

Embedded Resonances for Discrimination of Multiple Passive Nonlinear Targets Applicable to DORT

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Abstract—This paper presents a method to distinguish multiple passive nonlinear targets, which can be applied to detection and selective wave focusing based on the decomposition of the time-reversal operator (DORT). A recent demonstration of DORT applied to harmonic scattering has shown that passive nonlinear targets (scatterers) can be detected in the presence of linear scatterers and separated into discrete eigenvalues. While DORT is effective in detecting multiple nonlinear targets, it could be difficult to discriminate these nonlinear scatters as their harmonic responses would look similar to each other. Our proposed approach to overcoming this difficulty is based on simply embedding a unique resonant notch in the second harmonic band for each nonlinear scatterer, so as to make the notch appear in the associated eigenvalue, permitting identification and discrimination of the scatterer. We numerically demonstrate the basic feasibility of the proposed idea by considering various configurations in a two-dimensional model. The results show that a uniquely embedded resonant notch in a nonlinear target consistently appears in the corresponding eigenvalue of the time reversal operator, allowing it to be a reliable identifying feature. Further investigation into this technique holds promise towards smart wireless power transfer, biomedical, and IoT applications.

1. INTRODUCTION

For detection of multiple scatterers (or targets), utilizing an array-based system can be advantageous as it can provide a complete set of multistatic responses, allowing one to acquire the information necessary for separating the detected scatterers and determining their locations. Our interest here is with the decomposition of the time-reversal operator (DORT), a time-reversal based technique that processes multistatic scattered responses by means of eigendecomposition. With DORT, the detected targets are separated into a set of discrete eigenvalues and their corresponding eigenvectors containing the information related to their locations [1, 2]. Therefore, by feeding the array using the eigenvectors associated with a given eigenvalue, it is possible to selectively transmit waves onto a detected target of interest, either physically for focusing electromagnetic energy at the scatterer or virtually for imaging purposes. For this reason, DORT has been studied for various applications [1–11].

A recent demonstration has shown that DORT can also be applied to detection of passive nonlinear scatterers in the presence of linear scatterers [10, 11]. Nonlinear scatterers refer to electronic devices containing semiconductor junctions which can generate harmonic responses upon excitation. Hence, exploiting the harmonic content in the received signal allows for nonlinear targets to be detected and separated from linear scatters which are considered clutter. Nonlinear detection has been studied for applications such as detection of RF electronics, insect tracking, RFID, temperature sensing, and monitoring of human activities [12–17]. As for DORT applied to nonlinear scatterers, due to its ability to selectively focus electromagnetic energy at a scatterer in addition to detection, it could find applications in wireless power transfer where harmonic responses from passive rectifiers can be exploited

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for detection and subsequent selective focusing (beamforming) to concentrate wireless power at a desired device [10, 11]. Additionally, harmonic detection and selective focusing via DORT may also be used to adaptively send power or information to passive biomedical implants or small sensors for potential IoT applications.

When DORT is applied to nonlinear targets, the eigenvalues appearing in the harmonic bands indicate the presence of nonlinear scatterers in the probed environment. Furthermore, applying pulse inversion (PI) in addition to DORT suppresses the fundamental and odd-ordered harmonics while retaining the even ordered harmonics, thereby rejecting clutter from linear scatterers [11, 18]. PI can be particularly useful when using wideband signals as there may exist some overlap between the harmonic bands. An additional advantage of using PI in a multistatic system is the removal of inter-element coupling which only occurs in the fundamental band, especially at short detection range.

While PI-DORT is effective in detecting nonlinear scatterers and separating them into discrete eigenvalues, discrimination of multiple detected nonlinear scatterers could be challenging. That is, the eigenvalues obtained for two passive nonlinear targets via PI-DORT may look identical in the second harmonic band (even though their eigenvectors differ), rendering it difficult to identify and discriminate one from the other. The ability to identify detected nonlinear targets could be essential for applications where one needs to ensure that the waves are selectively transmitted onto the intended target. An example scenario would be PI-DORT applied to selective wireless power transfer in an environment where multiple passive devices are present, in which case the detected devices must be identified and discriminated from one another to ensure that power is selectively transmitted to the device of interest. In this paper, we propose embedding a unique resonant signature in the second harmonic band for each nonlinear scatterer, such that a distinct resonant notch appears in the eigenvalue of each detected nonlinear scatterer. Therefore, a given nonlinear target can distinctively be identified and discriminated from other detected nonlinear scatterers. The proposed approach is numerically validated by considering various configurations.

2. PI-DORT

A general scenario considered here consists of an environment with multiple scatterers (linear and nonlinear) probed by a multistatic array system (Figure 1). For an N -element array and P individual well-resolved scatterers (negligible multiple scattering between scatterers), the time-domain multistatic responses can be represented with an $N \times N$ matrix $\mathbf{R}(t)$, where each matrix element $r_{i,j}(t)$ represents

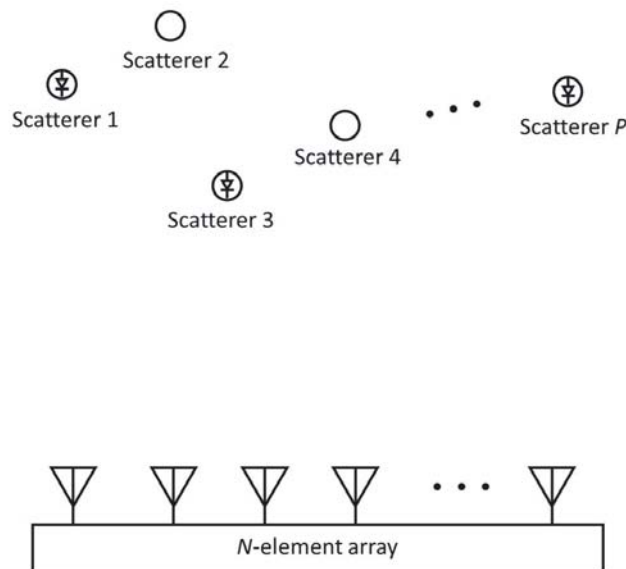


Figure 1. Illustration of a general scenario of multistatic array-based detection of multiple scatterers.

the response between the i th (receive) and j th (transmit) antenna elements. Assuming point scatterers for simplicity of derivation, $r_{i,j}(t)$ is expressed as

$$r_{i,j}(t) = \sum_{p=1}^P q_{p,j}(t) * g_{i,p}(t), \quad (1)$$

where $*$ denotes temporal convolution; $q_{p,j}(t)$ represents the response of the p th scatterer due to a pulse transmitted from the j th antenna; and $g_{i,p}(t)$ represents the Green's function between the p th scatterer and i th antenna element. Here $q_{p,j}(t)$ can be expanded in a power series to account for both linear and nonlinear targets in general, i.e.,

$$q_{p,j}(t) = \sum_{k=1}^{\infty} \alpha_k (f(t) * g_{p,j}(t))^k, \quad (2)$$

where $f(t)$ is the transmit pulse. For nonlinear targets, and α_k is ideally nonzero for all values of k , generating scattered responses in the harmonic bands of $f(t)$. For linear targets, α_k is nonzero only for $k = 1$, thereby producing scattered responses only in the fundamental band of $f(t)$. In Eq. (2), $g_{p,j}(t)$ represents the Green's function between the p th scatterer and j th antenna element.

For detection of nonlinear responses, pulse inversion (PI) can be utilized to suppress fundamental and odd-ordered harmonic responses, while enhancing even-ordered harmonic responses by twofold. PI is particularly useful in the case of a wideband transmit pulse, where there may exist some overlap between the fundamental and harmonic bands, causing a difficulty in extracting the harmonic responses using a filter. Additionally, PI inherently eliminates any coupling between antenna elements which only occurs in the fundamental band and may be a significant problem particularly at short detection range, since they could inundate scattered responses. PI can be applied by separately transmitting two pulses that are opposite in phase (polarity), but otherwise identical, that is, $f^-(t) = -f^+(t)$. As a result, the multistatic responses are obtained as two sets, i.e., $\mathbf{R}^+(t)$ and $\mathbf{R}^-(t)$. By taking the sum of these two sets, we obtain $\mathbf{R}^s(t) = \mathbf{R}^+(t) + \mathbf{R}^-(t)$, and each matrix element in $\mathbf{R}^s(t)$ is expressed as

$$r_{i,j}^s(t) = r_{i,j}^+(t) + r_{i,j}^-(t) = \sum_{p=1}^P \left[\sum_{k=0}^{\infty} 2\alpha_{2(k+1)} (f^+(t) * g_{p,j}(t))^{2(k+1)} \right] * g_{i,p}(t). \quad (3)$$

where only the even-ordered harmonics are retained and enhanced by a factor of two, while the fundamental and odd-ordered harmonics are eliminated.

DORT is then applied to detect and separate targets in terms of discrete eigenvalues. Since the DORT process is done in the frequency domain, the Fourier transform of the multistatic responses, $\mathbf{R}^s(\omega)$, is used. The time-reversal operator (TRO) of $\mathbf{R}^s(\omega)$ is defined as

$$\mathbf{T}(\omega) = \mathbf{R}^{s\dagger}(\omega)\mathbf{R}^s(\omega) \quad (4)$$

where \dagger denotes the conjugate transpose representing time-reversal in the frequency domain. The eigendecomposition of $\mathbf{T}(\omega)$ should yield

$$\mathbf{T}(\omega) = \mathbf{V}(\omega)\mathbf{\Lambda}(\omega)\mathbf{V}^\dagger(\omega), \quad (5)$$

with $\mathbf{\Lambda}(\omega)$ being a diagonal matrix representing the eigenvalues of $\mathbf{T}(\omega)$. Since $\mathbf{T}(\omega)$ is an Hermitian matrix, its eigendecomposition can be done through the singular value decomposition of $\mathbf{R}^{s\dagger}(\omega)$ and $\mathbf{R}^s(\omega)$, that is,

$$\begin{aligned} \mathbf{R}^{s\dagger}(\omega) &= \mathbf{V}(\omega)\mathbf{\Sigma}^\dagger(\omega)\mathbf{U}^\dagger(\omega) \\ \mathbf{R}^s(\omega) &= \mathbf{U}(\omega)\mathbf{\Sigma}(\omega)\mathbf{V}^\dagger(\omega) \end{aligned} \quad (6)$$

where $\mathbf{V}(\omega)$ and $\mathbf{U}(\omega)$ are unitary matrices representing the singular vectors, and $\mathbf{\Sigma}(\omega)$ is a diagonal matrix containing the singular values. Substituting (6) into (4), (5) becomes

$$\mathbf{T}(\omega) = \mathbf{V}(\omega) \left[\mathbf{\Sigma}^\dagger(\omega)\mathbf{\Sigma}(\omega) \right] \mathbf{V}^\dagger(\omega), \quad (7)$$

where $\mathbf{\Lambda}(\omega) = \mathbf{\Sigma}^\dagger(\omega)\mathbf{\Sigma}(\omega)$ and therefore $\lambda_i(\omega) = \sigma_i^2(\omega)$. Since DORT is applied to $\mathbf{R}^s(\omega)$ after PI in this case, $\lambda_i(\omega)$ should in principle only be associated with nonlinear targets with nonzero values only in the even-ordered harmonic bands. Therefore it should be noted that the content of $\lambda_i(\omega)$ is not linearly scalable and should represent the scattered responses of the corresponding nonlinear target for a particular case of transmit pulse (amplitude, pulsewidth and shape). Each column $\mathbf{v}_i(\omega)$ in $\mathbf{V}(\omega)$ contains the eigenvectors of the corresponding eigenvalue, representing the phase conjugated Green's functions between the array elements and the associated scatterer. One can then use $\mathbf{v}_i(\omega)$ to generate a set of signals for selective focusing (or beamforming) to concentrate electromagnetic waves at a desired target. Such a set of signals is expressed as

$$\mathbf{x}_i(\omega) = k\sigma_i(\omega)\mathbf{v}_i(\omega), \quad (8)$$

where k is a scalar constant representing signal amplification. The amplitude and phase of $\mathbf{x}_i(\omega)$ at a particular frequency can be used for phasing the array, or a set of time-domain pulses can be generated by means of the inverse Fourier transform of $\mathbf{x}_i(\omega)$ over a specified bandwidth, i.e.,

$$\mathbf{x}_i(t) = F^{-1} \{k\sigma_i(\omega)\mathbf{v}_i(\omega)\}. \quad (9)$$

As shown above, PI-DORT can separate detected nonlinear scatterers into discrete $\lambda_i(\omega)$ and the corresponding $\mathbf{v}_i(\omega)$ to provide the information regarding the location of each detected nonlinear target to allow selective focusing. However, apart from the target locations, identification and discrimination of one target from another remains a challenge as the spectral shape of $\lambda_i(\omega)$ (or $\sigma_i(\omega)$) would look similar between the targets exhibiting similar passive nonlinear characteristics.

3. EMBEDDED RESONANT NOTCH AS A DISTINGUISHING FEATURE

Here we describe the basic concept of the proposed idea of embedding resonances for nonlinear target discrimination using a circuit model consisting of a simple diode (Figure 2) to represent a passive nonlinear scatterer. It is to be noted that the diode model and circuit parameters used here may not represent an actual nonlinear device used in practice, but are chosen for simplicity of describing the concept without loss of generality. Such a circuit in the figure may roughly represent an antenna terminated with a nonlinear circuit (e.g., rectifier to be used in wireless power transfer applications), where $v_s(t)$ corresponds to the induced voltage at the antenna terminal due to an incident field and R_s corresponds to the antenna impedance. The nonlinear (exponential) relation between the voltage and current across the diode can also be represented by means of power series expansion [19, 20], allowing for $v_o(t)$ from the model to represent the nonlinear scatterer response $q_{p,j}(t)$ in Eq. (2).

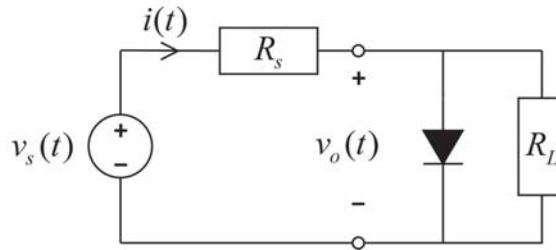


Figure 2. Simple circuit model for a passive nonlinear target.

The circuit model in Figure 2 is simulated to obtain $v_o(t)$ for different amplitude levels of $v_s(t)$, which are arbitrarily chosen to represent a transmit signal incident on three identical passive nonlinear targets at different distances from the antenna array. For the input voltage $v_s(t)$, a Gaussian modulated pulse with a center frequency of 3 GHz and pulsewidth of 1 ns is used. R_s and R_L is arbitrarily chosen as 377Ω . Figures 3(a) and 3(b) show the simulated $v_o(t)$ and its Fourier transform magnitude $|V_o(\omega)|$, respectively, for three different amplitude levels of $v_s(t)$. As shown in Figure 3(a), the amount of rectified voltage in $v_o(t)$ varies due to the difference in the relative signal amplitude with respect to the diode voltage, resulting in different amount of harmonics generate for each case as shown in Figure 3(b). The values that appear in the lower frequency region (below 2 GHz) are due to the “beat” frequencies.

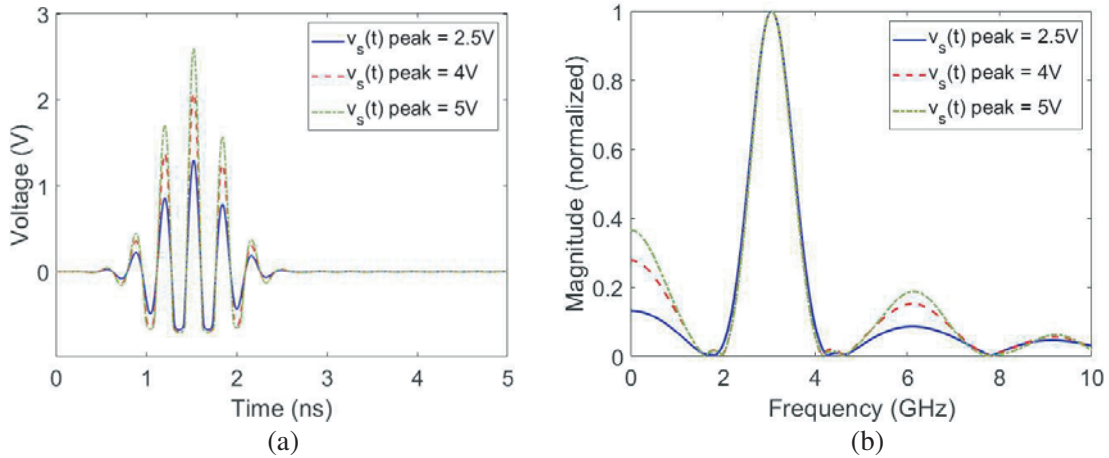


Figure 3. (a) Response $v_o(t)$ and (b) its fourier transform $|V_o(\omega)|$ of the diode circuit model in Figure 2 to various amplitude levels of $v_s(t)$.

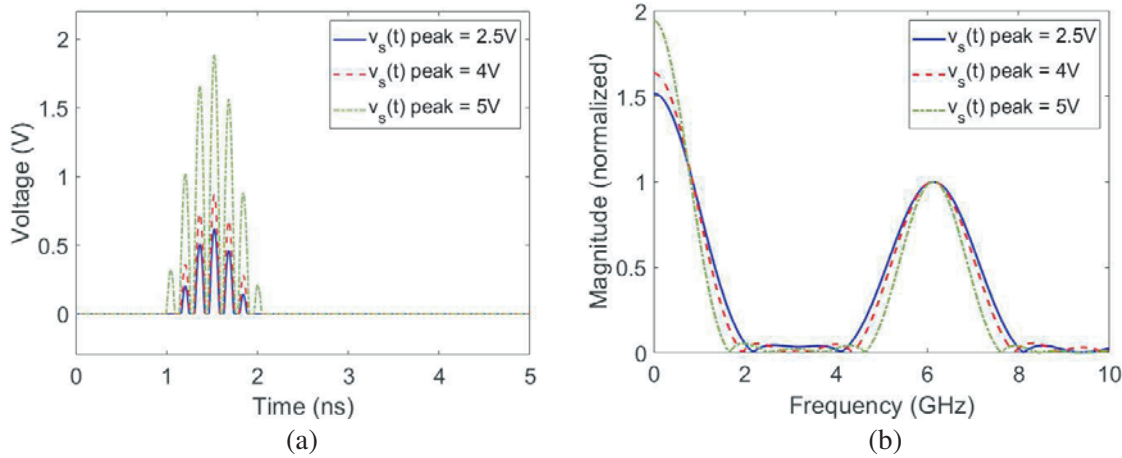


Figure 4. (a) Pulse inversion sum $v_o^s(t) = v_o^+(t) + v_o^-(t)$ and (b) its fourier transform $|V_o^s(\omega)|$ of the diode circuit model in Figure 2 to various amplitude levels of $v_s(t)$.

The amount of harmonics (even-ordered) generated in $v_o(t)$ can be seen more vividly in Figure 4(a), where the pulse inversion sum $v_o^s(t) = v_o^+(t) + v_o^-(t)$ is plotted. Figure 4(b) shows the corresponding $|V_o^s(\omega)|$ with their values normalized to the peak around the second harmonic frequency of 6 GHz for a better comparison. While there is a slight difference in bandwidth due to the difference in effective pulse width as observed in Figure 4(a), the frequency content (shape) of the harmonic responses remain generally the same since the level of rectification primarily determines the amount, not the shape, of harmonics generated. This implies that it would be very difficult to distinguish multiple identical or similar passive nonlinear targets.

Now we embed a resonant notch by adding a pair of LC elements to the same nonlinear circuit from Figure 2, where a parallel LC connection is added in series with the source and the branches containing the diode and load as shown in Figure 5. One way to embed such an LC resonance in a practical nonlinear target (e.g., rectenna) is by integrating split-ring resonator-type structures in the target antenna itself [21–23]. The LC configuration in Figure 5 allows for zero current at resonance, i.e., $I(\omega_o) = 0$ where $\omega_o = 1/\sqrt{LC}$, resulting in $V_o(\omega_o) = 0$ thereby creating a notch in the frequency band. Since the goal here is to embed unique resonant features for nonlinear circuits, the notch frequencies are chosen to be in the second harmonic band of the transmit signal. Figures 6(a) and 6(b), respectively, show $v_o^s(t)$ and the corresponding $|V_o^s(\omega)|$ for the circuit in Figure 5 when the LC element values are

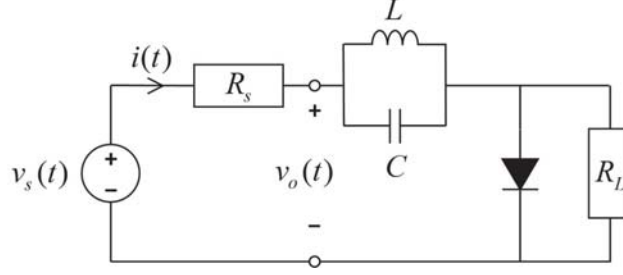


Figure 5. Simple circuit model for a passive nonlinear target with embedded resonant notch.

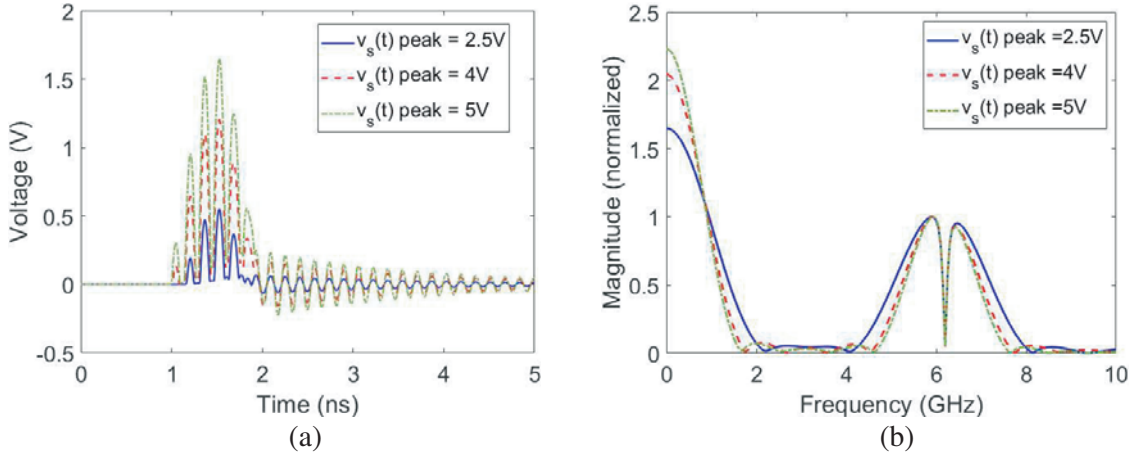


Figure 6. (a) Pulse inversion sum $v_o^s(t)$ and (b) its fourier transform $|V_o^s(\omega)|$ of the diode circuit model in Figure 5 designed to have a notch frequency at 6.15 GHz to various amplitude levels of $v_s(t)$.

chosen to resonate at $f_o = 6.15$ GHz for the three amplitude levels of $v_s(t)$ considered previously. In the time-domain plot (Figure 6(a)), a ringing with the same period is observed for all three cases. In the frequency domain plot (Figure 6(b)), a notch appears at the expected frequency of 6.15 GHz for all three amplitude levels. Since the resonance occurs due to the linear interaction of LC elements, the notch frequency is independent of the amplitude level of $v_s(t)$ and nonlinear rectification process, allowing for the embedded notch to be a reliable distinguishing feature for nonlinear targets regardless of their position or distance from the antenna array.

By assigning different sets of LC element values to circuits (targets) considered, a resonant notch unique to each associated circuit can be generated. Figures 7(a) and 7(b) show, respectively, $v_o^s(t)$ and the corresponding $|V_o^s(\omega)|$ for the circuit in Figure 5 designed for three different notch frequencies, namely $f_1 = 5.7$ GHz, $f_2 = 6.15$ GHz and $f_3 = 6.5$ GHz. The period of the ringing in the responses in Figure 7(a) is different from one another, resulting in different notch positions occurring at the aforementioned resonance frequencies as expected (Figure 7(b)). Due to these uniquely assigned notches, the harmonic responses can now be distinguished from one another with relative ease. It is expected that once each nonlinear scatterer is uniquely assigned with a resonant notch, the corresponding eigenvalue $\lambda_i(\omega)$ obtained via PI-DORT in the second harmonic band can be distinguishable.

4. NUMERICAL SIMULATION

To validate the utility of embedded resonances for nonlinear target discrimination using PI-DORT, a 2D model is created and simulated with SEMCAD X, an FDTD-based electromagnetics solver [24]. With reduced complexity and computation time, a 2D model can provide a qualitative insight into the proposed approach without loss of generality. The model consists of a lossless homogeneous medium (free-space) with 10-element linear array and three scatterers (one linear and two nonlinear) as shown

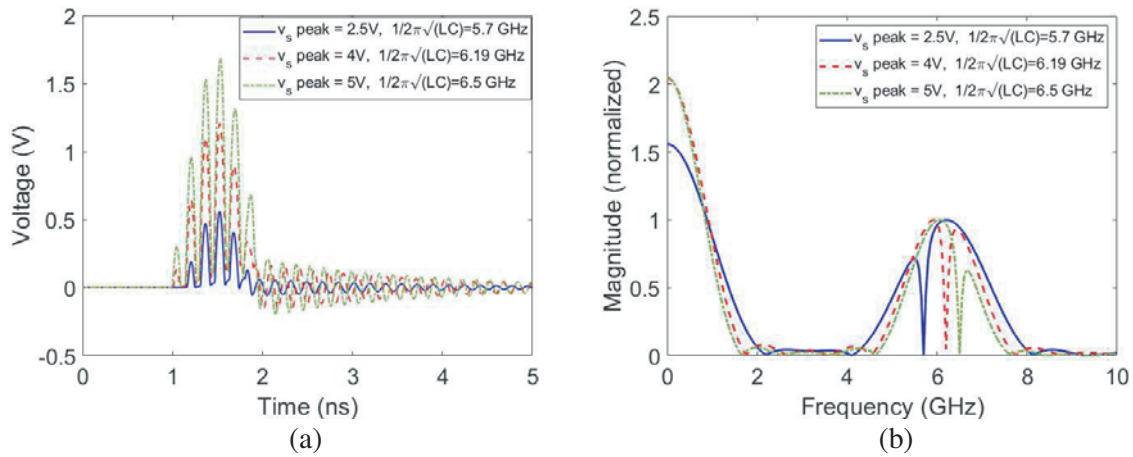


Figure 7. (a) Pulse inversion sum $v_o^s(t)$ and (b) its Fourier transform $|V_o^s(\omega)|$ of the diode circuit model in Figure 5 designed to have a notch frequency at three different frequencies, i.e., 5.7, 6.15 and 6.5 GHz.

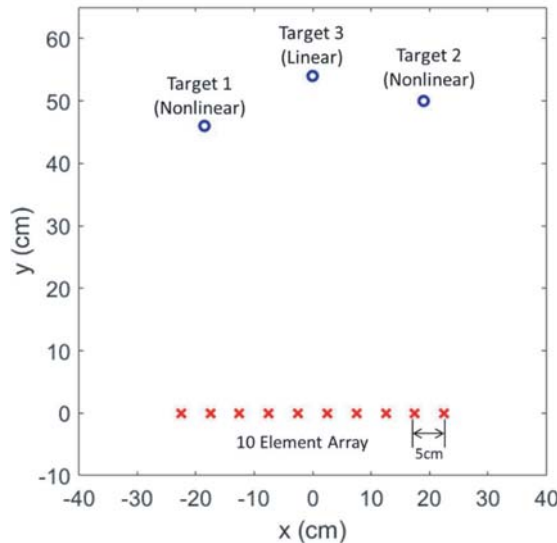


Figure 8. Numerical model used for simulation which consists of a 10-element array and three targets including one linear and two nonlinear targets.

in Figure 8. The elements in the array are modeled as point sources that radiate and receive z -polarized (TM_z) electric fields. The targets are modeled as point scatterers in the EM solver, but linked with a SPICE port so that their responses can be calculated via circuit co-simulation using the models introduced in the previous section. For the transmit signal $f(t)$, a Gaussian modulated pulse with a center frequency of 3 GHz and pulse width of 1 ns is used. The frequency band and dimensions of the model are arbitrarily chosen as the purpose of this paper is to demonstrate the basic feasibility of the concept. The frequency band and dimensions can be scaled depending on the intended application. A few representative target configurations are simulated and the results are discussed below.

The first target configuration is when both nonlinear targets (Target 1 and Target 2) are simple passive nonlinear targets represented with the circuit model from Figure 2. The linear target is modeled as a conducting point target. The simulation is run discretely using $f^+(t)$ and $f^-(t)$ in order to perform PI to obtain $\mathbf{R}^{st}(\omega)$. In Figure 9, the first four singular values of $\mathbf{R}^{st}(\omega)$ are plotted. Since $\mathbf{R}^{st}(\omega)$ is the pulse inversion sum of the multistatic responses, the singular values appear only in

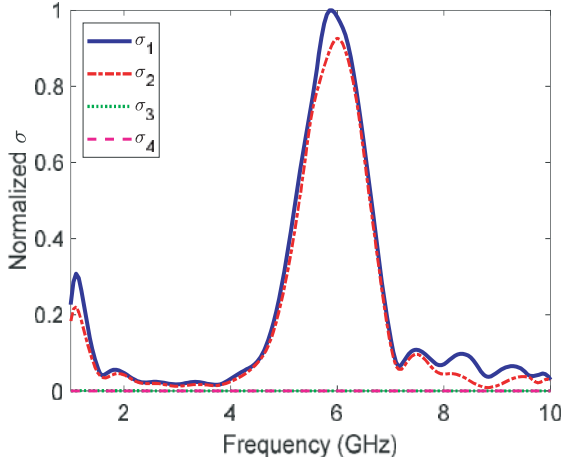


Figure 9. Singular values obtained from $\mathbf{R}^{s\dagger}(\omega)$ of two simple passive nonlinear targets and one linear target.

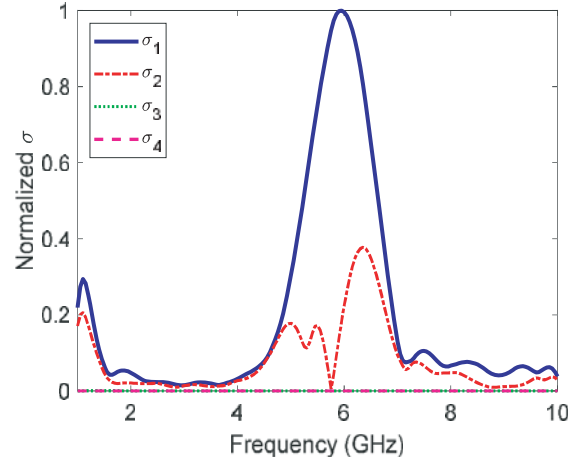


Figure 10. Singular values obtained from $\mathbf{R}^{s\dagger}(\omega)$ of one simple passive nonlinear target, one notch-embedded nonlinear target and one linear target.

the second harmonic band (around 6 GHz), which means that the responses from Target 3 (linear target) in the fundamental band is suppressed, allowing for detection of nonlinear targets only. As a result, there are only two significant singular values in the plot, namely $\sigma_1(\omega)$ and $\sigma_2(\omega)$, respectively associated with Target 1 and Target 2. It is also observed that $\sigma_1(\omega)$ and $\sigma_2(\omega)$ are nearly identical in shape as expected. This configuration may represent the case where all nonlinear targets in the probed environment are “unknown” with similar characteristics. One can still use the corresponding eigenvectors $\mathbf{v}_i(\omega)$ to generate signals for selective focusing on either of the two targets, but without identifying and distinguishing them.

The second target configuration consists of Target 1 as a simple passive nonlinear target (circuit model from Figure 2), Target 2 as a notch-embedded nonlinear target (circuit model from Figure 5), and Target 3 as a conducting linear target. The target locations remain the same as in Figure 8. For Target 2, the LC elements are designed to resonate at 5.7 GHz. In Figure 10, the first four singular

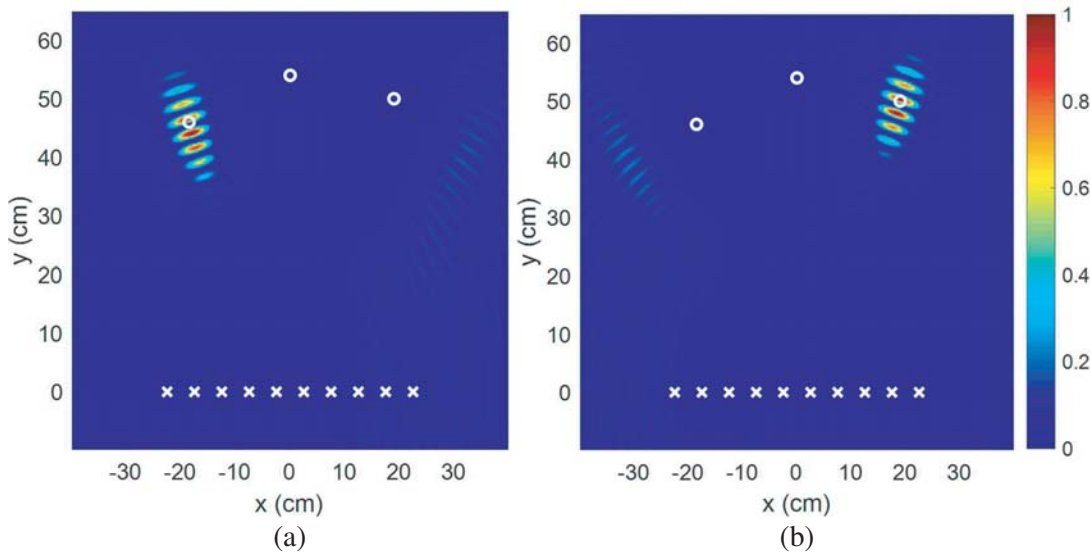


Figure 11. Spatial plots of the electric field (power level) resulting from: (a) transmitting $\mathbf{x}_1(t)$ and (b) transmitting $\mathbf{x}_2(t)$, for the case of one simple passive nonlinear target, one notch-embedded nonlinear target and one linear target.

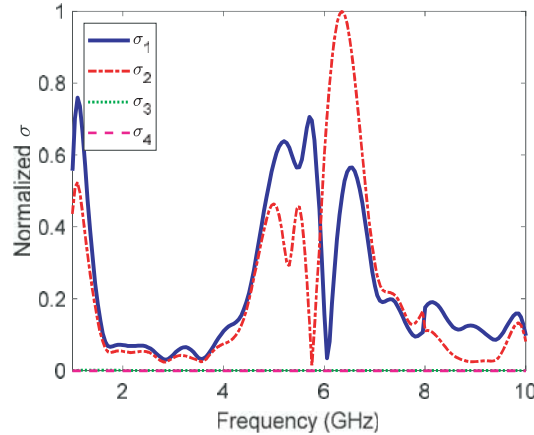


Figure 12. Singular values obtained from $\mathbf{R}^{s\dagger}(\omega)$ of one simple passive nonlinear targets, one notch-embedded nonlinear target and one linear target.

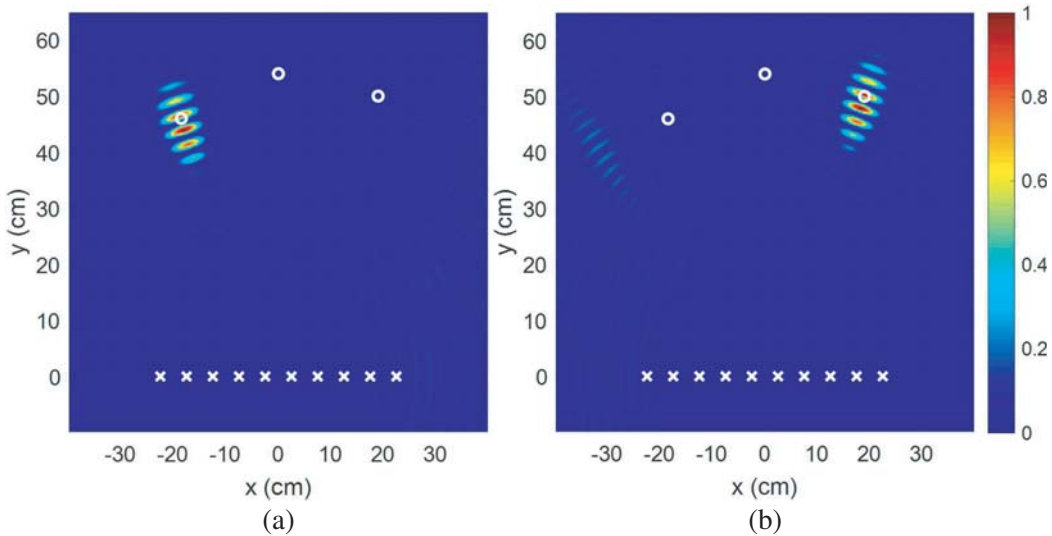


Figure 13. Spatial plots of the electric field (power level) resulting from: (a) transmitting $\mathbf{x}_1(t)$ and (b) transmitting $\mathbf{x}_2(t)$, for the case of two notch-embedded nonlinear targets and one linear target.

values of $\mathbf{R}^{s\dagger}(\omega)$ are plotted. Just as in the previous case, only two significant singular values associated with Target 1 and Target 2 are observed in the plot as a result of PI. However, in this case the shape of $\sigma_2(\omega)$ is distinctively different from that of $\sigma_1(\omega)$, with a frequency notch observed at the expected frequency of 5.7 GHz, allowing identification of Target 2 and discriminating it from Target 1. Note that the values of $\sigma_2(\omega)$ are generally smaller than that of $\sigma_1(\omega)$, since the notch occurs near the peak frequency. Nevertheless, it does not affect the shape of the singular values, and therefore identification of Target 2. This configuration may represent the case of a notch-embedded nonlinear target in the presence of an unknown nonlinear target. Selective focusing can then be done by generating $\mathbf{x}_2(t)$ for Target 2, which is now “identified”. Figure 11(b) shows the spatial distribution of the electric fields (in power level, i.e., $|E_z|^2$) radiated by feeding $\mathbf{x}_2(t)$ into the array, at a time instance where the wave focusing occurs at Target 2. Figure 11(a) shows the spatial distribution of the electric fields (power level) radiated by feeding $\mathbf{x}_1(t)$ into the array, where it shows that wave focusing is still possible for “unknown” Target 1.

The third target configuration includes both Target 1 and Target 2 as notch-embedded nonlinear targets (circuit model from Figure 5) but with different notch-frequencies, and Target 3 as a conducting

point target. The target locations remain the same as in Figure 8. For Target 1 and Target 2 the LC elements are designed to resonate respectively at 6.1 GHz and 5.7 GHz. In Figure 12, the first four singular values of $\mathbf{R}^{s\ddagger}(\omega)$ are plotted. As expected, only two significant singular values associated with Target 1 and Target 2 are observed in the plot as a result of PI. A frequency notch occurs in each of the singular values, i.e., at 6.1 GHz for $\sigma_1(\omega)$ and at 5.7 GHz for $\sigma_2(\omega)$, which identifies $\sigma_1(\omega)$ to be associated with Target 1 and $\sigma_2(\omega)$ associated Target 2, thereby discriminating one from the other. This configuration may represent the case where all nonlinear targets in the environment are notch-embedded and identifiable. Selective focusing on either of these identified targets can be done by generating $\mathbf{x}_1(t)$ or $\mathbf{x}_2(t)$ and feeding them into the array. Figures 13(a) and 13(b) show the spatial distribution of the electric fields (power level) radiated by feeding $\mathbf{x}_1(t)$ and $\mathbf{x}_2(t)$, respectively, at a time instance where the wave focusing occurs at the intended targets.

5. DISCUSSION

The results from the numerical models considered above show that a resonant notch embedded in a nonlinear target does consistently appear in the associated eigenvalue (singular values) from PI-DORT, validating the basic feasibility of the proposed approach of embedding unique resonances as an effective distinguishing feature for identifying multiple nonlinear targets from one another. Further investigation should then involve experimental validation to demonstrate the practical utility of the concept. The following are some important practical aspects that must be addressed:

1) *Real antennas used in the array as opposed to point sources:* Antenna elements must be designed to have ultra-wide bandwidth, so as to cover both fundamental and second harmonic bands. Moreover, antenna design must be carefully chosen that is free of any unwanted frequency characteristics (i.e., frequency notches or significant ripples), especially in the second harmonics band, which may cause confusion in discerning the frequency response from nonlinear targets. Once the antennas are configured into an array, the elements must be sufficiently spaced to work properly in the second harmonic band without grating lobes. The previous experimental work on PI-DORT reported in [11] validates the importance of antenna element design and element spacing.

2) *Required transmit power for exciting harmonic responses from nonlinear targets:* In order to excite harmonic responses from a nonlinear target, the incident power at target must be high enough to cause nonlinear behavior at the nonlinear junction. Therefore, in order to ensure detection of harmonic responses from nonlinear targets at a given range, one needs to make sure to use sufficient transmit power. Performing a calculation using the nonlinear radar equation [15] could help determine the appropriate transmit power level to ensure detection of nonlinear targets at a given maximum detection range.

3) *Extended targets as opposed to point targets:* Practical nonlinear targets have physical extent, which may affect the spectral shape of the frequency response, and also generate additional eigenvalues due to higher modes introduced in the target [11]. How such phenomena affect the resonant notches in the spectrum of the eigenvalues must be evaluated.

4) *Multiple scattering due to targets not well-resolved:* Closely spaced targets may cause non-negligible multiple scattering that results in additional eigenvalues, which could limit the performance of DORT. An investigation into the effects of nonlinear target spacing on the ability to distinguish them using embedded resonances may be necessary, in order to determine the limitations of the DORT-based approach and find potential ways to overcoming them.

6. CONCLUSION

A method of distinguishing multiple passive nonlinear targets is proposed for DORT-based nonlinear target detection and selective wave focusing, by embedding a resonant notch unique to each nonlinear scatterer. We numerically validate that a uniquely embedded resonant notch in a nonlinear target consistently appears in the corresponding eigenvalue of the TRO, allowing it to be a reliable distinct feature for the given target. Therefore, the detected nonlinear targets can be identified and discriminated before selective focusing. Further investigation into this technique holds promise towards smart wireless power transfer, biomedical, and IoT applications.

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