

# Tuned Y-Shaped Electromagnetic Switch for Directional Signal Control in Photonic Circuits

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**ABSTRACT:** In this study, we present a Y-shaped electromagnetic waveguide switch with integrated resonators designed to control wave propagation within a specific frequency range. The switch comprises two input lines and one output line, with each input line connected to a resonator of height  $d_1$  and  $d_3$  that can either allow or block transmission of the signal. Using the Transfer Matrix Method (TMM), we determined transmission and reflection properties to analyze the device's performance in ON (transmission) and OFF (blocking) states. Our results indicate that, depending on the choice of geometric and structural parameters, the resonators enable a transmission of more than 99% ( $T_{13}$ ) from the first input line to the output line in the ON state, while reducing the transmission from the second input line to less than 1% ( $T_{23}$ ) in the OFF state. These findings show the importance of resonator tuning for achieving precise electromagnetic wave control, offering a practical approach for enhancing signal management in advanced optical communication systems.

## 1. INTRODUCTION

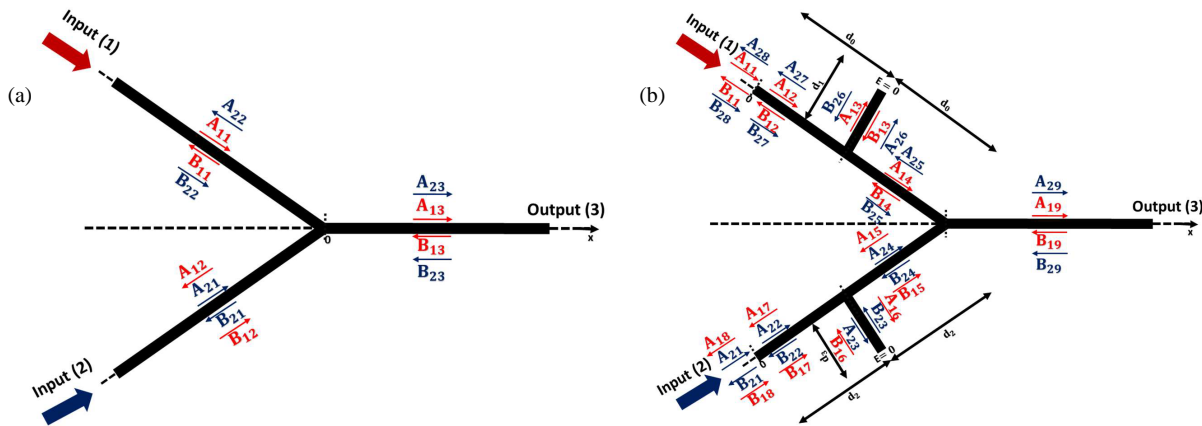
Electromagnetic waveguide switches are critical components in advanced signal processing and telecommunication systems, enabling dynamic control over the propagation of electromagnetic waves by adjusting signal direction and intensity within confined structures [1–6]. These switches are integral to modern optical communication networks and integrated photonic circuits, where they significantly improve sensing capabilities [7–10]. Their versatility and performance have been frequently in extensive use in data centers for high-speed data routing, in reconfigurable antennas to achieve flexible signal direction control and in optical computing platforms to support rapid signal processing and related operations [11, 12]. Such general uses improve the importance of electromagnetic waveguide switches in high-performance communication and processing environments.

In addition to their contributions to communication networks, electromagnetic waveguide switches are essential for imaging and environmental sensing applications. By precisely manipulating electromagnetic fields, these switches have the potential to enhance image clarity, facilitate detailed environmental analysis, and allow the detection of signal variations critical for both research and monitoring [4, 13–16]. Thus, there has been a great deal of research into new switch designs that ensure high efficiency, solid performance, flexibility, and simple integration with current platforms in response to growing demands for faster, more flexible communication systems.

Numerous approaches have been explored to satisfy these changing requirements. For example, Dao et al. [17] presented a compact  $2 \times 2$  photonic switch consisting of a waveguide with a phase-change material ( $\text{Sb}_2\text{Se}_3$ ) for switching. This system efficiently connects two inputs to two outputs, facilitating low-loss signal routing. Rehman et al. [18] introduced a three-dimensional switch based on guided mode resonances in photonic crystals, achieving a significant 13.75% data signal enhancement at a wavelength of  $1.55 \mu\text{m}$ . Similarly, Rehman et al. [19] employed crystal cavity methods to improve switching efficiency by approximately 7%. In addition, Hu et al. [1] exploited Fano resonance phenomena to realize high modulation intensity terahertz switches, making the way for future high speed communication systems.

In this study, we investigate a Y-shaped electromagnetic waveguide switch composed of two input channels and one output channel, integrating resonators to ensure precise directional control of electromagnetic waves to achieve the switch phenomenon. Using transfer matrix method (TMM), we calculate transmission and reflection rates, enabling a thorough analysis of the switch's ON and OFF states. Subsequently, we examine the influence of resonator parameters on switching performance and identify optimal configurations for distinct transmission states. We conclude by summarizing our main findings and discussing their potential applications in optical communication and photonics.

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**FIGURE 1.** (a) Y-shaped electromagnetic switch without resonator. (b) Y-shaped electromagnetic switch with two resonators of height  $d_1$  and  $d_3$  grafted into the first and second input lines respectively.

## 2. THEORETICAL FORMALISM

The transfer matrix method (TMM) is commonly used to study waveguides and to analyze properties such as reflection and transmission rates. This approach considers the evolution of the electromagnetic field as it passes through different sections of the waveguide, while ensuring consistency with the boundary conditions at each interface. This method is particularly useful for electromagnetic waveguide systems and can be used in a variety of fields, such as electronics and acoustics [20–26].

In Fig. 1(a), we examine a structure composed of two inputs and one output channels composed of waveguides. In Fig. 1(b), we illustrate a structure comprising two input channels and one output line. The first input includes two segments of lengths  $d_0$ , connected by a resonator of height  $d_1$ . The second input consists of two segments of lengths  $d_2$ , grafted at their middle by one resonator of height  $d_3$ . In this study, we use Transfer Matrix Method (TMM) to analyze electromagnetic wave propagation in a one-dimensional waveguide system Y-shaped electromagnetic switch (Fig. 1).

### 2.1. Analysis of Transmission and Reflection Rates in an Electromagnetic Switch without Resonator

In this section, we calculate the transfer matrix for a Y-shaped system electromagnetic switch without resonator (Fig. 1(a)). The expressions for the electric fields in the three regions of the system are as follows:

$$E(x) = \begin{cases} E_{11}(x) = A_{11}e^{j\alpha_0 x} + B_{11}e^{-j\alpha_0 x} & \text{for: } x \leq 0 \\ E_{12}(x) = A_{12}e^{j\alpha_1 x} + B_{12}e^{-j\alpha_1 x} & \text{for: } x \leq 0 \\ E_{13}(x) = A_{13}e^{j\alpha_2 x} + B_{13}e^{-j\alpha_2 x} & \text{for: } x \geq 0 \\ E_{21}(x) = A_{21}e^{j\alpha_1 x} + B_{21}e^{-j\alpha_1 x} & \text{for: } x \leq 0 \\ E_{22}(x) = A_{22}e^{j\alpha_0 x} + B_{22}e^{-j\alpha_0 x} & \text{for: } x \leq 0 \\ E_{23}(x) = A_{23}e^{j\alpha_2 x} + B_{23}e^{-j\alpha_2 x} & \text{for: } x \geq 0 \end{cases} \quad (1)$$

The electric field within each medium is expressed as the sum of an incident wave and a reflected wave. The amplitudes  $A_{1i}, B_{1i}, A_{2i}, B_{2i}$  (for  $i = [1-3]$ ) represent the amplitudes of the progressive and regressive electromagnetic waves.

We define  $\alpha_i = \frac{\omega}{c} \sqrt{\epsilon_i \mu_i}$ , for  $i = [0, 2]$  where  $\omega$  is the angular frequency of the incoming electromagnetic wave,  $\epsilon_i$  the relative permittivity,  $\mu_i$  the permeability of the non-magnetic medium, and  $c$  the speed of electromagnetic waves in a vacuum.

The conditions of passage in  $x = 0$  are:

$$\begin{cases} E_{11}(x=0) = E_{12}(x=0) = E_{13}(x=0) \\ \frac{dE_{11}}{dx}(x=0) = \frac{dE_{12}}{dx}(x=0) + \frac{dE_{13}}{dx}(x=0) \\ E_{21}(x=0) = E_{22}(x=0) = E_{23}(x=0) \\ \frac{dE_{21}}{dx}(x=0) = \frac{dE_{22}}{dx}(x=0) + \frac{dE_{23}}{dx}(x=0) \end{cases} \quad (2)$$

By applying the calculations described in system (2), we obtain the following results:

$$\begin{pmatrix} A_{11} \\ B_{11} \end{pmatrix} = \begin{pmatrix} \frac{\alpha_0 + \alpha_1}{2\alpha_0} & \frac{\alpha_0 - \alpha_1}{2\alpha_0} & \frac{\alpha_2}{2\alpha_0} & \frac{-\alpha_2}{2\alpha_0} \\ \frac{\alpha_0 - \alpha_1}{2\alpha_0} & \frac{\alpha_0 + \alpha_1}{2\alpha_0} & \frac{-\alpha_2}{2\alpha_0} & \frac{\alpha_2}{2\alpha_0} \end{pmatrix} \begin{pmatrix} A_{12} \\ B_{12} \\ A_{13} \\ B_{13} \end{pmatrix} \quad (3)$$

The matrix:  $T_1 = \begin{pmatrix} \frac{\alpha_0 + \alpha_1}{2\alpha_0} & \frac{\alpha_0 - \alpha_1}{2\alpha_0} & \frac{\alpha_2}{2\alpha_0} & \frac{-\alpha_2}{2\alpha_0} \\ \frac{\alpha_0 - \alpha_1}{2\alpha_0} & \frac{\alpha_0 + \alpha_1}{2\alpha_0} & \frac{-\alpha_2}{2\alpha_0} & \frac{\alpha_2}{2\alpha_0} \end{pmatrix}$  defines the connections between the input amplitudes  $A_{11}$  and  $B_{11}$  from the first input line and the output amplitudes  $A_{12}, B_{12}, A_{13}$  and  $B_{13}$  within our electromagnetic switching system.

To simplify, we represent the matrix  $T_1$  using a notation:

$$T_1 = \begin{pmatrix} Y_{11} & Y_{12} & Y_{13} & Y_{14} \\ Y_{15} & Y_{16} & Y_{17} & Y_{18} \end{pmatrix} \quad (4)$$

Then,

$$\begin{pmatrix} A_{21} \\ B_{21} \end{pmatrix} = \begin{pmatrix} \frac{\alpha_1 + \alpha_0}{2\alpha_1} & \frac{\alpha_1 - \alpha_0}{2\alpha_1} & \frac{\alpha_2}{2\alpha_1} & \frac{-\alpha_2}{2\alpha_1} \\ \frac{\alpha_1 - \alpha_0}{2\alpha_1} & \frac{\alpha_1 + \alpha_0}{2\alpha_1} & \frac{-\alpha_2}{2\alpha_1} & \frac{\alpha_2}{2\alpha_1} \end{pmatrix} \begin{pmatrix} A_{22} \\ B_{22} \\ A_{23} \\ B_{23} \end{pmatrix} \quad (5)$$

The matrix:  $T_2 = \begin{pmatrix} \frac{\alpha_1 + \alpha_0}{2\alpha_1} & \frac{\alpha_1 - \alpha_0}{2\alpha_1} & \frac{\alpha_2}{2\alpha_1} & \frac{-\alpha_2}{2\alpha_1} \\ \frac{\alpha_1 - \alpha_0}{2\alpha_1} & \frac{\alpha_1 + \alpha_0}{2\alpha_1} & \frac{-\alpha_2}{2\alpha_1} & \frac{\alpha_2}{2\alpha_1} \end{pmatrix}$  defines

the connections between the input amplitudes  $A_{21}$  and  $B_{21}$  the second input line and the output amplitudes  $A_{22}$ ,  $B_{22}$ ,  $A_{23}$  and  $B_{23}$  within our electromagnetic switching system.

To simplify, we represent the matrix  $T_2$  using a notation:

$$T_2 = \begin{pmatrix} Y_{21} & Y_{22} & Y_{23} & Y_{24} \\ Y_{25} & Y_{26} & Y_{27} & Y_{28} \end{pmatrix} \quad (6)$$

Using formulations (3) and (5), we obtain the following form of the global matrix for our proposed system without resonator:

$$\begin{pmatrix} A_{11} \\ B_{11} \\ A_{21} \\ B_{21} \end{pmatrix} = T_{S_1} \begin{pmatrix} A_{12} \\ B_{12} \\ A_{13} \\ B_{13} \\ A_{22} \\ B_{22} \\ A_{23} \\ B_{23} \end{pmatrix} \quad (7)$$

$$\text{With } T_{S_1} = \begin{pmatrix} a_{11} & a_{12} & a_{13} & a_{14} & a_{15} & a_{16} & a_{17} & a_{18} \\ a_{21} & a_{22} & a_{23} & a_{24} & a_{25} & a_{26} & a_{27} & a_{28} \\ a_{31} & a_{32} & a_{33} & a_{34} & a_{35} & a_{36} & a_{37} & a_{38} \\ a_{41} & a_{42} & a_{43} & a_{44} & a_{45} & a_{46} & a_{47} & a_{48} \end{pmatrix}.$$

The transmission and reflection coefficients are represented by the following formulas:

$$\left\{ \begin{array}{l} t_{12} = \frac{A_{12}}{A_{11}} \Big|_{B_{12}=0} = \frac{1}{a_{11}+a_{13}} \\ B_{13}=0 \\ B_{21}=0 \\ B_{23}=0 \\ t_{13} = \frac{A_{13}}{A_{11}} \Big|_{B_{12}=0} = \frac{1}{a_{11}+a_{13}} \\ B_{13}=0 \\ B_{21}=0 \\ B_{23}=0 \\ r_{11} = \frac{B_{11}}{A_{11}} \Big|_{B_{12}=0} = \frac{a_{21}+a_{23}}{a_{11}+a_{13}} \\ B_{13}=0 \\ B_{21}=0 \\ B_{23}=0 \\ t_{21} = \frac{A_{22}}{A_{21}} \Big|_{B_{12}=0} = \frac{1}{a_{35}+a_{37}} \\ B_{13}=0 \\ B_{21}=0 \\ B_{23}=0 \\ t_{23} = \frac{A_{23}}{A_{21}} \Big|_{B_{12}=0} = \frac{1}{a_{35}+a_{37}} \\ B_{13}=0 \\ B_{21}=0 \\ B_{23}=0 \\ r_{22} = \frac{B_{21}}{A_{21}} \Big|_{B_{12}=0} = \frac{a_{45}+a_{47}}{a_{35}+a_{37}} \\ B_{13}=0 \\ B_{21}=0 \\ B_{23}=0 \end{array} \right. \quad (8)$$

where:

- $t_{12}$ : transmission from input channel 1 through input channel 2.
- $t_{13}$ : transmission from input channel 1 through output channel.
- $r_{11}$ : reflection from input channel 1.
- $t_{21}$ : transmission from input channel 2 through input channel 1.
- $t_{23}$ : transmission from input channel 2 through output channel.
- $r_{22}$ : reflection from input channel 2.

The transmission and reflection rates are expressed as follows:

$$\left\{ \begin{array}{l} T_{12} = |t_{12}|^2 = \left| \frac{1}{a_{11}+a_{13}} \right|^2 \\ T_{13} = |t_{13}|^2 = \left| \frac{1}{a_{11}+a_{13}} \right|^2 \\ R_{11} = |r_{11}|^2 = \left| \frac{a_{21}+a_{23}}{a_{11}+a_{13}} \right|^2 \\ T_{21} = |t_{21}|^2 = \left| \frac{1}{a_{35}+a_{37}} \right|^2 \\ T_{23} = |t_{23}|^2 = \left| \frac{1}{a_{35}+a_{37}} \right|^2 \\ R_{22} = |r_{22}|^2 = \left| \frac{a_{45}+a_{47}}{a_{35}+a_{37}} \right|^2 \end{array} \right. \quad (9)$$

## 2.2. Analysis of Transmission and Reflection Rates in an Electromagnetic Switch with a Resonator on Each Input Channel

In this section, we calculate the transfer matrix for a Y-shaped electromagnetic switch with a resonator on each input line (Fig. 1(b)). The expressions for the electric fields are presented in

$$E(x, y) = \left\{ \begin{array}{l} E_{11}(x) = A_{11}e^{j\alpha_0 x} + B_{11}e^{-j\alpha_0 x} \\ E_{12}(x) = A_{12}e^{j\alpha_1 x} + B_{11}e^{-j\alpha_1 x} \\ E_{13}(y) = A_{13}e^{j\alpha_2 y} + B_{13}e^{-j\alpha_2 y} \\ E_{14}(x) = A_{14}e^{j\alpha_3 x} + B_{14}e^{-j\alpha_3 x} \\ E_{15}(x) = A_{15}e^{j\alpha_4 x} + B_{15}e^{-j\alpha_4 x} \\ E_{16}(y) = A_{16}e^{j\alpha_5 y} + B_{16}e^{-j\alpha_5 y} \\ E_{17}(x) = A_{17}e^{j\alpha_6 x} + B_{17}e^{-j\alpha_6 x} \\ E_{18}(x) = A_{18}e^{j\alpha_7 x} + B_{18}e^{-j\alpha_7 x} \\ E_{19}(x) = A_{19}e^{j\alpha_8 x} + B_{19}e^{-j\alpha_8 x} \\ E_{21}(x) = A_{21}e^{j\alpha_7 x} + B_{21}e^{-j\alpha_7 x} \\ E_{22}(x) = A_{22}e^{j\alpha_6 x} + B_{22}e^{-j\alpha_6 x} \\ E_{23}(y) = A_{23}e^{j\alpha_5 y} + B_{23}e^{-j\alpha_5 y} \\ E_{24}(x) = A_{24}e^{j\alpha_4 x} + B_{24}e^{-j\alpha_4 x} \\ E_{25}(x) = A_{25}e^{j\alpha_3 x} + B_{35}e^{-j\alpha_3 x} \\ E_{26}(y) = A_{26}e^{j\alpha_2 y} + B_{26}e^{-j\alpha_2 y} \\ E_{27}(x) = A_{27}e^{j\alpha_1 x} + B_{27}e^{-j\alpha_1 x} \\ E_{28}(x) = A_{28}e^{j\alpha_0 x} + B_{28}e^{-j\alpha_0 x} \end{array} \right. \quad (10)$$

Within each medium, the electric field is expressed as the sum of an incident wave and a reflected wave. The amplitudes  $A_{1i}$ ,  $B_{1i}$ ,  $A_{2i}$ ,  $B_{2i}$  (for  $i = 1, 8$ ) represent the amplitudes of the

progressive and regressive electromagnetic waves. The propagation constant  $\alpha_i$  is defined as:

$$\alpha_i = \frac{\omega}{c} \sqrt{\varepsilon_i \mu_i} \quad \text{for } i = 0, \dots, 8 \quad (11)$$

where:

- $\omega$  is the angular frequency of the incoming electromagnetic wave
- $\varepsilon_i$  is the relative permittivity
- $\mu_i$  is the permeability of the non-magnetic medium
- $c$  is the speed of electromagnetic waves in a vacuum

For our calculations, we assume a dielectric permittivity of ( $\varepsilon = 2.3$ ) (polyethylene) and a non-magnetic medium permeability of ( $\mu = 1$ ). These parameters are applied to the segments and resonators that constitute the electromagnetic switch.

To calculate the transfer matrix of our system, we will first determinate the transfer matrix from the first input line to output line. Next, we calculate the transfer matrix from the second input line to output line. This approach allows us to analyze each input channel independently, then combine them to obtain a complete global understanding of the system's behavior.

The transfer matrix for a segment  $T_{G_x}$  is defined as:

$$T_{G_x} = \begin{pmatrix} \cos(\alpha d_x) & \frac{-j \sin(\alpha d_x)}{\alpha} \\ -j\alpha \sin(\alpha d_x) & \cos(\alpha d_x) \end{pmatrix} \quad (12)$$

where:

- $\alpha = \frac{\omega}{c} \sqrt{\varepsilon \mu}$  is the propagation constant
- $d_x$  is the length of the segment
- $j = \sqrt{-1}$  is the imaginary unit

For a combination of a segment and a resonator, the transfer matrix  $T_{G_x R_y}$  is given by:

$$T_{G_x R_y} =$$

$$\begin{pmatrix} \cos(\alpha d_x) + \sin(\alpha d_x) \tan(\alpha d_y) & \frac{-j \sin(\alpha d_x)}{\alpha} \\ -j\alpha \sin(\alpha d_x) + j\alpha \cos(\alpha d_x) \tan(\alpha d_y) & \cos(\alpha d_x) \end{pmatrix} \quad (13)$$

where  $d_y$  is the height of the resonator.

The derivation of the transfert matrix elements in Eq. (13) was provided by Touiss et al. [25].

To calculate the transfer matrix from the first input line to the output line, which relates the first input amplitudes to the output amplitudes, we proceed as follows:

Initially, the transfer matrix  $T_{G_0 R_1} T_{G_0}$  relates the amplitudes  $A_{14}$  and  $B_{14}$  to  $A_{11}$  and  $B_{11}$ :

$$\begin{pmatrix} A_{11} \\ B_{11} \end{pmatrix} = T_{G_0 R_1} T_{G_0} \begin{pmatrix} A_{14} \\ B_{14} \end{pmatrix}$$

Subsequently, the amplitudes  $A_{14}$  and  $B_{14}$  are connected to  $A_{15}$ ,  $B_{15}$ ,  $A_{19}$ , and  $B_{19}$  using the transfer matrix derived for the electromagnetic switch without resonators. This transfer

matrix effectively links the input amplitudes of the first line to output amplitudes:

$$\begin{pmatrix} A_{14} \\ B_{14} \end{pmatrix} = \begin{pmatrix} G_{11} & G_{12} & G_{13} & G_{14} \\ G_{15} & G_{16} & G_{17} & G_{18} \end{pmatrix} \begin{pmatrix} A_{15} \\ B_{15} \\ A_{19} \\ B_{19} \end{pmatrix}$$

The amplitudes  $A_{15}$  and  $B_{15}$  are related to the output amplitudes  $A_{18}$  and  $B_{18}$  via the transfer matrix  $T_{G_2 R_3} T_{G_2}$ :

$$\begin{pmatrix} A_{15} \\ B_{15} \end{pmatrix} = T_{G_2 R_3} T_{G_2} \begin{pmatrix} A_{18} \\ B_{18} \end{pmatrix}$$

By substituting the expression of  $\begin{pmatrix} A_{15} \\ B_{15} \end{pmatrix}$  into the transfer matrix, we obtain:

$$\begin{pmatrix} A_{14} \\ B_{14} \end{pmatrix} = \begin{pmatrix} G_{11} & G_{12} \\ G_{15} & G_{16} \end{pmatrix} T_{G_2 R_3} T_{G_2} \begin{pmatrix} A_{18} \\ B_{18} \end{pmatrix} + \begin{pmatrix} G_{13} & G_{14} \\ G_{17} & G_{18} \end{pmatrix} \begin{pmatrix} A_{19} \\ B_{19} \end{pmatrix}$$

Similarly, substituting the expression just obtained for  $\begin{pmatrix} A_{14} \\ B_{14} \end{pmatrix}$  back into the initial transfer equation

$$\begin{pmatrix} A_{11} \\ B_{11} \end{pmatrix} = T_{G_0 R_1} T_{G_0} \begin{pmatrix} A_{14} \\ B_{14} \end{pmatrix}:$$

$$\begin{pmatrix} A_{11} \\ B_{11} \end{pmatrix} = T_{G_0 R_1} T_{G_0} \left[ \begin{pmatrix} G_{11} & G_{12} \\ G_{15} & G_{16} \end{pmatrix} T_{G_2 R_3} T_{G_2} \begin{pmatrix} A_{18} \\ B_{18} \end{pmatrix} + \begin{pmatrix} G_{13} & G_{14} \\ G_{17} & G_{18} \end{pmatrix} \begin{pmatrix} A_{19} \\ B_{19} \end{pmatrix} \right]$$

Through matrix multiplication, the overall transfer matrix connecting the input amplitudes  $A_{11}$  and  $B_{11}$  from the first input line to the output amplitudes  $A_{18}$ ,  $B_{18}$ ,  $A_{19}$ , and  $B_{19}$  is obtained as:

$$\begin{pmatrix} A_{11} \\ B_{11} \end{pmatrix} = \begin{pmatrix} H_{11} & H_{12} & H_{13} & H_{14} \\ H_{15} & H_{16} & H_{17} & H_{18} \end{pmatrix} \begin{pmatrix} A_{18} \\ B_{18} \\ A_{19} \\ B_{19} \end{pmatrix} \quad (14)$$

Here, the matrix  $T_3 = \begin{pmatrix} H_{11} & H_{12} & H_{13} & H_{14} \\ H_{15} & H_{16} & H_{17} & H_{18} \end{pmatrix}$  represents the elements of the transfer matrix that connect the input amplitudes from the first input line to the output amplitudes in our electromagnetic switching system, which includes a resonator on each input line.

To calculate the transfer matrix from the second input line to the output line, which relates the second input amplitudes to the output amplitudes, we proceed as follows:

Initially, the transfer matrix  $T_{G_2 R_3} T_{G_2}$  relates the amplitudes  $A_{24}$  and  $B_{24}$  to  $A_{21}$  and  $B_{21}$ :

$$\begin{pmatrix} A_{21} \\ B_{21} \end{pmatrix} = T_{G_2 R_3} T_{G_2} \begin{pmatrix} A_{24} \\ B_{24} \end{pmatrix}$$

Subsequently, the amplitudes  $A_{24}$  and  $B_{24}$  are connected to  $A_{25}$ ,  $B_{25}$ ,  $A_{29}$ , and  $B_{29}$  using the transfer matrix derived for the electromagnetic switch without resonators. This transfer matrix effectively links the input amplitudes of the second line to the output amplitudes:

$$\begin{pmatrix} A_{24} \\ B_{24} \end{pmatrix} = \begin{pmatrix} G_{21} & G_{22} & G_{23} & G_{24} \\ G_{25} & G_{26} & G_{27} & G_{28} \end{pmatrix} \begin{pmatrix} A_{25} \\ B_{25} \\ A_{29} \\ B_{29} \end{pmatrix}$$

The amplitudes  $A_{25}$  and  $B_{25}$  are related to the output amplitudes  $A_{28}$  and  $B_{28}$  via the transfer matrix  $T_{G_0 R_1} T_{G_0}$ :

$$\begin{pmatrix} A_{25} \\ B_{25} \end{pmatrix} = T_{G_0 R_1} T_{G_0} \begin{pmatrix} A_{28} \\ B_{28} \end{pmatrix}$$

By substituting the expression of  $\begin{pmatrix} A_{25} \\ B_{25} \end{pmatrix}$  into the transfer matrix equation, we obtain:

$$\begin{pmatrix} A_{24} \\ B_{24} \end{pmatrix} = \begin{pmatrix} G_{21} & G_{22} \\ G_{25} & G_{26} \end{pmatrix} T_{G_0 R_1} T_{G_0} \begin{pmatrix} A_{28} \\ B_{28} \end{pmatrix} + \begin{pmatrix} G_{23} & G_{24} \\ G_{27} & G_{28} \end{pmatrix} \begin{pmatrix} A_{29} \\ B_{29} \end{pmatrix}$$

Similarly, substituting the expression for  $\begin{pmatrix} A_{24} \\ B_{24} \end{pmatrix}$  back into the initial transfer equation,  $\begin{pmatrix} A_{21} \\ B_{21} \end{pmatrix} = T_{G_2 R_3} T_{G_2} \begin{pmatrix} A_{24} \\ B_{24} \end{pmatrix}$ :

$$\begin{pmatrix} A_{21} \\ B_{21} \end{pmatrix} = T_{G_2 R_3} T_{G_2} \left[ \begin{pmatrix} G_{21} & G_{22} \\ G_{25} & G_{26} \end{pmatrix} T_{G_0 R_1} T_{G_0} \begin{pmatrix} A_{28} \\ B_{28} \end{pmatrix} + \begin{pmatrix} G_{23} & G_{24} \\ G_{27} & G_{28} \end{pmatrix} \begin{pmatrix} A_{29} \\ B_{29} \end{pmatrix} \right]$$

Through matrix multiplication, the overall transfer matrix connecting the input amplitudes  $A_{21}$  and  $B_{21}$  from the second input line to the output amplitudes  $A_{28}$ ,  $B_{28}$ ,  $A_{29}$ , and  $B_{29}$  is obtained as:

$$\begin{pmatrix} A_{21} \\ B_{21} \end{pmatrix} = \begin{pmatrix} H_{21} & H_{22} & H_{23} & H_{24} \\ H_{25} & H_{26} & H_{27} & H_{28} \end{pmatrix} \begin{pmatrix} A_{28} \\ B_{28} \\ A_{29} \\ B_{29} \end{pmatrix} \quad (15)$$

Here, the matrix  $T_4 = \begin{pmatrix} H_{11} & H_{12} & H_{13} & H_{14} \\ H_{15} & H_{16} & H_{17} & H_{18} \end{pmatrix}$  repre-

sents the elements of the transfer matrix that connect the input amplitudes from the second input line to the output amplitudes in our electromagnetic switching system, which includes a resonator on each input line.

Using the matrices  $T_3$  and  $T_4$ , we obtain the following form of the global matrix for our proposed system with a resonator on each input line:

$$\begin{pmatrix} A_{11} \\ B_{11} \\ A_{21} \\ B_{21} \end{pmatrix} = T_{S_2} \begin{pmatrix} A_{18} \\ B_{18} \\ A_{19} \\ B_{19} \\ A_{28} \\ B_{28} \\ A_{29} \\ B_{29} \end{pmatrix} \quad (16)$$

$$\text{where } T_{S_2} = \begin{pmatrix} b_{11} & b_{12} & b_{13} & b_{14} & b_{15} & b_{16} & b_{17} & b_{18} \\ b_{21} & b_{22} & b_{23} & b_{24} & b_{25} & b_{26} & b_{27} & b_{28} \\ b_{31} & b_{32} & b_{33} & b_{34} & b_{35} & b_{36} & b_{37} & b_{38} \\ b_{41} & b_{42} & b_{43} & b_{44} & b_{45} & b_{46} & b_{47} & b_{48} \end{pmatrix}.$$

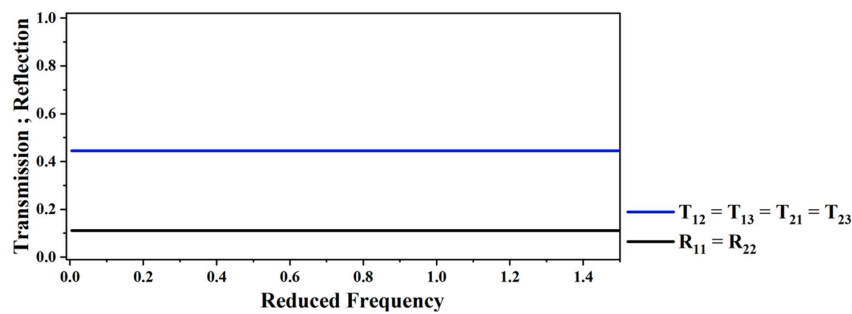
The transmission and reflection coefficients are represented by the following formulas:

$$\left\{ \begin{array}{l} t_{12} = \frac{A_{18}}{A_{11}} \Big) B_{18} = 0 \\ \quad B_{19} = 0 \\ \quad B_{28} = 0 \\ \quad B_{29} = 0 \\ t_{13} = \frac{A_{19}}{A_{11}} \Big) B_{18} = 0 \\ \quad B_{19} = 0 \\ \quad B_{28} = 0 \\ \quad B_{29} = 0 \\ r_{11} = \frac{B_{11}}{A_{11}} \Big) B_{18} = 0 \\ \quad B_{19} = 0 \\ \quad B_{28} = 0 \\ \quad B_{29} = 0 \\ t_{21} = \frac{A_{28}}{A_{21}} \Big) B_{18} = 0 \\ \quad B_{19} = 0 \\ \quad B_{28} = 0 \\ \quad B_{29} = 0 \\ t_{23} = \frac{A_{29}}{A_{21}} \Big) B_{18} = 0 \\ \quad B_{19} = 0 \\ \quad B_{28} = 0 \\ \quad B_{29} = 0 \\ r_{22} = \frac{B_{21}}{A_{21}} \Big) B_{18} = 0 \\ \quad B_{19} = 0 \\ \quad B_{28} = 0 \\ \quad B_{29} = 0 \end{array} \right. \quad (17)$$

where:

- $t_{12}$ : transmission from input channel 1 through input channel 2.
- $t_{13}$ : transmission from input channel 1 through output channel.
- $r_{11}$ : reflection from input channel 1.





**FIGURE 2.** Variation of the transmission and reflection rates of the electromagnetic switch system as function of reduced frequency [27].

- $t_{21}$ : transmission from input channel 2 through input channel 1.
- $t_{23}$ : transmission from input channel 2 through output channel.
- $r_{22}$ : reflection from input channel 2.

The transmission and reflection rates are expressed as follows:

$$\begin{cases} T_{12} = |t_{12}|^2 \\ T_{13} = |t_{13}|^2 \\ R_{11} = |r_{11}|^2 \\ T_{21} = |t_{21}|^2 \\ T_{23} = |t_{23}|^2 \\ R_{22} = |r_{22}|^2 \end{cases} \quad (18)$$

### 3. RESULTS AND DISCUSSIONS

In this study, we examine an electromagnetic switch with two input lines made of waveguides, and each is grafted by a resonator of lengths  $d_1$  and  $d_3$ , respectively, and one output channel that consists of semi-infinite segment (Fig. 1(b)). We use a relative dielectric permittivity  $\varepsilon = 2.3$  (polyethylene) and a relative magnetic permeability  $\mu = 1$  for the segments and resonators. In our calculations, we set the segment length as  $d_0 = 1D$ . The boundary condition at the ends of the resonators is  $E = 0$ , and the reduced frequency is  $\Omega = \frac{\omega\sqrt{\varepsilon\mu}}{c}D$ , where  $c$  is the speed of electromagnetic waves in a vacuum, and  $\omega$  represents the angular pulsation ( $s^{-1}$ ). We focus on frequencies in the MHz range for characteristic lengths in the meter range, and such a condition corresponds to very low attenuation; therefore, we neglect the imaginary part of dielectric permittivity.

#### 3.1. Analysis of the Electromagnetic Switch System without Resonator

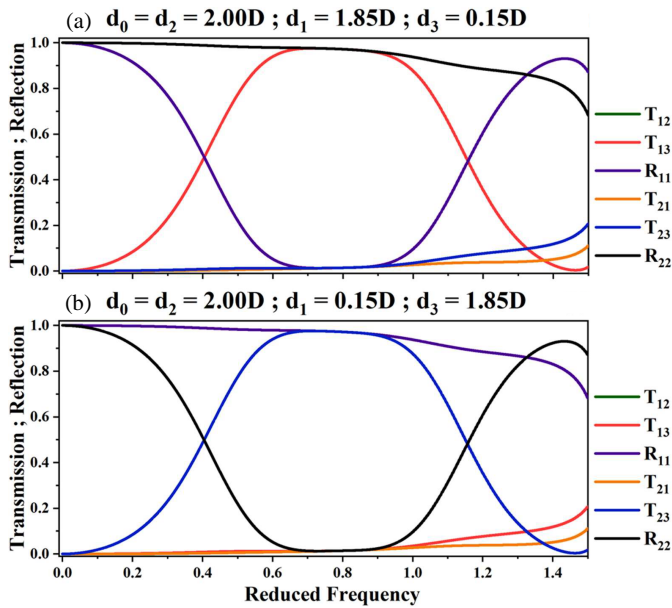
In this part, our objective is to analyze the transmission spectra:  $T_{12}$  from input channel 1 to output channel 2 (blue),  $T_{13}$  from input channel 1 to output channel (blue),  $T_{21}$  from input channel 2 to output channel 1 (blue), and  $T_{23}$  from input channel 2 to output channel (blue), as shown in Figure 2. Also, we analyze the reflection spectra:  $R_{11}$  in input channel 1 (black) and  $R_{22}$  in input channel 2 (black) of a Y-shaped electromagnetic switch system without a resonator as functions of the reduced frequency  $\Omega$ . In Fig. 2, we show that the transmission rates  $T_{12}$ ,

$T_{21}$ ,  $T_{13}$ , and  $T_{23}$  are steady at around 0.44 while the reflection rates  $R_{11}$  and  $R_{22}$  are about 0.11 showing that these rates are constant over the range of reduced frequencies  $\Omega = [0-1.5]$ . It indicates that the system is not efficiently directing the input electromagnetic wave to the single output, demonstrating the limitations of the switch without a resonator. Therefore, it is essential to add resonators to allow better control of electromagnetic wave propagation and improve switch performance by efficiently guiding the signal to the output. Similar results were found by El-Atmani et al. in their study of an acoustic switch, where they concluded that the addition of a resonator was essential to improving switch efficiency [21]. Moreover, in our recent work, we demonstrated that switches without resonators insufficiently controlled electromagnetic waves [27]. Introducing a resonator in input 1 transmits waves from input 2 to the output, but only for waves launched from input 2. In the present study, we place a resonator in each input line. The resonators in each input line allow electromagnetic waves from input 1 to reach the output while simultaneously blocking electromagnetic waves from input 2 at the output.

#### 3.2. The Effect of Resonator Heights $d_1$ and $d_2$ on Switch System Electromagnetic Wave

In this section, it is essential to understand the role of resonator heights  $d_1$  and  $d_3$  in controlling and directing electromagnetic waves in an electromagnetic switch system. Fig. 3 shows the transmission spectra:  $T_{13}$  from input channel 1 to output channel (red),  $T_{12}$  from input channel 1 to input channel 2 (green),  $T_{21}$  from input channel 2 to input channel 1 (orange), and  $T_{23}$  from input channel 2 to output channel (blue). It also examines the reflection spectra:  $R_{11}$  in input channel 1 (purple) and  $R_{22}$  in input channel 2 (black) as functions of the reduced frequency  $\Omega$  for  $d_0 = d_2 = 2.0D$ . The segment lengths  $d_0$  and  $d_2$  are kept constant while the resonator heights  $d_1$  and  $d_3$  are varied. The aim is to determine how adjusting the resonator lengths  $d_1$  and  $d_3$  to find matching conditions can direct electromagnetic waves, allowing passage from input 1 to the output ( $T_{13} = 1$ ) while blocking waves from input 2 ( $T_{23} = 0$ ) or vice versa ( $T_{23} = 1$ ,  $T_{13} = 0$ ).

In Fig. 3(a), with  $d_1 = 1.85D$  and  $d_3 = 0.15D$ , the transmission spectrum  $T_{13} = 0.97$  is observed within the frequency range  $\Omega = [0.66; 0.82]$ , while the transmission  $T_{23} = 0.01$  is minimized within the same range. This indicates that the system effectively transmits almost all electromagnetic waves



**FIGURE 3.** Variation of the transmission and reflection rates  $T_{12}$ ,  $T_{13}$ ,  $T_{21}$ ,  $T_{23}$ ,  $R_{11}$  and  $R_{22}$  of the electromagnetic switch as function of reduced frequency with  $d_0 = d_2 = 2D$ , for different values of the heights resonator  $d_1$  and  $d_3$ : (a)  $d_1 = 1.85D$  and  $d_3 = 0.15D$ ; (b)  $d_1 = 0.15D$  and  $d_3 = 1.85D$ .

from input 1 to the output (ON state) while blocking waves from input 2 to the output (OFF state). These results demonstrate the effectiveness of utilizing a taller resonator height  $d_1$  and a shorter resonator height  $d_3$  to achieve a precise switching behavior from the first input to the output channel. Conversely, in Fig. 3(b), with  $d_1 = 0.15D$  and  $d_3 = 1.85D$ , the transmission spectrum changes,  $T_{23} = 0.97$  within the frequency range  $\Omega = [0.66; 0.82]$ , while the transmission  $T_{13} = 0.01$  is minimized. This configuration indicates that the switch is ON for the transmission of electromagnetic waves from input 2 to output channel, while blocking waves from input 1 to output. These results show the essential role of precise adjustments to resonator heights  $d_1$  and  $d_3$  in the control of ON and OFF states, allowing efficient routing of electromagnetic waves in the switching system. The study concludes that for  $T_{13} = 1$  and  $T_{23} = 0$ , the condition  $d_1 \gg d_3$  must be satisfied, while for  $T_{13} = 0$  and  $T_{23} = 1$ ,  $d_1 \ll d_3$  is necessary. The generalized conditions are expressed as:  $d_1 = 1D + \delta$  and  $d_3 = 1D - \delta$ , where  $-1 < \delta < 1$ . This provides a simplified expression to study the effect of resonator height for optimal wave electromagnetic transmission control.

### 3.3. Adjustments of Resonator Height to Control the Electromagnetic Waves

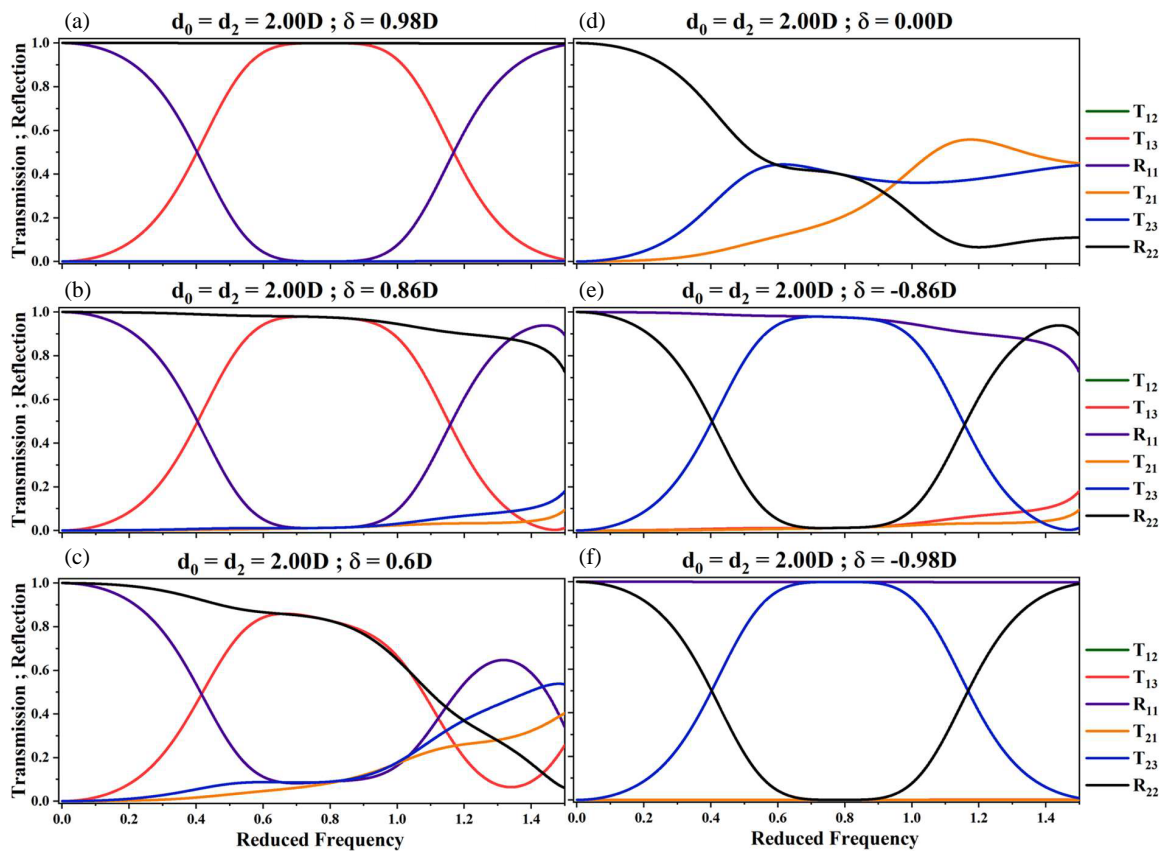
In this part, we examine the variation of the resonator heights  $d_1$  and  $d_3$  by applying the conditions  $d_1 = 1D + \delta$  and  $d_3 = 1D - \delta$ . Our aim is to achieve efficient switching between two states:  $T_{13} = 1$  and  $T_{23} = 0$  (where electromagnetic waves from input 1 are transmitted to the output (ON)), while waves from input 2 are blocked from the output (OFF)), or  $T_{13} = 0$  and  $T_{23} = 1$  (where waves from input 1 are blocked from the output (OFF), and waves from input 2 are transmitted to

the output (ON)). These states are achieved by adjusting  $\delta$  to control the switching behavior. Fig. 4 presents the transmission spectra:  $T_{13}$ ,  $T_{12}$ ,  $T_{21}$ ,  $T_{23}$  as well as the reflection spectra:  $R_{11}$  and  $R_{22}$  as functions of the reduced frequency  $\Omega$  with  $d_0 = d_2 = 2.0D$ . The segment lengths  $d_0$  and  $d_2$  are kept constant while the resonator heights  $d_1$  and  $d_3$  are varied by  $\delta$ .

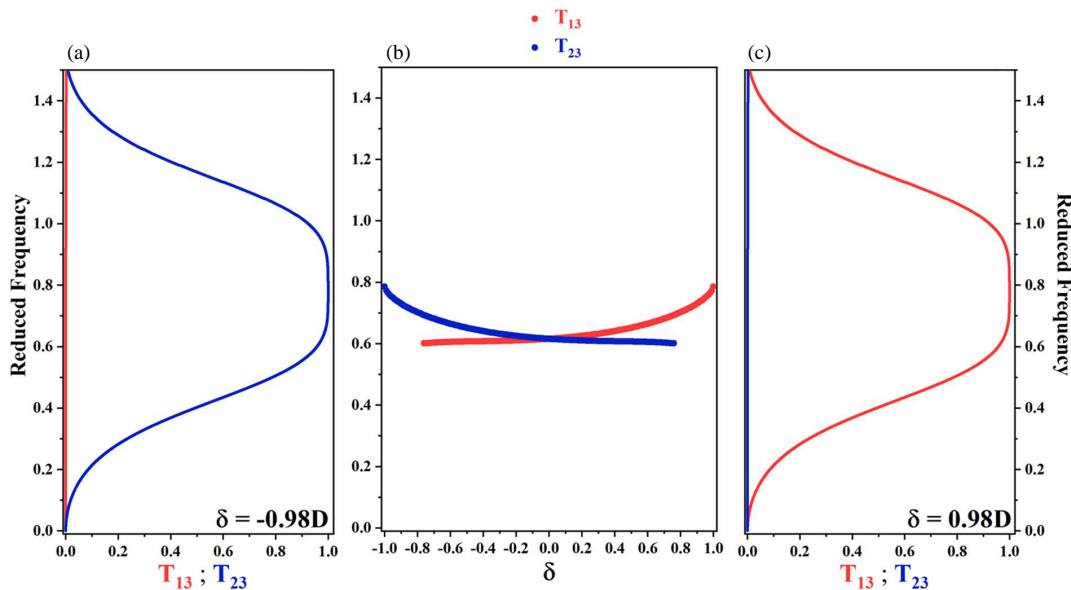
In Fig. 4(a) with  $\delta = 0.98D$ , transmission through the output line  $T_{13} = 1$  in the frequency range  $\Omega = [0.66; 0.82]$  demonstrates efficient switching, allowing complete transmission of electromagnetic waves from input 1 to the output (ON). At the same time,  $T_{23} = 0$  in the same frequency range confirms complete blocking of electromagnetic waves from input 2 to the output (OFF). Zero reflection  $R_{11} = 0$ , indicates that the system switches and efficiently directs electromagnetic waves from input 1 without significant losses. These states are obtained by ensuring  $d_1 \gg d_3$ . In Fig. 4(b) with  $\delta = 0.86D$ ,  $T_{13} = 0.97$  within the frequency range  $\Omega = [0.65; 0.85]$  indicates efficient switching, allowing nearly full transmission of electromagnetic waves from input 1 to the output. At the same time,  $T_{23} = 0.02$  almost completely blocks electromagnetic wave transmission from input 2 to the output. In Fig. 4(c), with  $\delta = 0.6D$ ,  $T_{13} = 0.8$  and  $T_{23} = 0.08$  show a partial distribution of electromagnetic energy at the output, with no clear ON/OFF state. The system is not very effective at switching, as the electromagnetic waves are not completely blocked or fully transmitted from input line 1 or 2 to the output line. In contrast, in Fig. 4(d), with  $\delta = 0D$ ,  $T_{13} = T_{23} = 0.66$ , the transmission of electromagnetic waves is distributed uniformly across the output line, without clear ON/OFF states. This indicates that there is ineffective switching behavior in the system as electromagnetic waves are transmitted equally from input 1 and input 2 to the output, making it impossible to control the direction of electromagnetic wave transmission. In Fig. 4(e), with  $\delta = -0.86D$ ,  $T_{23} = 0.97$  in the range frequency  $\Omega = [0.65; 0.85]$  indicates efficient switching, allowing nearly full transmission of electromagnetic waves from input 2 to output (ON), while  $T_{13} = 0.02$  reflects nearly complete blocking from input line 1 to output line. In Fig. 4(f), with a more negative  $\delta = -0.98D$ , the system shows its ability to fully reverse the electromagnetic wave transmission, enabling complete transmission from input line 2 to the output channel and total blocking from input line 1 to output line. The combined influence of  $d_1$  and  $d_3$  shows that adjusting the two resonator heights with  $\delta$  allows precise control of the direction of electromagnetic waves. With a positive  $\delta$ , ensuring  $d_1 \gg d_3$ , electromagnetic waves are transmitted from input 1 to output (ON), while blocking waves from input 2 (OFF). Conversely, with a negative  $\delta$ , ensuring  $d_1 \ll d_3$ , the behavior is reversed. By precisely adjusting these parameters, we can efficiently control the direction of electromagnetic waves and achieve precise ON/OFF switching.

### 3.4. Directional Control of Electromagnetic Waves: The Parameter $\delta$ Effect

Figure 5 illustrates that the reduced frequency of resonant modes varies with the parameter  $\delta$ . The red branches represent the maximum transmission  $T_{13}$ , while the blue branches indicate the maximum transmission  $T_{23}$ . As  $\delta$  increases positively,



**FIGURE 4.** Variation of the transmission and reflection rates  $T_{12}$ ,  $T_{13}$ ,  $T_{21}$ ,  $T_{23}$ ,  $R_{11}$  and  $R_{22}$  of the electromagnetic switch as function of reduced frequency, for different values of  $\delta$ : (a)  $\delta = 0.98D$ ; (b)  $\delta = 0.86D$ ; (c)  $\delta = 0.6D$ ; (d)  $\delta = 0.0D$ ; (e)  $\delta = -0.86D$ ; and (f)  $\delta = -0.98D$ .

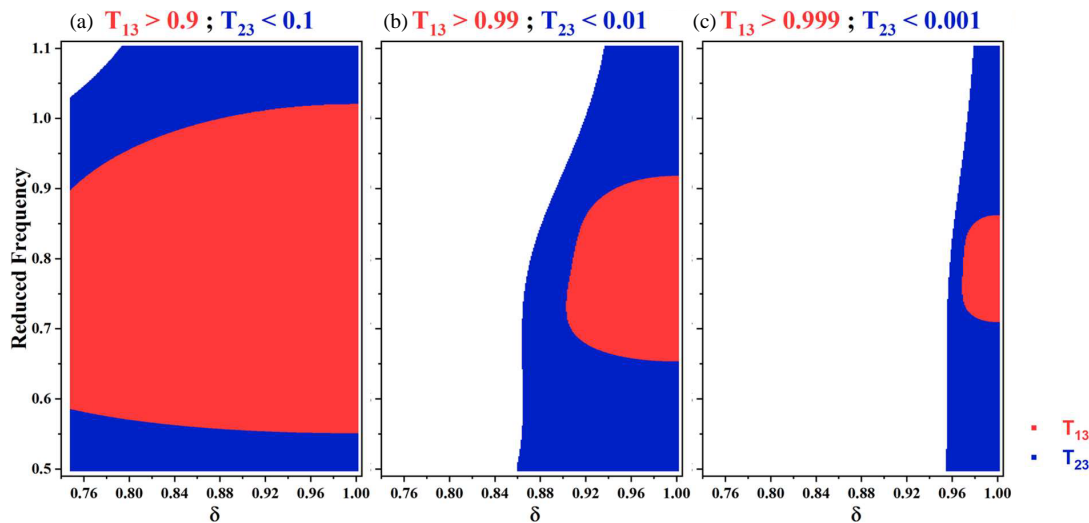


**FIGURE 5.** Variation of the reduced frequency as a function of the transmission rates  $T_{13}$  (red color),  $T_{23}$  (blue color) through the output line for: (a)  $\delta = -0.98D$  and (c)  $\delta = 0.98D$ . (b) Variation of the reduced frequency as function parameter  $\delta$ .

$T_{13}$  approaches 1 within specific frequency ranges, demonstrating efficient transmission from input 1 to the output line (ON), while  $T_{23}$  approaches 0, effectively blocking input 2 to output line (OFF). Conversely, when  $\delta$  takes on negative values,  $T_{23}$

nears 1, and  $T_{13}$  approaches 0, reversing the transmission direction. For intermediate values of  $\delta$  ( $\delta = 0$ ), two rates demonstrate a mixed transmission response, which reduces the clarity of the switching mechanism. This tunability of the coefficients





**FIGURE 6.** Electromagnetic switching efficiency: variation of maximum  $T_{13}$  and minimum  $T_{23}$  transmission rates as function parameter  $\delta$  for (a)  $T_{13} > 0.9$ , (b)  $T_{13} > 0.99$ , and (c)  $T_{13} > 0.999$ .

enables precise control over the direction of electromagnetic waves, facilitating reliable ON/OFF switching based on the selected coefficient value for effective electromagnetic control in our system.

### 3.5. Electromagnetic Switches with Parameter Positive $\delta$ for Maximum $T_{13}$ and Minimum $T_{23}$ Transmission Rates

In this study, we examine the operation of an electromagnetic switch that alternates between ON and OFF states (Fig. 6). This figure shows the maximum transmission  $T_{13}$  and the minimum  $T_{23}$ , giving important information about the switch's performance at different frequencies. We take the value of  $\delta$  positive to obtain the case allowing to transmit electromagnetic waves to pass from input 1 to the output ( $T_{13}$ ) in the state ON, while in the OFF state, it effectively blocks the waves from input 2 to the output ( $T_{23}$ ), resulting in minimal or no transmission. The figure represents the different maximum transmission values of  $T_{13}$  (red area) and different minimum transmission values of  $T_{23}$  (blue area) providing insights into the system's switching behavior across various frequencies. Based on the analysis of these curves, the parameter  $\delta$  is changed to maximize the functionality of the switch. We use specific transmission thresholds:  $T_{13} > 0.9$ ,  $T_{13} > 0.99$ ,  $T_{13} > 0.999$  for  $T_{13}$ , and  $T_{23} < 0.1$ ,  $T_{23} < 0.01$ , and  $T_{23} < 0.001$  for  $T_{23}$ , to characterize the system's switching capabilities. In the first case (Fig. 6(a)), the red area indicates that the transmission reaches a maximum of 90% around  $\delta = 1$ , in the frequency range [0.4–1.1]. In the second case (Fig. 6(b)), the red area shows that the transmission reaches a maximum of 99% around  $\delta = 1$ , in the frequency range [0.5–0.91]. Finally, in the third case (Fig. 6(c)), the red area indicates that the transmission reaches a maximum of 99.9% around  $\delta = 1$ , in the frequency range [0.7–0.85]. These results demonstrate how increasing the switching rate affects performance within the same frequency range. Moreover, adjusting the resonator heights helps optimize the

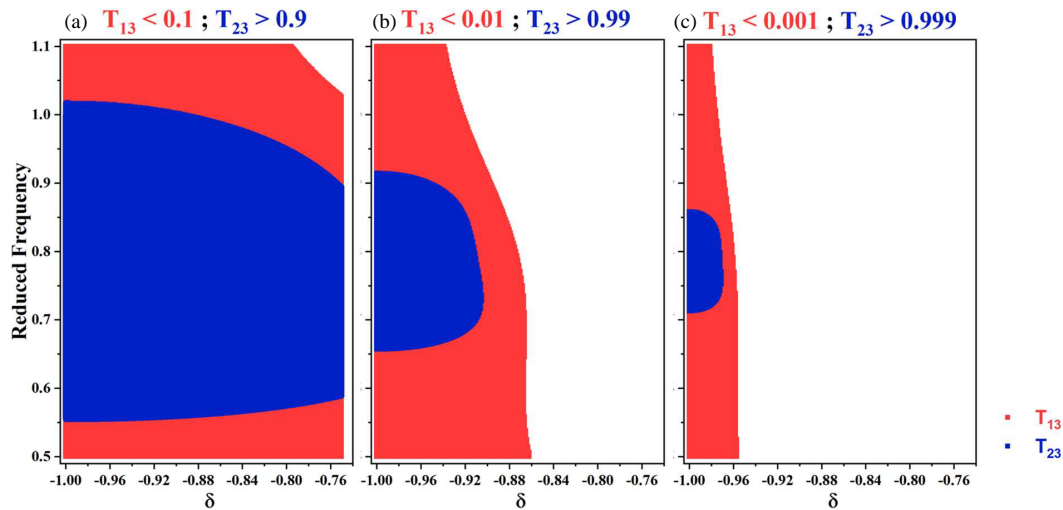
switching rate in specific frequency intervals. This shows that the switch rate is a crucial performance indicator, reflecting the system's ability to meet the required transmission thresholds in the output lines. Similar findings were reported by El-Atmani et al. in their study of an acoustic switch, where they observed comparable results [26].

### 3.6. Electromagnetic Switch Efficiency with Negative Parameter $\delta$ for Maximum $T_{23}$ and Minimum $T_{13}$ Transmission Rates

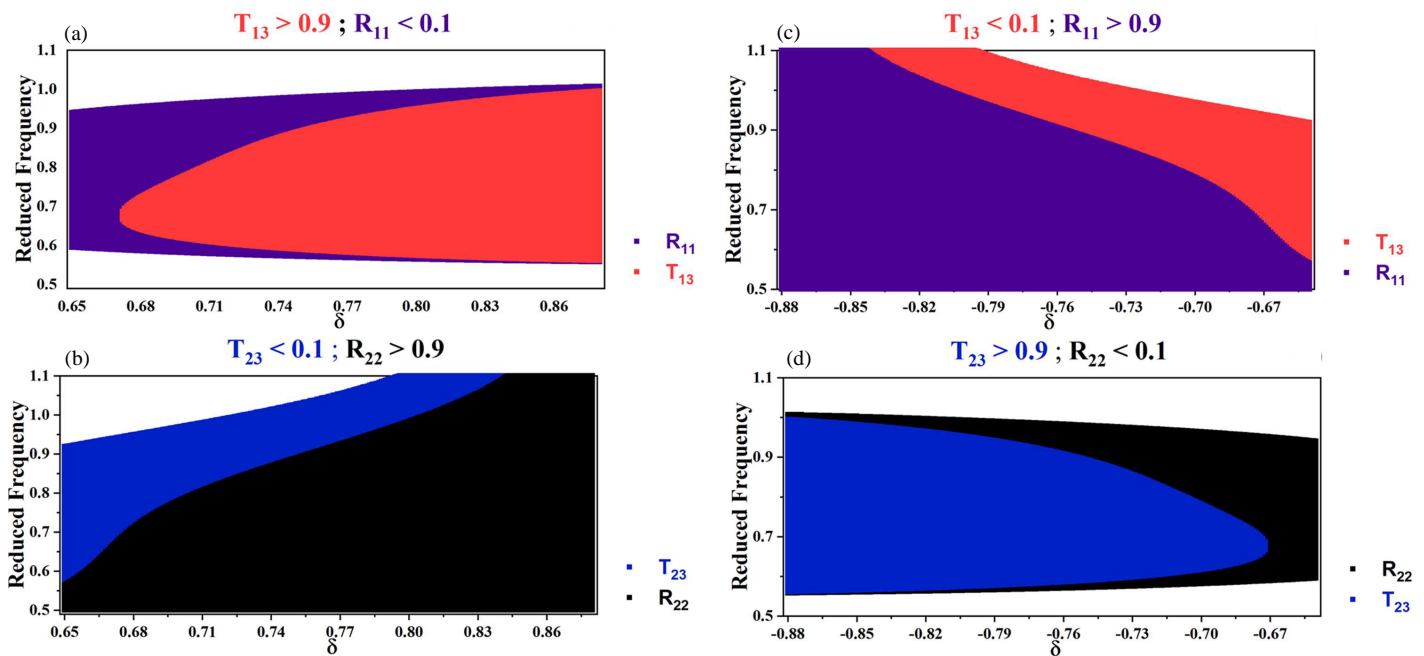
In this study, we examine the reduced frequency as a function of the negative value of  $\delta$  (Fig. 7), facilitating the understanding of the system's behavior. In this inverse case, compared to the situation shown in Fig. 6 where  $\delta$  is positive, the system allows electromagnetic waves to pass from input 2 to the output ( $T_{23}$ ) in the ON state, while blocking the waves from input 1 to the output ( $T_{13}$ ) in the OFF state. The figure displays maximum transmission values of  $T_{23}$  (blue area) and minimum values of  $T_{13}$  (red area), providing insights into the system's switching behavior. Transmission thresholds are used to characterize performance, with  $T_{23} > 0.9$ ,  $T_{23} > 0.99$ ,  $T_{23} > 0.999$  for  $T_{23}$ , and  $T_{13} < 0.1$ ,  $T_{13} < 0.01$ , and  $T_{13} < 0.001$  for  $T_{13}$ . The analysis demonstrates that adjusting the resonator heights improves switching rate efficiency within specific frequency ranges.

### 3.7. Analysis of Electromagnetic Switching Behavior Based on Positive and Negative $\delta$

In this section, we analyze the behavior of an electromagnetic switch (ON/OFF) that operates selectively based on the sign of parameter  $\delta$ . For positive  $\delta$ , where the condition  $d_1 \gg d_3$  realized, the switch allows the transmission  $T_{13}$  of electromagnetic waves from input 1 to the output, while simultaneously blocking transmission  $T_{23}$  of waves from input 2 to output. Conversely, for negative  $\delta$ , where  $d_1 \ll d_3$ , the system permits transmission  $T_{23}$  of electromagnetic waves from input 2 to the output and blocks transmission  $T_{13}$  of waves from input 1 to



**FIGURE 7.** Electromagnetic switching efficiency: variation of maximum  $T_{23}$  and minimum  $T_{13}$  transmission rates as function parameter  $\delta$  for (a)  $T_{23} > 0.9$ , (b)  $T_{23} > 0.99$ , and (c)  $T_{23} > 0.999$ .



**FIGURE 8.** Schematic representation and behavioural analysis of electromagnetic switching.

output. The colored area in the figures (Fig. 8) corresponds to specific operational thresholds of the switch. For positive  $\delta$ , the red area ( $T_{13}$ ) indicates maximum transmission through output; the blue area ( $T_{23}$ ) represents minimum transmission through output; the black area ( $R_{22}$ ) indicates maximum reflection from input 2; and the purple area represents minimum reflection ( $R_{11}$ ) from input 1. For negative  $\delta$ , the behavior shifts: the red area indicates minimum transmission ( $T_{13}$ ) through output; the blue area represents maximum transmission ( $T_{23}$ ) from input 2 through output; the black area indicates minimum reflection ( $R_{22}$ ) from input 2, while the purple area highlights maximum reflection ( $R_{11}$ ) from input 1.

In Fig. 8(a), under the desired thresholds transmission and reflection  $T_{13} > 0.9$  and  $R_{11} < 0.1$  with positive value of pa-

rameter  $\delta$ , the switch effectively transmits waves from input 1 to output, showing stable behavior in a range of reduced frequency specific. In Fig. 8(b), with  $T_{23} < 0.1$  and  $R_{22} > 0.1$ , the system blocks waves from input 1, confirming strong reflection. For negative value of parameter  $\delta$ , Fig. 8(c) demonstrates that  $T_{13} < 0.1$  and  $R_{11} > 0.9$ , meaning that the system primarily reflects waves from input 1. In Fig. 8(d), where  $T_{23} > 0.9$  and  $R_{22} < 0.1$ , the system allows efficient transmission from input 2 to output, demonstrating the versatility of the switch. In summary, the system effectively switches between transmission and reflection based on the sign and value of  $\delta$ , ensuring precise control over wave propagation in both ON and OFF states.

## 4. CONCLUSION

The purpose of this paper was to present and analyze a Y-shaped electromagnetic waveguide switch that enables the efficient and precise control of electromagnetic wave propagation. Our investigation confirmed that this switch can achieve selective transmission from one input channel to the output while effectively blocking the other input or inverse, depending on the resonator configurations. By using Transfer Matrix Method (TMM), we observed that adjusting the resonator heights and segment lengths within the waveguide structure enabled near-total transmission in the ON state, achieving rates above 99%, while maintaining minimal transmission (below 1%) in the OFF state. These results highlight the critical role of resonator tuning in achieving the desired switching behavior and demonstrate the effectiveness of our design for applications that require high levels of signal precision and control. The study further indicates that the system's performance can be optimized over a wider frequency range by adjusting the resonator characteristics, suggesting that the switch is adaptable for broader spectral applications. This adaptability, combined with the switch's high transmission efficiency, underscores its potential for integration into optical communication systems. Future perspectives include experimental validations to verify theoretical outcomes and adjustments to enhance frequency versatility, making the switch a strong candidate for advanced signal processing and telecommunications applications that demand reliable wave directionality and adaptability.

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