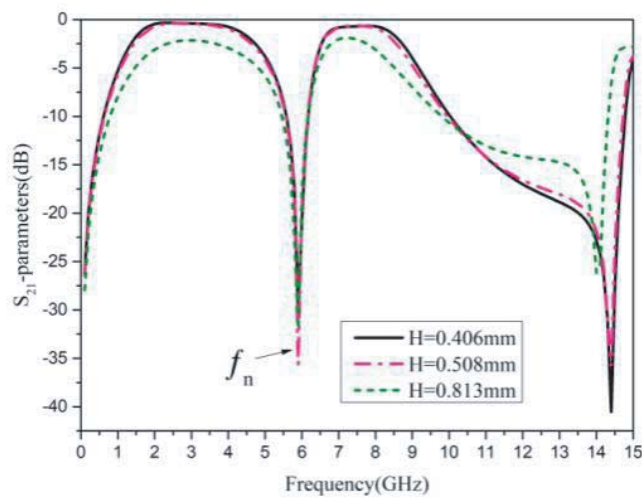
The equivalent circuit is shown in Fig. 4(b). Overlap of the curved T-shaped microstrip patches can be equivalent to grounding capacitors  $C_s$  and inductors  $L_s$  in series, thus a stopband circuit is



**Figure 5.** The structure of the notched filter. (a) The curved-T-shaped structure of notched filter. (b) The structure of couple slot on the mid ground.



**Figure 6.** The  $S$ -parameters of the notched filter.



**Figure 7.** The effect of  $H$  on the  $S$  parameters.

formed between two resonators. This circuit can be regarded as that the grounding capacitance  $C_g$  is transformed to a bandstop circuit where  $C_s$  and  $L_s$  are connected in series. The relationships among  $C_s$ ,  $L_s$ , and  $C_g$  are as follows [12]:

$$L_s = \frac{1}{2\pi\Delta C_g} \quad (7)$$

$$C_s = \frac{\Delta C_g}{2\pi f_n^2} \quad (8)$$

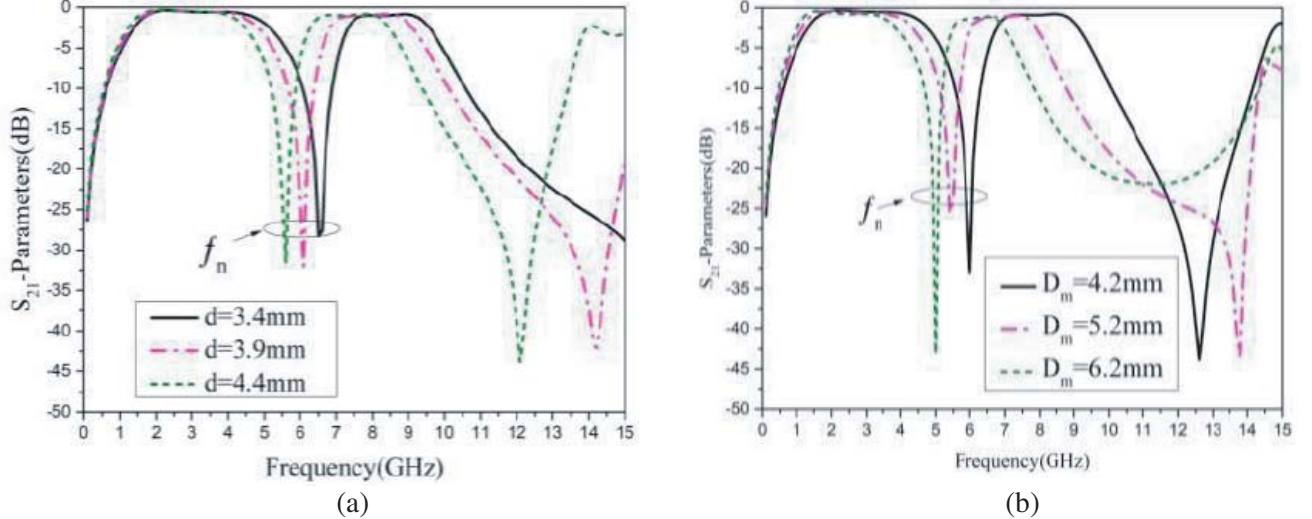
where the notched bandwidth  $\Delta = f_2 - f_1$ . According to Eqs. (7) and (8),  $C_g$  can be eliminated, and then  $f_n$  can be expressed as follows:

$$f_n = \frac{1}{2\pi\sqrt{C_s L_s}} \quad (9)$$

It is clear that  $f_n$  is independent of  $C_g$ , while  $C_g$  is related to the thickness of the substrate. Fig. 7 shows that, as  $H$  changes,  $f_n$  almost has no variation, and its value only depends on  $C_s$  and  $L_s$ .

### 2.3. Adjustment of the Notched Frequency

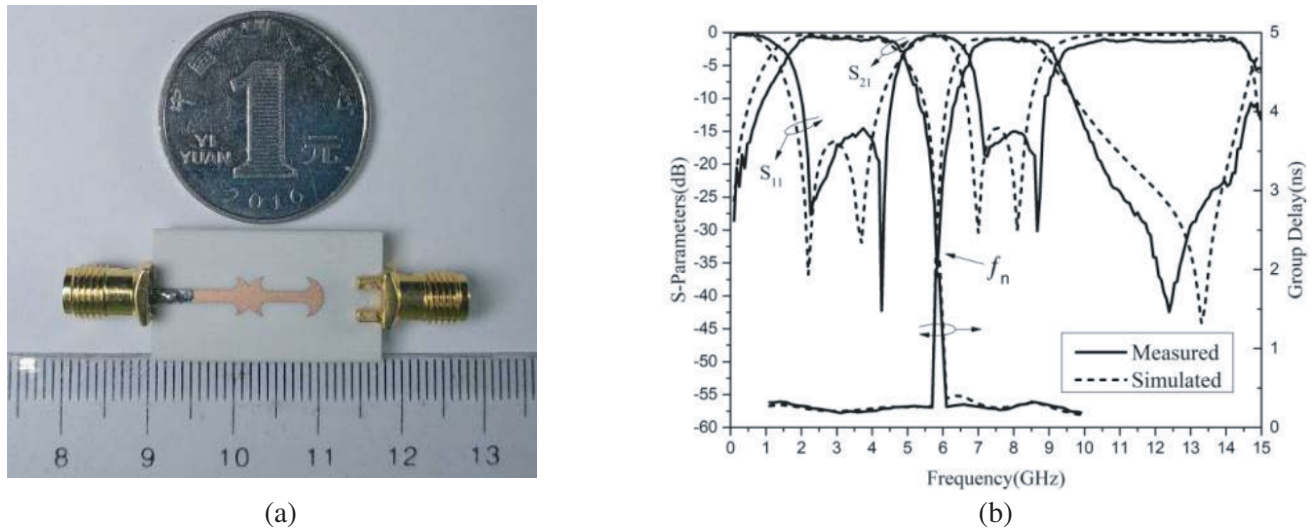
Based on the above analysis, it can be deduced that different values of  $C_s$  and  $L_s$  can affect  $f_n$ , while  $C_s$  and  $L_s$  can only be changed by adjusting the geometrical structure of the overlapped T-shaped patches. Three sets of values have been given to illustrate the influence of  $d$  and  $D_m$  in Fig. 8. Just as shown in Fig. 8(a), as  $d$  is increased,  $f_n$  moves from 6.5 GHz to 5.5 GHz, and Fig. 8(b) exhibits that  $f_n$  moves from 6 GHz to 5 GHz because of the increase of  $D_m$ , while the width of the notched bandwidth remains almost unchanged. The rules can be used to adjust the notched frequency to an interesting band and exclude other useless signals.



**Figure 8.** The effect of  $D_m$  and  $d$  on the performance of the notched band with  $D_s = 5.3$  mm,  $w_1 = w_2 = 1.15$  mm, here,  $S_{21}$  is insertion loss. (a) The effect of  $D_m$  on the  $S$  parameters with  $d = 4.12$  mm. (b) The effect of  $d$  on the  $S$  parameters with  $D_m = 4.5$  mm.

## 3. IMPLEMENTATION AND RESULTS

A photograph of the fabricated filter is shown in Fig. 9(a), and Rogers 4003C is used as the dielectric substrate, with dielectric constant  $\epsilon_r = 3.55$ , loss tangent  $\delta = 0.0029$ , and thickness 0.508 mm. The physical circuit has considered the WLAN signals of 5.8 GHz, here taking  $w_1 = 1.15$  mm,  $w_2 = 1.15$  mm,  $D_m = 4.22$  mm,  $d = 4.12$  mm,  $D_s = 5.02$  mm. Simulated and measured results of  $S$  parameters are



**Figure 9.** Photograph of the notched filter and experimental and simulated  $S$ -parameter results. (a) The photograph of the band notched filter. (b) Experimental and simulated  $S$ -parameter results.

shown in Fig. 9(b). The notched frequency is at 5.8 GHz, and the width of notched-band below  $-10$  dB is 1.1 GHz (5.3–6.4 GHz). The in-band group delays before and after the notched band are 0.08 ns and 0.12 ns. Measured and simulated results have an error of approximately 0.2 GHz within the passband due to insufficient precision in circuit fabrication. The overall size of the circuit is  $L \times W = 26.7 \text{ mm} \times 15 \text{ mm}$ .

#### 4. CONCLUSION

In this paper, a wideband filter with notched characteristics is proposed, which is composed of curved T-shaped microstrip patches. The feasibility is verified by fabricated production. The notched band can be flexibly adjusted by regulating the length of the coupling regions. The filter has a compact size and excellent performance.

#### ACKNOWLEDGMENT

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